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# NAVAL POSTGRADUATE SCHOOL

## Monterey, California



# THESIS

N 63653

EXTENSION OF AGGREGATION AND SHRINKAGE  
TECHNIQUES USED IN THE ESTIMATION OF  
MARINE CORPS OFFICER ATTRITION RATES

by

John M. Misiewicz

September 1989

Thesis Advisor:

Robert R. Read

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Extension of Aggregation and  
Shrinkage Techniques Used in  
the Estimation of Marine Corps  
Officer Attrition Rates

by

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requirements for the degree of

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## ABSTRACT

In this thesis we treat the "small cell" problem encountered when building an attrition rate generator for large-scale manpower flow models, specifically for the USMC Officer Corps. Such models have a large number of low-inventory (i.e. small) personnel cells. This presents a dilemma: on one hand we want to preserve as much fidelity as possible in our work by preserving a great deal of detail in each cell; on the other hand our statistical estimation techniques require larger cell sample sizes than intrinsically occur cell-by-cell in actual sample data. Our approach to producing stable attrition rates for such cells involves two efforts: (i) the aggregation of cells into groups that exhibit homogeneity of attrition behavior, and (ii) the development of "shrinkage" estimation techniques for use in the individual groups. A heuristic algorithm is developed and tested to treat the aggregation problem. Empirical Bayes methods are developed to serve the multi-cell estimation requirements needed to preserve the fidelity. Cross validation techniques are used to verify these methods.

The present work builds upon the results of previous studies; we integrate what was learned into a coherent package that is ready for use.

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## THESIS DISCLAIMER

The reader is cautioned that computer programs developed in this research may not have been exercised for all cases of interest. While every effort has been made, within the time available, to ensure that the programs are free of computational and logic errors, they cannot be considered validated. Any application of these programs without additional verification is at the risk of the user.

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## I. INTRODUCTION

### A. GENERAL

The Officer Planning and Utility System (OPUS), a comprehensive and fully integrated manpower management system, is currently being implemented by the U.S. Marine Corps (Decision System Associates, 1986). This system contains a set of computer-based manpower planning models and is used by the Officer Plans Section (MPP-30), Headquarters, U.S. Marine Corps, to produce several manpower planning documents. The system must be able to accurately predict personnel attrition, i.e., officers leaving the service for purposes such as resignation, retirement, discharge, disability, or release. The forecasting of attrition is accomplished by the Marine Corps Officer Rate Projector (MCORP), developed by the Navy Personnel Research and Development Center (NPRDC), San Diego, California (NPRDC, 1985).

The attrition rate generator developed by NPRDC calculates empirical attrition rates using historical data with user-defined weights and threshold parameters (Siegel, 1983). This subjective input makes the current generator susceptible to unintentional misuse.

In support of MCORP, Professor Robert R. Read of the Naval Postgraduate School has been working on the "small cell" problem: applying multiparameter statistical estimation schemes to estimating attrition when there is low personnel inventory, or small cells, which generally exhibit unstable empirical rates.

A comment on terminology is in order. By attrition rate generator we mean methodology for estimating attrition probabilities for the various cells. The expression "empirical rates" refers to the ratio of leavers to inventory for each cell, unmodified by any information contained in "neighboring" cells. In contrast to this, the expression "empirical Bayes" refers to Bayes estimators whose prior parameters are estimated from data.

Accurate forecasting of losses is extremely important to the manpower planner. Overestimating losses causes excess accessions, promotion delays, underutilized personnel and increased costs, while underestimation causes personnel shortages and decreased readiness. The problem is compounded in that all but a few accessions must start at the bottom, i.e., Second Lieutenant, and work their way up to the higher ranks only after many years of service. For example, if a shortage of Lieutenant Colonels arises, it can

only be remedied by promoting more Majors, which has a rippling effect down the rank structure.

## **B. BACKGROUND**

There have been seven Master's theses over the past four years which have studied various aspects of the attrition estimation problem. A concise summary of these works is given by Read (NPS Report NPS55-88-006, 1988, pp.16-23). These studies can be grouped into three general areas: shrinkage methods, cell aggregation and peripheral studies.

The application of a shrinkage method begins by identifying a number of personnel inventory cells, followed by the development of the empirical rates for individual cells and a weighted grand mean of these empirical rates. The final estimate for a cell is a convex combination of its empirical rate and the grand mean. There are numerous methods for accomplishing this, several of which have been applied in previous studies.

Tucker was the first to investigate the application of these methods to attrition estimation. He compared traditional estimators to the James-Stein estimator and the minimax estimator for a few selected grades and occupational fields. His results gave strong support to the James-Stein estimator; minimax was discarded as being too conservative for small cell use. However, there remained pockets of instability for which goodness-of-fit tests failed. (Tucker, 1985)

Following Tucker was Robinson, who introduced the Efron-Morris limited translation shrinkage alternative to augment the James-Stein estimator. These methods were evaluated with a broader set of test cases. Robinson was able to confirm Tucker's results, but the limited translation option failed to provide any consistent relief in the unstable areas. (Robinson, 1986)

The final application of shrinkage methods to estimating officer attrition rates was undertaken by Dickinson. He applied the previously used methods and an empirical Bayes estimator to a new and refined data base. Improved results were obtained, but the instability remained. Dickinson also performed some exploratory side studies dealing with the Freeman-Tukey transform and the use of empirical Bayes methods that allow non-uniform shrinkage, both of which provided the impetus for the present study. (Dickinson, 1988)

These three studies used ad hoc methods to deal with the second general area of study--cell aggregation. Aggregation of cells with low personnel inventory into sets of cells, often of larger inventory, is required when applying these shrinkage methods. The

desire is to use cells which exhibit similar attrition behavior. Two previous studies have investigated this area.

Amin Elseramegy used the Classification and Regression Trees (CA $\tilde{R}$ T) program, which at the time was newly acquired by the Naval Postgraduate School, in an attempt to form aggregates of cells that exhibited homogeneous attrition behavior. Several difficulties in using this program were encountered, e.g., because of insufficient memory allocation he found it necessary to partition the data base into nine sets and apply CART to each. The resulting aggregations were generally unusable. (Amin Elseramegy, 1985)

Major breakthroughs in cell aggregation were made by Larsen. He applied a hierarchical clustering algorithm to the new data base. The resulting rules for building aggregates are well defined and especially viable from an intuitive point of view. Larsen's work provides the framework for the cell aggregation method developed in Chapter II of this thesis. (Larsen, 1987)

The remaining two theses of the seven were peripheral studies which applied alternate methods to attrition estimation. Hogan attempted multi-year forecasting using exponential smoothing; the smoothing constants were rather unusual and extreme and his results inconsistent (Hogan, 1986). Yacin applied logistic regression in the attempt to develop an attrition rate scheme; the only new results were the identification of some areas that exhibited similar attrition behavior (Yacin, 1987).

This thesis is the first to integrate the two main areas of study. Whereas previous studies of shrinkage methods have used ad hoc aggregation schemes, we now combine the implementation of a defensible aggregation method with empirical Bayes estimators. Moreover, these are applied to a larger and more refined data base. The results have been quite promising in that we have achieved greater stability in attrition rate estimation; we have defined guidelines for a heuristically appealing aggregation scheme; and we have acquired an increased understanding of the data base and developed more efficient ways to use it.

### C. ORGANIZATION

The remainder of this introductory chapter provides a more detailed description of the small cell problem and the data base. The aggregation problem is discussed and the proposed aggregation method is presented in Chapter II.

The shrinkage estimation methods, generally classified as empirical Bayes type estimators, are described in Chapter III. Several variations are presented to allow



comparison and to gain further insight into their performance. Testing of these methods is important but for practical purposes must be carried out using sampling methods. The rationale used to select test cases, the cross validation techniques, and the measures of effectiveness used to evaluate the results are discussed in Chapter IV. A discussion of the results of the cross validation is also included in this chapter.

Finally, conclusions and recommendations based on these results are contained in Chapter V.

#### **D. SMALL CELL PROBLEM**

Marine Corps officers can be classified and thus partitioned by several attributes. The major partitioning of officers is by grade, years commissioned service (YCS), and military occupational specialty (MOS). Grade describes the position an officer holds in the service. The numbers of officers in each higher grade have a pyramid structure, i.e., there are more officers in the lower grades than in the higher grades. YCS is the total number of years served since becoming a commissioned officer. There is a strong correlation between grade and YCS since an officer generally moves up the grade structure as he gains in YCS. MOS is a four-digit code identifying the specific skill for which a Marine is trained. MOS need not remain constant over an officer's career, although most changes in MOS occur in the early years of commissioned service. An officer has a single primary MOS, however as he develops new job skills he may be assigned one or more additional MOSs.

For many purposes, partitioning by grade, YCS and MOS is sufficient. However in some applications additional refinement by service component, commissioning source, sex, race or education level may be necessary. Service component consists of three categories: regular officers, reserve officers, and reserves who have augmented to become regulars. It is strongly correlated with commissioning source, i.e., an officer receives a regular or reserve commission depending upon the commissioning source. Both affect an officer's initial service obligation, which is generally three to five years (except aviators, whose obligation is dependent upon the amount of flight training). Officers who receive a reserve commission normally serve three to four years active duty (except aviators), by the end of which they must have either augmented into the regular force or are then separated from active service.

These cross-classifications may be viewed as breaking the officer population into a multidimensional array, with each specific intersection of the classifications called a cell. The total number of possible cells is quite large, on the order of  $10^6$ . Many of these cells

are structurally infeasible in that no officer could possibly fit the cell characteristics, e.g., there are no Majors with two years commissioned service. The total officer inventory of approximately 20,000 officers is partitioned by the remaining feasible cells; some cells have inventory as large as 50, however most have less than five. An officer's characteristics are dynamic, i.e., as an officer moves through the grade, YCS and MOS structure he moves from one cell to another. As a result, the inventory of the feasible cells is also dynamic and fluctuates between zero and low inventory (less than five) over time.

These sparsely populated cells have very unstable empirical attrition rates. For example, a cell whose inventory is two officers of which one leaves the service during a given time period yields a 50% empirical attrition rate, whereas a cell whose inventory is one officer who remains in service during the same time period yields a 0% attrition rate. It is obvious that neither of these empirical estimations provides a usable attrition rate. Furthermore, these two rates could change dramatically during the next time period, typifying their instability.

Even when more modern estimation techniques (e.g. shrinkage) are applied, these small cells can still create statistical instability, thereby producing intolerably variable attrition rate estimates. The problem then is how to deal with these low inventory cells, or "small cells" in order to achieve stability.

## **E. DATA BASE**

In this thesis we benefit from a refined data base compiled by NPRDC and made available to the Naval Postgraduate School in 1987. This data base, used by Larsen in his aggregation work (Larsen, 1987), was not available for the previous estimation studies at NPS.

The new data base provides more detailed information about the officer population. The grade structure now allows separation of Limited Duty Officers (LDO) as well as Warrant Officers (WO) from unrestricted officers. Officers who have failed selection to the next higher grade can also be identified. YCS is listed instead of length of service (LOS), which became ambiguous when dealing with officers who have prior enlisted service. MOS can now be broken out completely into 236 MOSs or summarized by the 39 occupational fields. Service component and commissioning source are both new categories. Other new categories that are not considered here are education level, race, additional MOSs, and military schools completed. Larsen gives a complete description of the classifications (Larsen, 1987, pp.66-82).



The data base also allows attrition to be broken out by retirement, release, discharge, resignation, etc., but for our immediate purpose we are only concerned with the total number of losses for any reason.

This refinement of the data presents a dichotomy: we can now break the data into more definitive cells to search for homogeneous attrition behavior and stability in estimation, but this leads to an even greater number of low inventory cells.

The new data base contains ten years of inventory and attrition data from the period 1977-1986, a significant improvement from the previous seven year data base covering the period 1977-1983. The inventory data is now obtained from quarterly vice yearly snap-shots of the officer population. The attrition data is annualized, i.e., the attrition count for a cell reflects the number of personnel who leave the service at any time during the year. Attritions are credited to the cell which the officer occupies at the time he leaves.

Two problems arise from this quarterly versus annualized data. First, it is possible for a cell to record zero inventory via the snap-shots, yet be credited with one or more attritions. To avoid this situation, the cell inventory used in all calculations is defined to be the larger of the inventory and the attrition count. This ensures that the inventory for a cell is at least as large as its recorded number of leavers. (This override occurs infrequently; a more sophisticated treatment would require significant model enhancement.) Second, to use the inventory and attrition data together we must divide the inventory data by four. This poses a philosophical problem when invoking a binomial model: the sample size may not be integral. However, for our application the usual mean and variance formulas are usable and can still serve in the interpolative sense.

## II. CELL AGGREGATION

### A. GENERAL

The aggregation problem takes on new meaning with the use of shrinkage estimators. Originally, aggregation had only one concern: how to pool cells together into a **single** cell in order to meet a user-defined minimum inventory threshold. This single aggregated cell was then used to determine the attrition rate estimate for the original, unaggregated cell. In this way an estimated value for a cell is obtained by using the grand mean for many cells.

The empirical Bayes multiparameter estimation techniques provide a way to compromise, using both the stability of a grand mean and the specific information of an individual cell. Now we pool cells together and obtain a **number** of cells that meet the user-defined minimum inventory threshold. It is important to note that we should be able to use a lower inventory threshold with empirical Bayes, thus retaining individual cell behavior to a greater extent. It is also important to use cells with homogeneous attrition behavior in the aggregation process.

### B. BACKGROUND

The aggregation method currently used by MCORP is called the Small Cell Override Methodology (NPRDC, 1985, Appendix H). It is used to solve the original aggregation problem, i.e., if a cell is below the user-defined threshold, then cells are adjoined to the original cell until the threshold is met. The process for selecting cells for adjunction is rather crude, and large-scale with only a few levels (prior to using the entire officer corps). The attrition rate estimate for the original cell is the empirical rate from this aggregated cell.

To begin the process, the user defines a cell for which an attrition rate estimate is required by grade, YCS and MOS. The user also defines the minimum cell inventory threshold (and other parameters which are not relevant here). If the cell he identifies meets the threshold, no aggregation is required and the empirical attrition rate is determined. If the cell is below the threshold, additional cells must be added until the threshold is met.

This search for additional cells occurs by expanding by YCS and MOS, with grade remaining fixed throughout. Expanding in this sense means changing the YCS or MOS parameter to identify the additional cells to be added to the original cell. Initially, the

single cell is expanded by YCS. For example, if the original cell's grade/YCS/MOS was Capt/7/0802, the cells identified by Capt/6/0802, Capt/8/0802, etc., are added sequentially until the threshold is met. This YCS expansion has an upper bound at the 20 YCS point; an obvious boundary for attrition behavior due to retirement eligibility. If the original cell's YCS is above 20, then 20 would serve as the lower YCS bound.

If the threshold is not met after the YCS expansion, the override method starts over with the original cell and expands by MOS. Each MOS belongs to one of nine MOS groups which are defined along traditional Marine Corps functional areas, e.g., all helicopter pilot MOSs are grouped together as are all combat support MOSs. MOS expansion adds those cells identified by the MOSs in the same MOS group as the MOS of the original cell for the original YCS and grade. If the threshold is not met, all the MOSs in the MOS group are expanded by YCS in the same manner as the YCS expansion discussed previously.

If this MOS group and YCS expansion is unsuccessful, the override method starts over with the original cell and expands by all MOSs for the original grade and YCS. If necessary, all the MOSs are expanded by YCS as before.

Cell aggregation using this expansion method can potentially include all MOSs and YCS bounded only at the 20 year point. The desire to aggregate using cells with homogeneous attrition behavior is obviously compromised. Larsen provides a more comprehensive description of the current method (Larsen, 1987, pp.16-22).

Larsen examined attrition behavior in the MOS and YCS structure. He applied a hierarchical clustering algorithm in an attempt to find MOSs and YCSs that displayed homogeneous attrition behavior. He confirmed the belief that YCS is an important factor. The YCS expansion bounds he proposed reflect points at which officers reach the end of their initial service obligation as well as when they are eligible for retirement, which makes them especially viable from an intuitive point of view. Larsen also found that some MOSs did not cluster strictly by functional areas. This was especially significant in the aviation community. Whereas the previous data base allowed aviators to be considered only as one occupational field, the refined MOS information was able to identify six distinct homogeneous groups of aviators.

Larsen uses these results to define more refined MOS groups and YCS boundaries. To avoid the giant expansion leap from MOS group to all MOSs, he proposed a hierarchy of small MOS groups, large MOS groups and major MOS groups developed by observing which MOSs tend to exhibit similar attrition behavior. Homogeneity is greatest within the MOS group, and becomes successively worse as we move to the large



MOS group and then the major MOS group. Each MOS is assigned to a small MOS group. Small MOS groups combine to make a large MOS group, and large MOS groups combine to make a major MOS group.

Each small MOS group is assigned a set of YCS expansion bounds. Due to the different attrition behavior of the small MOS groups with respect to YCS, three different sets of YCS expansion bounds are proposed.

Initial expansion is by YCS within the specified boundaries, with grade and MOS held constant. If more expansion is required, we retain this aggregated cell and expand by small MOS group for the original grade and YCS. If the aggregated cell is still below the threshold, the MOSs in the small MOS group are expanded by YCS. Subsequent expansion to large MOS group and YCS, and major MOS group and YCS is accomplished until the threshold cell inventory is met.

Unlike the current expansion method, expansion using Larsen's proposed method will not cross defined MOS groups or YCS bounds to ever include all MOSs and YCSs bounded only at the 20 year point. Larsen provides a more detailed description of his recommended expansion rules (Larsen, 1987, pp.45-61).

### **C. EXPANSION METHOD**

We now address the methods used to obtain the cells required for use with empirical Bayes estimation techniques. Expansion continues to mean finding more cells to be used, however we no longer simply add these cells to the original cell to form a single aggregated cell. The cells identified by the expansion process are now aggregated together to produce a number of cells. After the discussion of the expansion process in this section, an actual aggregation scheme is introduced in the next section.

To begin the estimation process, the manpower planner defines a specific cell by grade, YCS and MOS. The attributes service component and commissioning source are also included as possible cell descriptors for the purposes of this study. All other descriptors listed in the data base--sex, education level, additional MOSs, race and military schools--are ignored. Loss types are considered as a combined total, i.e., in this study we do not discriminate among the various types of losses. The first three user-defined descriptors--grade, YCS and MOS--are single-value inputs. The last two descriptors, service component and commissioning source, can be single values, or either one of them can be treated as a vector of values for each single cell. This vector is collapsed (total the components) during the aggregation process, i.e., all records which meet any of the vector's values are included in the same cell. As in the previously described expansion

methods, only YCS and MOS change during expansion, the remaining cell descriptors remain constant.

To use shrinkage techniques, the amount of expansion required not only depends upon the minimum cell inventory threshold but also upon a new input parameter: the threshold number of cells. These two parameters are denoted:

1.  $T_0$  - cell inventory threshold. The minimum average inventory for a cell obtained by averaging the cell inventory over the ten years of data.
2.  $K_0$  - threshold number of cells. The minimum number of aggregated cells whose inventory exceeds  $T_0$ . These aggregated cells are the input cells for the empirical Bayes techniques.

For example, if  $T_0 = 5.0$  and  $K_0 = 10$ , the expansion algorithm continues until at least ten aggregated cells, each with average inventory 5.0 or larger are obtained. Since we are concerned primarily with the small cell problem the values of  $T_0$  and  $K_0$  used are selected to range from five to 30. It is also presumed that  $T_0$  is less than or equal to  $K_0$ . These threshold values can certainly exceed 30 for other applications, however the resulting cells are not considered small and their attrition behavior most likely would not be as unstable, therefore not requiring special attention.

Prior to explaining the expansion process, we first define the MOS groups and YCS bounds. We have adopted much of Larsen's work in this area; many of the changes are minor but are necessary for implementation purposes.

The general idea of a hierarchy of MOS groups is repeated, as shown in Table 1. Each MOS belongs to a small MOS group, a large MOS group and a major MOS group. Listed are 14 small MOS groups, which combine to make six large MOS groups, which combine to make four major MOS groups. For example, small MOS groups one and two form large MOS group one, and small MOS groups three through six form large MOS group two. Large MOS groups one and two, which collectively contain small MOS groups one through six, make up major MOS group one. Major MOS group one contains only ground MOSs, and major MOS group two contains only aviation MOSs. Major MOS groups three and four are special cases as discussed below.

A subjective decision was made to keep the ground MOSs in groups defined along the more traditional functional areas. This is reflected in small MOS groups one through six. For estimation purposes it is advantageous if the cell inventories are not too variable in size (Carter and Rolph, 1974, p.882). It is also desirable to avoid having too many MOSs in each small MOS group. This allows the expansion to occur more gradually, and is especially important for small values of  $T_0$  and  $K_0$ . As a result, MOS 0302

**Table 1. MOS GROUPS**

Group Name	MOSs	Small MOS Group	Large MOS Group	Major MOS Group		
Combat	0302	1	1	1		
Combat Support	0802 1302 1802 1803	2				
Combat Service 1	0180 0202 2502 2602	3	2			
Combat Service 2	3415 4002 4302 5803	4				
Combat Logistics	0402 3002 3060 3502 6002	5				
Air Control	7204 7208 7210 7320	6				
Fixed Wing Pilots	7501 7511 7522 7542 7543 7545 7576	7	3	2		
F-18 Pilots	7521 7523	8				
Rotary Wing Pilots +	7556 7557 7562 7564 7565 7566 7587	9	4			
Naval Flight Officers +	7508 7509 7563 7581 7583 7584 7585 7586 7588	10				
Basic Ground	0101 0201 0301 0401 0801 1301 1801 2501 2601 3001 3401 3501 4001 4301 4401 5801 6001 7201 7301 9901	11	5	3		
	Student Aviators				7580 7597 7598 7599	12
	Basic Pilots				7500 7510 7520 7540 7550 7560 7575	13
	Lawyers				4402	14

(infantry) is placed alone in a small MOS group. This MOS contains approximately 15% of the total officer population, and therefore its respective cells normally contain large inventory. The MOSs in small MOS group two also contain fairly large inventory, therefore are grouped together and their first expansion is with MOS 0302. The remaining ground MOSs in small MOS groups three through six have similarly small inventory.

The aviation small MOS groups (seven through ten) remain relatively unchanged from Larsen's recommendations. MOS 7564 (CH-53 pilot), was removed from a ground MOS group and added to small MOS group nine, which reflects its functional area. MOSs 7551 (C-9 pilot), 7552 (TC-4C pilot), 7555 (UC-12B pilot) and 7559 (CT-39 pilot)



were deleted since they are not primary MOSs. MOS 7530 (basic pilot VMFA (F-4)) was deleted since it is not a current MOS. (MCO P1200.7G, 1988)

Officers who have not acquired sufficient schooling or field experience to qualify for a primary MOS listed in small MOS groups one through ten are gathered together as basic officers or students in small MOS groups 11-13. These officers are generally second lieutenants or junior first lieutenants with three or fewer YCS. They are disregarded for the remainder of the study because their attrition rates are extremely low; probably because none of the officers in these groups have reached the end of their initial obligations.

MOS 4402 (lawyers) is considered a special case and is not addressed in this study.

All MOSs listed in Table 1 are primary MOSs for unrestricted officers as listed in the current Military Occupational Specialties Manual (MCO P1200.7G, 1988). It would be a logical and relatively simple extension of this table to create additional groups containing LDO and WO MOSs. These grades are not considered in this study and therefore their respective MOSs are excluded from the table.

Several of these seemingly ad hoc decisions to alter Larsen's recommended MOS groups are due to the YCS expansion bounds shown in Table 2. Every effort was made to group MOSs with similar YCS expansion bounds to allow for feasible implementation of the expansion algorithm. This is especially applicable when expanding to large and major MOS groups.

**Table 2. YCS EXPANSION BOUNDS**

MOS Group	Small MOS Groups	Bounded YCS Groups
Fixed Wing Pilots, F-18 Pilots, Lawyers	7, 8, 14	(1-6, 8-19) (7) (20-25) (26)
Rotary Wing Pilots, Naval Flight Officers	9, 10	(1-5, 8-19) (6,7) (20-25) (26)
All Others	1-6, 11-13	(1-3, 6-19) (4,5) (20-25) (26)

The YCS expansion bounds reflect the maximum expansion allowed from the initial YCS defined by the user. For example, if the original cell's grade/YCS/MOS is Capt/9/7501, we see from Table 1 that this MOS belongs to small MOS group seven. Thus its YCS expansion bounds are listed on the first line of Table 2. The value of nine

for YCS falls in the first YCS range, thus we could expand using all YCSs from one through 19, excluding seven. If the YCS for this original cell had been seven, **no** YCS expansion would be allowed.

These YCS expansion bounds are used with the MOS groups to define the additional cells which can be used with the original cell to obtain the required number of cells,  $K_0$ , each with minimum average inventory,  $T_0$ . The expansion stages are:

1. Stage 1 - Locate the small MOS group which contains the user-defined MOS. The initial cells are those specified by the MOSs in this group for the user-defined YCS, grade, service component and commissioning source (grade, service component and commissioning source remain fixed throughout the expansion process and thus are not repeated). These cells are aggregated to obtain cells with average inventory greater than or equal to  $T_0$ . After aggregation, if the number of cells is greater than  $K_0$ , stop, otherwise go to Stage 2.
2. Stage 2 - Expand by incrementing YCS (YCS-1, YCS+1, YCS-2, YCS+2, etc.) within the YCS bounds listed in Table 2 for all MOSs in the small MOS group. After **each** YCS increment, aggregate the cells to obtain cells with average inventory greater than or equal to  $T_0$ . After aggregation, if the number of cells is greater than  $K_0$ , stop, otherwise continue to increment by YCS. If the YCS bounds are reached before obtaining enough aggregated cells, retain the cells identified in Stages 1 and 2 and go to Stage 3.
3. Stage 3 - Expand to the large MOS group for the **single** user-defined YCS. Aggregate the cells to obtain cells with average inventory greater than or equal to  $T_0$ . After aggregation, if the number of cells is greater than  $K_0$ , stop, otherwise go to Stage 4.
4. Stage 4 - Expand by incrementing YCS for the large MOS group. After **each** YCS increment, aggregate the cells to obtain cells with average inventory greater than or equal to  $T_0$ . After aggregation, if the number of cells is greater than  $K_0$ , stop, otherwise continue to increment by YCS. If the YCS bounds are reached before obtaining enough aggregated cells, retain the cells identified in Stages 1 through 4 and go to Stage 5.
5. Stage 5 - Expand to the major MOS group for the **single** user-defined YCS. Aggregate the cells to obtain cells with average inventory greater than or equal to  $T_0$ . After aggregation, if the number of cells is greater than  $K_0$ , stop, otherwise go to Stage 6.
6. Stage 6 - Expand by incrementing YCS for the major MOS group. After **each** YCS increment, aggregate the cells to obtain cells with average inventory greater than or equal to  $T_0$ . After aggregation, if the number of cells is greater than  $K_0$ , stop, otherwise continue to increment by YCS. If the YCS bounds are reached before obtaining enough aggregated cells, **stop**. No more expansion is allowed. Inform the user that the thresholds are unattainable. Do not cross any major MOS group or YCS bounds.

Two points about the expansion process are emphasized. First, we retain the cells identified by all previous stages as we progress to the next stage. As stated before, the degree of homogeneity decreases as we move from small to large to major MOS groups.

Thus we want to locate as many cells from the small MOS group as possible before we expand to the large MOS group, and then locate as many cells from the large MOS group as possible before expanding to the major MOS group. The YCS expansion for each group may be different, e.g., the small MOS group may be expanded by all YCSs within the given YCS range, but the large MOS group may only be expanded by a few YCSs before the thresholds are attained.

The second point is that, when aggregating cells, any aggregation that was performed previously is discarded and all cells currently identified are pooled and made available for aggregation. This affords the aggregation algorithm greater flexibility and could create more aggregated cells than if the aggregated cells from previous stages were left intact, thereby keeping the amount of expansion to a minimum.

The aviation small MOS groups (seven through ten) make up the only major MOS group (two) that contains different YCS bounds, i.e., small MOS groups seven and eight have different YCS expansion with regard to year six than do small MOS groups nine and ten. To implement the expansion algorithm in a computer program, this difference is overcome by using the YCS bounds for the original user-defined MOS. For example, suppose MOS 7501 from small MOS group seven is the original MOS. If MOS expansion continues into the major MOS group, the MOSs in small MOS groups nine and ten would follow small MOS group seven's YCS expansion bounds.

In summary, this method of grouping MOSs should provide greater homogeneity among cells which are used in estimating attrition rates. Unlike the current method, ground and aviation MOSs are never used together. The YCS bounds provide a logical and effective way to treat periods of different attrition behavior. However, the greater the expansion the less homogeneous the cells become, which should be kept foremost in mind when setting the threshold parameters.

#### **D. AGGREGATION METHOD**

While the expansion steps are being undertaken in order to achieve the threshold levels specified by the user, those cells with inventory less than  $T_0$  must be gathered up into larger, aggregated cells whose combined inventory exceeds  $T_0$ . In order to limit the expansion to as few additional MOSs and YCSs as possible, we desire to maximize the number of aggregated cells obtained at any stage of the expansion.

The term maximization suggests the possible use of linear programming (LP). While an LP would ensure maximization, this would not be a trivial problem to solve, i.e., the LP relaxation would almost certainly fractionate cells, using their inventory in more than

one aggregated cell. This is not allowed since a cell may be assigned intact to only one aggregated cell. Thus an integer LP would be required which would typically contain 500 or more integer variables. This method would not be expedient in terms of computer usage, especially considering the potential number of integer LPs that may have to be solved for a single estimation cycle.

While we are trying to maximize the number of aggregated cells, it would be satisfactory to obtain close to the maximum if we could preclude the expense in computer time required by an integer LP. For this reason, a heuristic “greedy” algorithm was developed. Complete descriptions of the heuristic algorithm and the LP formulation are contained in Appendix A. The performance of this heuristic is discussed along with the results of the empirical Bayes methods in Chapter IV.



### III. ESTIMATION METHODS

#### A. GENERAL

Once the cell aggregation phase is completed, we begin the attrition rate estimation process. The following notation is used to define the cell data

$$\begin{aligned} K &= \text{number of cells} \\ T &= \text{number of years of data.} \end{aligned} \tag{1}$$

Then for  $i = 1, \dots, K$  and  $t = 1, \dots, T$

$$\begin{aligned} N_i(t) &= \text{inventory of cell } i \text{ in year } t \\ Y_i(t) &= \text{number of attritions in cell } i \text{ in year } t. \end{aligned} \tag{2}$$

The cell data is assumed to be independent binomial, i.e.,  $Y_i(t) \sim \text{Bin}(N_i(t), p_i)$ . A success is defined to be an attrition, i.e., an officer from that cell leaves the service during the year. The empirical attrition rate for cell  $i$  is given by the Maximum Likelihood Estimator (MLE)

$$\hat{p}_i = \frac{\sum_t Y_i(t)}{\sum_t N_i(t)}. \tag{3}$$

This estimate of  $p$  works well for cells with large inventory, but not those with small inventory, which is most often the case in our application.

The MLE has been shown to be dominated by shrinkage methods for  $K \geq 3$  (Carter and Rolph, 1974; Efron and Morris, 1975; Casella, 1985). These methods find a grand mean or central attrition rate for the group of cells and a shrinkage factor for each cell. Previous theses have primarily used a common shrinkage factor for all cells; we now allow this shrinkage factor to vary from cell to cell. Each cell's MLE is shrunk towards the central rate by its shrinkage factor. In this way, attrition information from one cell "spills over" into other cells.

The shrinkage methods are developed under the theoretical assumption that the data is normally distributed. Most of the previous studies using empirical Bayes methods have used independent normal data with constant variance (Efron and Morris, 1972,

1973, 1975; Dickinson, 1988). Some applications have used binomial data, using a transformation to make it behave more like normal data (Carter and Rolph, 1974; Efron and Morris, 1975). In Carter and Rolph's estimation of fire alarm probabilities, transformation of the binomial data did not have a large effect on the results (Carter and Rolph, 1974). Our application allows us to investigate the impact of the transformation when applied with more extreme values of  $p$ .

Six variations of the empirical Bayes method are applied to the attrition rate estimation problem. The first four are similar in that they use the same iterative procedure to compute the amount of shrinkage for each cell. Of these four, two are on the transformed scale and two on the original scale. Each scale includes two methods of computing the cell variance: one method where the variance is time dependent and the other where it is time independent. The two variance calculations, if they produce like results, provide supporting evidence for the assumption that the data is independent and identically distributed over time. This assumption is certainly questionable, since an officer who remains in a given MOS will move through the YCS and grade cell structure in a predictable manner. As a result, variance that is constant in time (time independent) may not perform as well as one that allows for time variation. The fifth method uses a different iterative procedure to determine the amount of shrinkage and is addressed separately in paragraph III.C.. The final method breaks the cell data into its vector components (service component or commissioning source) before shrinkage techniques are applied and is addressed in paragraph III.D..

## B. EMPIRICAL BAYES

### 1. Transformed Scale

We begin our application of empirical Bayes methods on the transformed scale in an effort to overcome some of the weaknesses in our assumptions. The transformation we use is the Freeman-Tukey transform, a modification of the basic arcsin transformation for binomial data. Its purpose is to stabilize the variance at one and make the data behave more like normal random variables. The form used is

$$X_i(t) = \frac{1}{2} \sqrt{N_i(t) + .5} \left\{ \arcsin\left(\frac{2Y_i(t)}{N_i(t) + 1} - 1\right) + \arcsin\left(2 \frac{Y_i(t) + 1}{N_i(t) + 1} - 1\right) \right\}. \quad (4)$$



Now, let

$$XT_i(t) = \frac{X_i(t)}{\sqrt{N_i(t) + .5}} \quad \text{for } t = 1, \dots, T_i \quad (5)$$

except when  $N_i(t) = 0$  (no inventory in year  $t$ ), in which case  $XT_i(t)$  does not exist and we reduce  $T_i$  by one. The time average of the transformed values for cell  $i$  becomes

$$XTB_i = \frac{1}{T_i} \sum_t XT_i(t). \quad (6)$$

We now need to compute the variance of these time averages. Two methods are used: the first calculation is time dependent, i.e., the variance changes over time, the second is time independent.

The transform stabilizes the variance at one for large values of  $n$  and non-extreme values of  $p$ . These requirements on  $n$  and  $p$  are often violated in our application, therefore we have many combinations of  $n$  and  $p$  for which the variance is less than one. Dickinson was able to discover an interpolative formula which provides a good approximation for the variance of the transformed values,  $X_i(t)$ , for small values of  $n$  and  $p$ , and  $K \geq 3$  (Dickinson, 1988, pp.8-11). This variance is given by

$$Var(X_i(t)) = \min\{1, V(X_i(t))\} \quad (7)$$

where  $V(X_i(t))$  is found by solving

$$V(X_i(t)) = a(X_i(t) + C)^{b_1} (X_i(t) + C - 1)^{b_2} \quad (8)$$

with

$$C = \sqrt{N_i(t) + .5} \left( \frac{\pi}{2} \right) \quad (9)$$

and

$$a = 1.6835 \quad b_1 = -.8934 \quad b_2 = .9881. \quad (10)$$

Equation (8) obviously breaks down if  $X_i(t) + C < 1$ . When this occurs, we set  $X_i(t) + C = 1.001$  and continue. The effect is to use a small but positive variance. The

value of one in Equation (7) dominates for about  $X_i(t) + C \geq 2.2$ . The variance of the time average is then

$$Var(XTB_i) = \frac{1}{T_i^2} \sum_t Var(XT_i(t)) = \frac{1}{T_i^2} \sum_t \frac{Var(X_i(t))}{N_i(t) + .5} . \quad (11)$$

The second method of computing the variance is the more familiar one. Continuing from Equation (6), the variance of the transformed values is given by

$$Var(XT_i) = \frac{1}{T_i - 1} \sum_t (XT_i(t) - XTB_i)^2 . \quad (12)$$

The variance of their average is therefore

$$Var(XTB_i) = \frac{1}{T_i} Var(XT_i) . \quad (13)$$

Regardless of which variance calculation we use, the same iterative algorithm is used to determine the empirical Bayes estimate for each cell. This estimate,  $XEB_i$ , is found by solving

$$XEB_i = \frac{A}{A + Var(XTB_i)} XTB_i + \frac{Var(XTB_i)}{A + Var(XTB_i)} XBB \quad (14)$$

where  $XEB_i$ ,  $XTB_i$  and  $Var(XTB_i)$  are cell specific,  $XBB$  is the (weighted) grand mean or central attrition rate, and  $A$  is the variance of the prior distribution of the cell means. These latter two values must be estimated simultaneously using the following iterative algorithm.

We initialize the algorithm with  $A = 0$  and store the previous value of  $A$  by

$$A_0 \leftarrow A . \quad (15)$$

Now compute the (weighted) grand mean,  $XBB$ . Let

$$\alpha_i = \frac{1}{A + Var(XTB_i)} \quad (16)$$

and

$$\gamma_i = \frac{\alpha_i}{\sum_{j=1}^K \alpha_j} . \quad (17)$$

Then

$$XBB = \sum_{i=1}^K \gamma_i XTB_i . \quad (18)$$

The updated value of  $A$  becomes

$$A \leftarrow A - \frac{K - 1 - \sum_{i=1}^K \alpha_i (XTB_i - XBB)^2}{\sum_{i=1}^K \alpha_i^2 (XTB_i - XBB)^2} . \quad (19)$$

If  $A \leq 0$ , set  $A = 0$  and exit. This represents the case when there is 100% shrinkage toward the grand mean. If  $A > 0$ , then check  $|A - A_0| < \varepsilon$  (e.g.,  $\varepsilon = .0001$ ). If false, return to Equation (15) for another iteration. If true, the iterations have converged. Exit with the current values of  $A$  and  $XBB$  for use in Equation (14) to solve for the  $XEB_i$ .

Close study of Equation (14) shows that the amount of shrinkage changes from cell to cell since the variance terms are generally not equal. Specifically, cells with higher variance are shrunk more than those with lower variance. In addition, if  $A$  is small the shrinkage is greater towards  $XBB$ . As  $A \rightarrow \infty$ , the shrinkage is minimal and the individual cell means dominate.

Once the  $XEB_i$  are determined, these values must be transformed back to the original scale. We use

$$\hat{p}_i = \frac{1}{2} \{1 + \sin(XEB_i)\} . \quad (20)$$

## 2. Original Scale

We return to the assumption of binomial data for original scale calculations. As in the transformed scale, two methods to calculate the variance are used. We begin

with

$$XT_i(t) = \hat{p}_i(t) = \frac{Y_i(t)}{N_i(t)}. \quad (21)$$

As before, if  $N_i(t) = 0$  (no inventory in year  $t$ ),  $XT_i(t)$  does not exist and we reduce  $T_i$  by one. This leads to the time average for cell  $i$  as

$$XTB_i = \frac{1}{T_i} \sum_t XT_i(t) = \frac{1}{T_i} \sum_t \hat{p}_i(t). \quad (22)$$

The variance calculation which is time dependent, i.e., changes over time, is given by

$$Var(XTB_i) = \frac{1}{T_i^2} \sum_t Var(XT_i(t)) = \frac{1}{T_i^2} \sum_t \frac{\hat{p}_i(t)(1 - \hat{p}_i(t))}{N_i(t)}. \quad (23)$$

We return to Equation (15) with these variance values to perform the iterative algorithm for finding the empirical Bayes estimate,  $XEB_i$ , given by Equation (14). Since we are already in the original scale, the transformation given in Equation (20) is ignored, i.e.,  $\hat{p}_i = XEB_i$ .

A problem arises while performing the iterations if a cell has  $Y_i(t) = 0 \ \forall t$  (zero attrition for every year). In this case, the variance given by Equation (23) equals zero. When this value is used in Equation (16), the formula for  $\alpha_i$  becomes undefined. We resolve this problem using the Laplace Law of Succession. Assume that  $Y_i(t) \sim Bin(N_i(t), p_i)$  and let

$$p_i^* = \frac{Y_i(t) + 1}{N_i(t) + 1} \quad \text{and} \quad q_i^* = \frac{N_i(t) - Y_i(t)}{N_i(t) + 1} \quad (24)$$

be the estimates as prescribed by this law, i.e., Bayes estimator using uniform prior. Then

$$Var\left(\frac{Y_i(t)}{N_i(t)}\right) = \frac{p_i^* q_i^*}{N_i(t)} = \frac{\left(\frac{Y_i(t) + 1}{N_i(t) + 1}\right)\left(\frac{N_i(t) - Y_i(t)}{N_i(t) + 1}\right)}{N_i(t)}. \quad (25)$$

If  $Y_i(t) = 0$ , then

$$Var\left(\frac{Y_i(t)}{N_i(t)}\right) = \frac{\left(\frac{1}{N_i(t)+1}\right)\left(\frac{N_i(t)}{N_i(t)+1}\right)}{N_i(t)} = \frac{1}{(N_i(t)+1)^2} . \quad (26)$$

This value is used as the summand in Equation (23) whenever  $Y_i(t) = 0$  (zero attrition in any year).

For comparison purposes we again compute an alternate variance which is time independent. Continuing from Equation (22), let

$$\tilde{p}_i = \frac{\sum_t Y_i(t)}{\sum_t N_i(t)} . \quad (27)$$

The alternate variance is given by

$$Var(XTB_i) = \frac{1}{T_i^2} \sum_t Var(XT_i(t)) = \frac{\tilde{p}_i(1-\tilde{p}_i)}{T_i^2} \sum_t \frac{1}{N_i(t)} . \quad (28)$$

The problem with cells that have  $Y_i(t) = 0 \ \forall t$  (zero attrition for every year) also occurs here, since the variance given by Equation (28) would equal zero. Using the same concept as before, we obtain the formula

$$Var(XTB_i) = \frac{\sum_t N_i(t)}{\left(1 + \sum_t N_i(t)\right)^2} \frac{1}{T_i^2} \sum_t \frac{1}{N_i(t)} . \quad (29)$$

However in this case, this variance formula is necessary only if all years have zero attrition.

As before, we return to Equation (15) to perform the iterative algorithm for finding the empirical Bayes estimate,  $XEB_i$ , given by Equation (14).



### C. EFRON-MORRIS METHOD

This method is a modification of the iterative algorithm used to estimate  $A$  and  $XBB$  given by Efron and Morris (Efron and Morris, 1973, pp.127-129). It differs from the method given by Equations (14) through (19) in that it allows the variance of the prior,  $A$ , to change from cell to cell. It also gives greater weight to the cells with low variance, and reduces to the James-Stein estimator when the cell variances are constant.

Only one scenario for this method is considered, corresponding to the initial transformed scale, time dependent variance case. Thus, Equations (4) through (11) are repeated, and we begin from the point where we are entering the iterative algorithm. To simplify the following equations, let  $D_i = Var(XTB_i)$  as given by Equation (11).

We initialize the algorithm with  $A_i = 0$  and  $SP_i = 0$  (previous values of  $S$ ) for  $i = 1, \dots, K$ . Let

$$\alpha_i = \frac{1}{A_i + D_i} \quad (30)$$

and

$$\gamma_i = \frac{\alpha_i}{\sum_{j=1}^K \alpha_j} \quad (31)$$

Then

$$\hat{X} = \sum_{i=1}^K \gamma_i XTB_i \quad (32)$$

and

$$S_i = (XTB_i - \hat{X})^2 \quad (33)$$

Now set  $i = 1$  and let

$$SN_i = \sum_{j \neq i} \frac{S_j - D_j}{(A_j + D_j)^2} \quad (34)$$

and

$$SD_i = \sum_{j \neq i} \frac{1}{(A_j + D_j)^2} . \quad (35)$$

We then use the Newton-Raphson iteration method to solve

$$A_i = \frac{(S_i - 3D_i) + (A_i + D_i)^2 SN_i}{3 + (A_i + D_i)^2 SD_i} = g(A_i) . \quad (36)$$

First set  $AP_i \leftarrow A_i$  for  $i = 1, \dots, K$  (previous values of  $A_i$ ). The updated value for  $A_i$  becomes

$$A_i \leftarrow A_i - \frac{A_i - g(A_i)}{1 - g'(A_i)} . \quad (37)$$

If  $A_i \leq 0$ , set  $A_i = 0$ , let  $i = i + 1$ , and return to Equation (34). If  $A_i > 0$ , then test  $|A_i - AP_i| > \varepsilon$ . If true, return to Equation (36). If false, let  $i = i + 1$  and return to Equation (34).

In either case after incrementing  $i$ , if  $i = K + 1$ , we exit and test  $|S_i - SP_i| < \varepsilon \ \forall i$ . If false, we update  $SP_i \leftarrow S_i$  and return to Equation (30) with updated values of  $A_i$ . If true, the iterations have converged and we must finalize the estimators,  $XEM_i$ . Let

$$d_i^* = 3 + (A_i + D_i)^2 \sum_{j \neq i} \frac{1}{(A_j + D_j)^2} \quad (38)$$

and

$$B_i = \left(1 - \frac{4}{d_i^*}\right) \frac{D_i}{A_i + D_i} . \quad (39)$$

If  $B_i > 1$ , set  $B_i = 1$ , or if  $B_i < 0$ , set  $B_i = 0$ . Then

$$XEM_i = \hat{X} + (1 - B_i)(XTB_i - \hat{X}) . \quad (40)$$

This equation is comparable to Equation (14), which was used to determine the transformed scale estimates,  $XEB_i$ , using the previous iterative algorithm. The quantity  $B_i$  is

the amount of shrinkage toward the grand mean,  $\hat{X}$ . The corresponding quantity in Equation (14) is  $\frac{Var(XTB_i)}{A + Var(XTB_i)}$ .

To obtain  $\hat{p}_i$ , the  $XEM_i$  must be transformed back to the original scale using  $XEM_i$  in place of  $XEB_i$  in Equation (20).

#### D. VECTOR METHOD

This method is similar to the previous methods in the sense that it uses the aggregated cells produced to meet the defined threshold levels. However, prior to the estimation process, we now partition each aggregated cell by either service component or commissioning source, thus obtaining cells whose elements are vectors. The procedure given by Efron and Morris, modified to compensate for the assumed variance of the time averages, provides the framework for this method (Efron and Morris, 1972, pp.341-344).

The separation by service component or commissioning source requires us to define a third index: the components of the vector. Let

$$P = \text{number of service components/commissioning sources.} \quad (41)$$

Then for  $i = 1, \dots, K, j = 1, \dots, P$  and  $t = 1, \dots, T$

$$\begin{aligned} N_{ij}(t) &= \text{inventory of cell } i \text{ and vector component } j \text{ in year } t \\ Y_{ij}(t) &= \text{number of attritions in cell } i \text{ and vector component } j \text{ in year } t. \end{aligned} \quad (42)$$

Before we had  $K$  cells with scalar information, but now we need a  $K \times P$  matrix where

$$\sum_{j=1}^P N_{ij}(t) = N_i(t) \quad \text{and} \quad \sum_{j=1}^P Y_{ij}(t) = Y_i(t). \quad (43)$$

A requirement for this method is that  $K > P + 2$ , for reasons that will soon become obvious.

We begin by defining  $X_{ij}(t)$  as the transformed value for  $N_{ij}(t)$  and  $Y_{ij}(t)$  as given by Equation (4). Continuing in similar manner as the previous transformed scale methods, let

$$XT_{ij}(t) = \frac{X_{ij}(t)}{\sqrt{N_{ij}(t) + .5}} \quad \text{for } t = 1, \dots, T_{ij} \quad (44)$$

except when  $N_{ij}(t) = 0$ , in which case  $XT_{ij}(t)$  does not exist and we reduce  $T_{ij}$  by one.

The time averages of the transformed values are then

$$XTB_{ij} = \frac{1}{T_{ij}} \sum_t XT_{ij}(t). \quad (45)$$

Here we obtain a vector of grand mean values, with each of the  $P$  grand means defined by

$$XBB_j = \frac{1}{K} \sum_{i=1}^K XTB_{ij}. \quad (46)$$

The transformed scale estimate,  $\delta_{ji}$ , is then found by solving

$$\delta_{ji} = XBB_j + \{I_P - (K - P - 2)\tilde{S}^{-1}\}(XTB_{ji} - XBB_j) \quad (47)$$

where  $I_P$  is the identity matrix of order  $P$ , and  $\tilde{S}^{-1}$  is found as discussed below. Reversal of the  $ij$  index in this and subsequent equations simply means the transpose of the  $K \times P$  matrix to a  $P \times K$  matrix.

To solve for  $\tilde{S}^{-1}$ , we begin by defining

$$\tilde{S} = X_{ji}X_{ji}^T \quad (48)$$

where

$$X_{ji} = (XTB_{ji} - XBB_j)\sqrt{V_{ji}}. \quad (49)$$

The  $V_{ji}$  matrix is the modification required by our application. (The multiplication in Equation (49) is element-wise as opposed to normal matrix multiplication.) The Efron and Morris method was developed under the assumption that  $XTB_{ij} \sim N(\theta_{ij}, 1)$ , whereas we are using

$$XTB_{ij} \sim N\left(\theta_{ij}, \frac{1}{T_{ij}^2} \sum_t \frac{1}{N_{ij}(t) + .5}\right) \quad (50)$$

provided that  $XT_{ij}(t)$  has variance of one. Therefore



$$V_{ij} = \frac{1}{T_{ij}^2} \sum_i \frac{1}{N_{ij}(i) + .5} . \quad (51)$$

We use the requirement that the  $P \times P$  matrix resulting from the operations within the brackets in Equation (47) must be nonnegative definite to solve for  $\tilde{S}^{-1}$  without having to actually compute its inverse. We proceed by doing an eigenanalysis of  $\tilde{S}$ , which is seen by Equation (48) to be a real symmetric matrix. We form the diagonal matrix  $E$ , which has the eigenvalues,  $e_j$ , as its diagonal elements, and the matrix  $\Gamma$ , which has the corresponding eigenvectors as its columns. For any  $e_j < (K - P - 2)$ , we replace it with the value  $(K - P - 2)$ . The eigenanalysis provides us with the solution to

$$\begin{aligned} \tilde{S} \Gamma_j &= \Gamma_j e_j \\ \text{or } \tilde{S} \Gamma &= \Gamma E . \end{aligned} \quad (52)$$

Post-multiplying by  $\Gamma^T$ , we obtain

$$\tilde{S} = \Gamma E \Gamma^T \quad (53)$$

since  $\Gamma$  is ortho-normal and therefore  $\Gamma \Gamma^T = I_p$ . We then have

$$\tilde{S}^{-1} = (\Gamma E \Gamma^T)^{-1} = \Gamma E^{-1} \Gamma^T \quad (54)$$

which is easily solved since  $E^{-1}$  is found by replacing the diagonal elements of  $E$  by their reciprocal. This solution for  $\tilde{S}^{-1}$  is then used in Equation (47) to solve for the transformed scale estimates,  $\delta_{ji}$ . To obtain the attrition rate estimate for a cell,  $\hat{p}_{ji}$ , we use the inversion formula given by Equation (20) with  $\delta_{ji}$  in place of  $XEB_i$ .

## IV. CROSS VALIDATION

### A. GENERAL

The six estimation methods discussed in Chapter III are evaluated using cross validation of the data base. This consists of successively holding out one year's data while the other nine years are used to estimate that year's attrition rates. Three measures of effectiveness (MOEs) are used to evaluate the validity of our assumptions and the performance of the estimation methods. Two of these are original scale MOEs--mean absolute deviation (MAD) and chi square statistic. The third is a transformed scale MOE--mean squared error (MSE). Test cases are chosen as input. The results of the cross validation are then discussed.

### B. MEASURES OF EFFECTIVENESS

#### 1. Mean Absolute Deviation

The MAD is probably the most useful MOE to the manpower planner. Our version is augmented to display overestimation and underestimation information. Along with the MAD we observe the magnitude of our errors in both directions, which is especially important since the cost of overestimating is generally not the same as the cost of underestimating. While it does not provide a specific value or standard to gauge the performance of our estimation methods, it does provide very useful insight into tendencies to consistently underestimate or overestimate.

For comparison of the estimation methods, we desire a MAD measure that does not depend upon cell inventories, yet still displays the overage/underage information. For these reasons, we use the attrition rate estimates,  $\hat{p}_i$ , as opposed to the estimated number of attritions,  $(\hat{p}_i \cdot N_i(t))$  (where  $t$  = validation year), in our MAD calculations. For those estimates obtained in the transformed scale, the  $XEB_i$  are inverted back to the original scale using Equation (20) prior to calculating this MOE.

We define the empirical attrition rate for cell  $i$  in validation year  $t$  as

$$p_i^a = \frac{Y_i(t)}{N_i(t)} \quad (55)$$

except when  $N_i(t) = 0$  (no inventory in cell  $i$  for the validation year). In this case we do not compute the cell's deviation from the estimated attrition rate since it would

artificially create an overage situation. Therefore, we reduce  $K$  by one and continue with the remaining cells (the reduced value of  $K$  is then used in the following formulas).

The MAD measures generated for each validation year are

$$\frac{K_u}{K} = \text{fraction of cells with underage} \quad (56)$$

where  $K_u$  is the number of cells which have underage,

$$\frac{\sum_i (p_i^a - \hat{p}_i)^+}{\sum_i |p_i^a - \hat{p}_i|} = \text{fraction of MAD due to underage} \quad (57)$$

and

$$MAD = \frac{1}{K} \sum_i |p_i^a - \hat{p}_i| . \quad (58)$$

We also calculate the average MAD over the validation years. Here we use a weighted average, since the number of cells may have been different in some validation years, i.e., a reduced value of  $K$  was used in these years. The weighted average takes the form

$$Avg \ MAD = \frac{\sum_t K_t MAD_t}{\sum_t K_t} \quad (59)$$

where  $K_t$  is the (possibly reduced) number of cells used in validation year  $t$ .

## 2. Chi Square

The chi square test is used as an indicator of how well the binomial model serves as a description of the attrition process. The test statistic is

$$X_{(K)}^2(t) = \sum_i \frac{(Y_i(t) - \hat{p}_i N_i(t))^2}{N_i(t) \hat{p}_i (1 - \hat{p}_i)} \quad (60)$$

where  $t$  is the validation year. As with the MAD calculations, if  $N_i(t) = 0$  we reduce  $K$  by one and continue. Additionally, if  $\hat{p}_i = 0$  or  $1$ , the denominator equals zero and the summand is undefined. The same course of action is used if this occurs--reduce  $K$  by one and continue. Those estimates obtained in the transformed scale are inverted back to the original scale prior to using Equation (60).

This MOE can be used as a gauge. The chi square statistic given by Equation (60) has expected value  $K$  and variance  $2K$ . We are looking for a  $X^2$  value that is less than two standard deviations to the right of the mean, or

$$X_{(K)}^2 \leq K + 2\sqrt{2K} . \quad (61)$$

A weighted average chi square is computed in the same manner as the weighted average MAD in Equation (59). However, if the number of cells and thus the degrees of freedom,  $K$ , are different over the validation years a problem arises in determining the degrees of freedom for the weighted average. We solve this dilemma by assuming that the weighted average chi square has the original value of  $K$  degrees of freedom.

### 3. Mean Squared Error

The MSE is used to check the validity of our theoretical basis. It is the average squared deviation of the estimated rate from the actual rate, both rates on the transformed scale. The actual rate used is the transformed validation year data. The MSE is defined as

$$L(\delta, \mu) = \frac{1}{K} \sum_i (\delta_i - \mu_i)^2 \quad (62)$$

where

$$\begin{aligned} \delta_i &= XEB_i \\ \mu_i &= XT_i(t) \quad (t = \text{validation year}) . \end{aligned} \quad (63)$$

Again, if  $N_i(t) = 0$ , we reduce  $K$  by one and continue. A weighted average MSE is also computed similar to Equation (59).

The MSE also has a standard to gauge our model. Using Equations (5) and (12) we can compute a baseline variance for any given validation cell. The MSE for that cell, when compared to the baseline value, provides a figure to gauge the value of using shrinkage estimators instead of the cell averages,  $XTB_i$ . There is considerable variability



in these ratios, ranging from 20% to 100%, but 80% appears to be a fair median figure. For example, for cell variances computed from Equation (12) running about 0.15, the MSE hovers about 0.12.

#### 4. Vector Method MOEs

The MOEs discussed above require slight modification before being applied to the vector method described in paragraph III.D.. Recall that this method uses  $K$  cells with service component or commissioning source broken out into a vector of length  $P$ . An attrition rate estimate,  $\delta_{ij}$ , is obtained for each of the  $K \times P$  matrix components. Thus now we have  $KP$  estimates which are compared to the corresponding empirical rates for the validation year. Equations (55) through (63) are modified by replacing all  $i$  subscripts with  $ij$ , replacing all summations over  $i$  by double summations over  $i$  and  $j$ , and replacing all instances of  $K$  by the product  $KP$ .

### C. TEST CASES

The selection of test cases takes on great importance since they provide the foundation for comparison of these methods. It would be impossible to test every permutation of input parameters; therefore we seek a representative fraction of these which would give an accurate account of the performance of our aggregation and estimation methods. Because we are using a different data base from previous theses on estimation methods, no attempt to duplicate their test cases was made.

An approach based upon Latin square experimental design principles was used to select 30 test cases for the first five estimation methods. The test cases for the vector estimation method are addressed later. In determining the test cases, we randomized when possible and intervened to force pairings only when necessary. To begin, we selected values for the input parameters-- $T_0$ ,  $K_0$ , grade, YCS and MOS. Service component and commissioning source are ignored for these test cases, i.e., all classifications of both are accepted.

To ensure proper representation from small MOS groups one through ten, one MOS from each group was randomly selected: 0302, 1802, 2502, 4002, 3060, 7204, 7545, 7523, 7557 and 7563. Since YCS and grade are strongly correlated, these parameters were selected jointly. To ensure each YCS range within the bounded YCS groups was represented along with a fair representation of grades, four grade/YCS pairs were selected: 1Lt/4 YCS, Capt/7 YCS, LtCol/20 YCS and LtCol(failed select)/26 YCS. The two threshold parameters were also selected jointly, resulting in ten pairs ( $T_0/K_0$ ): 30.0/30, 20.0/30, 20.0/20, 10.0/30, 10.0/20, 10.0/10, 5.0/30, 5.0/20, 5.0/10 and 5.0/5.

With these choices in place, it was necessary to combine them to define the actual test cases. It was decided to limit the grade/YCS pairs for these cases to 1Lt/4 YCS and Capt/7 YCS due to the large values for the first five threshold pairs. With ten MOSs specified, we sought ten test cases. Thus, each of the first five threshold pairs was listed twice. Each of the four aviation MOSs was randomly assigned to one of the five threshold pairs; the six ground MOSs were then randomly assigned to the remaining pairs. The two grade/YCS pairs were then randomly assigned within a set of common threshold pairs, e.g., for the two cases with  $T_0/K_0$  of 30.0/30, one was randomly assigned 1Lt/4 YCS, the other was then assigned Capt/7 YCS.

All four grade/YCS pairs would be used with the five remaining threshold pairs. Thus 20 more test cases were generated, with each of the five threshold pairs listed four times. Each MOS was randomly assigned to two distinct threshold pairs, ensuring that the large and major MOS groups were evenly spread throughout the pairs. The four grade/YCS pairs were assigned in random order to each set of common threshold pairs, ensuring that they were evenly spread across large and major MOS groups. The 30 test cases are summarized in Table 3.

The input parameters for six vector test cases were selected from the 30 test cases: Nos. 2, 3, 6, 10, 11 and 20. A small number of vector test cases was initially chosen to investigate the possible advantages of the vector method. If this method appeared to be favorable, then further testing would be conducted.

The six test cases contain a cross section of the input parameters. They include three ground and three aviation MOSs, and use each of the first three grade/YCS pairs twice. The grade/YCS pair of LtCol(FS)/26 YCS was not used because of its extremely low inventory numbers, which when broken out into a vector would have been of little exploratory use. These cases also include six different  $T_0/K_0$  pairs.

Each of the vector test cases is used twice: first with service component and then with commissioning source as the vector component. All three service components--regular, augmented regular and reserve--were used as vector components. Rather than use all 15 commissioning sources (these 15 are listed below Table 4) as vector components (many of them would contain little or no inventory) five commissioning sources for the ground test cases and five for the aviation test cases were chosen. These five were determined to be the sources which contain the largest percentage of inventory for the respective ground or aviation MOSs. The specific commissioning sources selected along with the other vector test case input parameters are summarized in Table 4.

**Table 3. TEST CASES FOR METHODS 1-5**

No.	$T_0$	$K_0$	MOS	S : L : M	YCS	Grade
1	30.0	30	0302	1 : 1 : 1	4	1Lt
2	30.0	30	7523	8 : 3 : 2	7	Capt
3	20.0	30	3060	5 : 2 : 1	7	Capt
4	20.0	30	7563	10 : 4 : 2	4	1Lt
5	20.0	20	2502	3 : 2 : 1	7	Capt
6	20.0	20	7557	9 : 4 : 2	4	1Lt
7	10.0	30	7204	6 : 2 : 1	4	1Lt
8	10.0	30	1802	2 : 1 : 1	7	Capt
9	10.0	20	7545	7 : 3 : 2	7	Capt
10	10.0	20	4002	4 : 2 : 1	4	1Lt
11	10.0	10	2502	3 : 2 : 1	20	LtCol
12	10.0	10	7557	9 : 4 : 2	26	LtCol(FS)
13	10.0	10	7545	7 : 3 : 2	7	Capt
14	10.0	10	0302	1 : 1 : 1	4	1Lt
15	5.0	30	4002	4 : 2 : 1	4	1Lt
16	5.0	30	0302	1 : 1 : 1	20	LtCol
17	5.0	30	7204	6 : 2 : 1	26	LtCol(FS)
18	5.0	30	7563	10 : 4 : 2	7	Capt
19	5.0	20	3060	5 : 2 : 1	7	Capt
20	5.0	20	7545	7 : 3 : 2	20	LtCol
21	5.0	20	1802	2 : 1 : 1	26	LtCol(FS)
22	5.0	20	7563	10 : 4 : 2	4	1Lt
23	5.0	10	7204	6 : 2 : 1	20	LtCol
24	5.0	10	4002	4 : 2 : 1	26	LtCol(FS)
25	5.0	10	7523	8 : 3 : 2	4	1Lt
26	5.0	10	1802	2 : 1 : 1	7	Capt
27	5.0	5	2502	3 : 2 : 1	7	Capt
28	5.0	5	7557	9 : 4 : 2	20	LtCol
29	5.0	5	3060	5 : 2 : 1	4	1Lt
30	5.0	5	7523	8 : 3 : 2	26	LtCol(FS)

(S : L : M = Small MOS Group : Large MOS Group : Major MOS Group)

**Table 4. TEST CASES FOR VECTOR METHOD**

No.	$T_0$	$K_0$	MOS	YCS	Grade	Service Comp	Comm Source
2	30.0	30	7523	7	Capt	1 2 3	(all)
2	30.0	30	7523	7	Capt	(all)	1 2 3 5 11
3	20.0	30	3060	7	Capt	1 2 3	(all)
3	20.0	30	3060	7	Capt	(all)	1 3 7 10 11
6	20.0	20	7557	4	1Lt	1 2 3	(all)
6	20.0	20	7557	4	1Lt	(all)	1 2 3 5 11
10	10.0	20	4002	4	1Lt	1 2 3	(all)
10	10.0	20	4002	4	1Lt	(all)	1 3 7 10 11
11	10.0	10	2502	20	LtCol	1 2 3	(all)
11	10.0	10	2502	20	LtCol	(all)	1 3 7 10 11
20	5.0	20	7545	20	LtCol	1 2 3	(all)
20	5.0	20	7545	20	LtCol	(all)	1 2 3 5 11

**Service Component:**

- 1 - regular
- 2 - augmented regular
- 3 - reserve

**Commissioning Sources used:**

- 1 - U.S. Naval Academy
- 2 - Platoon Leader Class-Aviation
- 3 - Platoon Leader Class-Ground
- 5 - Aviation Officer Candidate
- 7 - Officer Candidate Course-Ground
- 10 - Enlisted Commissioning Program
- 11 - NROTC-Scholarship

**Commissioning Sources not used:**

- 4 - Platoon Leader Class-Law
- 6 - Marine Aviation Cadet
- 8 - Officer Candidate Course-Law
- 9 - Officer Candidate Course-Women
- 12 - NROTC-Ground College
- 13 - NROTC-Aviation College
- 14 - NESEP
- 15 - All Other



## D. RESULTS

For each test case, we apply the aggregation method to meet the threshold levels and then execute the estimation methods. While the ultimate use of these methods is to obtain an attrition rate estimate for the original cell, inspection of these estimates would be of little value in evaluating and comparing the estimation methods. Thus the output from the program takes the form of the MOEs.

The inclusion of the entire output from every test case would not only be cumbersome but would provide an inadequate means of comparing the methods. Therefore the output is summarized in Tables 5 through 7. They contain the output from the first five estimation methods only; the output from the vector test cases is presented later. Sample output for the six methods is contained in Appendix C.

The results summaries list the test case number, the cell inventory threshold,  $T_0$ , and the actual number of cells used,  $K$ . The level of expansion required to achieve these parameter levels is also listed. For example, test case one had a cell inventory threshold of 30.0, and 24 aggregated cells were obtained by expanding the small, large and major MOS group by YCSs four and five. The value for  $K$  is often different from the threshold number of cells,  $K_0$ , listed in Table 3. When  $K$  is less than  $K_0$ , maximum expansion occurred and the threshold was unattainable. When  $K$  is greater than  $K_0$ , the expansion was the least amount possible to remain above the thresholds. From these test cases we can see that it is difficult to meet the threshold number of cells exactly.

The results summaries then list the weighted average MOEs for each of the five estimation methods. The first row within each test case contains the MAD values, the second row the chi square values and the third row the MSE values. The maximum desired chi square value as given by Equation (61) is listed in parentheses, e.g., for test case one this value is 37.9. This affords easier comparison of the chi square values for the different methods. The values of MSE for both original scale methods are blank because MSE is a transformed scale MOE only.

Before discussing the results in general, some additional comments about specific test cases are necessary. Test case four could not be executed by the Efron-Morris method. This is because one of the aggregated cells contains zero attrition for all ten years of data. As a result, the iterative algorithm does not converge.

Test case 12 was not possible because not even one aggregated cell meeting the cell inventory threshold was obtained with maximum expansion in major MOS group two. This extremely low inventory problem was generally true for all test cases involving the LtCol(FS)/26 YCS pair. Test cases 17, 21 and 24 obtained only three aggregated cells

with maximum expansion in major MOS group one. Test case 30 was also from major MOS group two, and obtained only one aggregated cell meeting the cell inventory threshold. As a result, test case 30 was changed to Major(FS)/18 YCS so that results for these low thresholds could be obtained.

As the thresholds became low (test cases 23-30) cells with inventory much larger than  $T_0$  were being obtained prior to any aggregation. This was especially true for the 1Lt/4 YCS and Capt/7 YCS pairs. To avoid masking the results of low inventory thresholds by actually using large inventory cells, the service component/commissioning source parameters for test cases 26, 27 and 29 were changed. Rather than accepting all classifications of these parameters, only one classification for each was accepted. Thus test case 26 was executed with regular/USNA, test case 27 was executed with augmented regular/PLC-ground, and test case 29 was executed with regular/NROTC-scholarship.

We now focus our attention on the results of these test cases with respect to the MOEs. The weighted average MAD figures vary little within each test case over the five methods. This suggests that the total deviation from the validation year empirical attrition rate was the same for all methods. However, this figure does not identify whether the deviations were overestimations or underestimations. The fraction of MAD from underage (not listed in the results summaries) was studied to gain more insight into this important consideration. For each of the 29 test cases (no results for test case 12), a weighted average fraction of MAD from underage was computed for each of the five estimation methods (weighted by the number of cells just as the weighted averages for the MOEs). A weighted average of these 29 values was then computed. This overall weighted average indicates the tendency of the method to underestimate or overestimate--averages above 0.5 indicate a tendency to underestimate; averages below 0.5 indicate a tendency to overestimate. The author is unaware of any information comparing the relative costs of underage and overage. Hence, as a default, we look for values of 0.5, which is a balance between overestimation and underestimation. The averages calculated were: TS1=0.426; TS2=0.436; OS1=0.481; OS2=0.512; and EM=0.452. Although the MAD figures were generally the same for all methods, these averages indicate that the tendencies to overestimate or underestimate may not be the same. The original scale methods seem to have achieved more balance than the transformed scale methods.

The chi square results were not entirely consistent across test cases nor across methods within a test case. These results are discussed first by comparisons between test cases; then by comparisons within test cases.

Of the first ten test cases, only three (Nos. 3, 5 and 8) had weighted average chi square values within the acceptable range. These three test cases expanded only into the large MOS group, whereas of the seven test cases which were unacceptable, all but one (No. 10) expanded into the major MOS group. Of the last 20 test cases, only four had chi square values outside the acceptable range (Nos. 13, 14, 15, and 18). Of these four, two expanded into the large MOS group, and two into the major MOS group. All the test cases with unacceptable values had either 1Lt/4 YCS or Capt/7 YCS pairs. They were fairly well spread across MOS groups. None of the test cases with lower thresholds (Nos. 19-30) had unacceptable chi square values. This suggests that lower thresholds, which result in less expansion, achieve more acceptable results with respect to this MOE.

To investigate this claim further, different combinations of threshold levels for test cases seven and nine were used. The results are contained in Table 8. These results reinforce the claim that lower thresholds are in fact better, since in both cases the chi square results improved as the thresholds, and therefore the level of expansion, were reduced. When comparing these extra test cases, keep in mind that the chi square values for each set of threshold values should be compared to the acceptable range for that specific number of cells; comparisons across test cases with different values of  $K$  are not valid. An important aspect of the argument for lower thresholds is that the thresholds must be considered jointly. For example, in test case seven, with a  $T_0/K$  pair of 10.0/6, the chi square values were nearly acceptable, whereas with 5.0/19 they were clearly unacceptable. Thus we should be most aware of the value  $T_0 \times K_0$ .

We now turn our attention to comparing the chi square values within a test case. Several test cases had chi square values that varied significantly over the estimation methods (Nos. 4, 6 and 22). These three all had 1Lt/4 YCS pairs and were large MOS group four. In test cases four and six the chi square values for the transformed scale methods were not too much larger than the desired maximum; the values for the original scale methods were significantly larger than the desired maximum. In test case 22 the chi square values for the transformed scale methods were acceptable, however the values for the original scale methods were again significantly larger than the desired maximum.

Several other test cases had varying chi square values, but to a lesser degree. In test case eight, only the transformed scale methods had acceptable chi square values, the original scale methods exceeded the desired maximum, although not by a significant margin. In test case 19, only the OS2 method exceeded the desired maximum. All methods for test cases 16, 25, and 27 were within the desired maximum, however the chi square values varied to a large degree over the five methods. Thus, using the chi square



MOE, it appears that the transformed scale methods were generally the same, and as a group outperformed the original scale methods.

The MSE was used only with the transformed scale methods, and thus no comparison with original scale methods can be made. The values for this MOE were generally equal between methods within a test case, and acceptable overall.

The results for the vector method test cases are summarized in Table 9. The table lists the value  $K \times P$  (instead of  $K$ ) because this is the number of estimates obtained and compared to the validation year empirical attrition rates with this method.

Test case two with commissioning source as the vector component had to be modified because only seven aggregated cells were obtained. As a result,  $K = P + 2$ , and the vector method could not be conducted. Therefore, commissioning source three (Platoon Leader Class-ground) was deleted as a vector component and the test case run with only four commissioning sources (1, 2, 5 and 11). Test case 20 with service component as the vector component was infeasible. By starting with a low cell inventory threshold (5.0), when the cells were broken out into the vector components their inventory became extremely low. As a result, when validating year five, two of the cells had zero inventory for all of the remaining nine years for service component three (reserve). Thus the value for  $XTB_{ij}$ , given by Equation (45), becomes undefined and the method cannot be completed.

The results of the vector method with respect to the MOEs is similar to the results of the previous five estimation methods. This method produced acceptable MAD and MSE values, but its chi square values were fairly inconsistent. Test cases two and ten had unacceptable chi square values for both vector components; test case six had an unacceptable chi square value with service component as the vector component. Recall that these test cases also had unacceptable values with the vector component collapsed.

No fair comparison with the first five estimation methods can be made using the summarized results. Obviously the MAD and MSE quantities will be larger since we are comparing three to five times as many estimates to empirical rates with the vector method. Thus a different evaluation technique must be used.

The vector method is designed to take advantage of any correlation between the cells when broken out into vector components. To see if this is occurring we must look at the matrix  $\tilde{S}^{-1}$  as given by Equation (54). In all of the vector test cases, this matrix was essentially diagonal, indicating little correlation between the vector components. In addition, all of the eigenvalues, which become the elements of the diagonal matrix  $E$ , were less than  $(K - P - 2)$ . Therefore, the eigenvalues were replaced by this quantity and the

**Table 5. SUMMARY OF RESULTS (CASES 1-10)**

No.	$T_0$	$K$	Expansion Required	MOE	TS1	TS2	OS1	OS2	EM
1	30.0	24	S:(4,5) L:(4,5) M:(4,5)	MAD X(37.9) MSE	0.102 98.79 0.079	0.101 99.28 0.078	0.102 100.99	0.102 100.96	0.103 101.23 0.080
2	30.0	8	S:(7) L:(7) M:(7)	MAD X(16.0) MSE	0.091 28.16 0.077	0.090 27.68 0.076	0.092 28.71	0.091 28.68	0.091 27.73 0.076
3	20.0	31	S:(1-3,6-19) L:(6-8)	MAD X(46.7) MSE	0.056 37.49 0.062	0.056 37.80 0.062	0.055 39.58	0.055 42.85	0.055 38.38 0.062
4	20.0	23	S:(1-5,8-19) L:(1-5,8-19) M:(1-5,8-19)	MAD X(36.6) MSE	0.029 39.34 0.035	0.029 47.36 0.037	0.026 95.41	0.024 139.14	
5	20.0	20	S:(1-3,6-19) L:(7)	MAD X(32.6) MSE	0.048 20.75 0.048	0.049 20.83 0.049	0.047 24.34	0.047 24.20	0.048 21.41 0.049
6	20.0	22	S:(1-5,8-19) L:(1-5,8-19) M:(3-5)	MAD X(35.3) MSE	0.029 40.42 0.037	0.029 50.70 0.039	0.027 90.93	0.025 127.86	0.029 65.20 0.040
7	10.0	32	S:(4,5) L:(4,5) M:(4)	MAD X(48.0) MSE	0.129 111.67 0.137	0.130 113.23 0.137	0.130 112.64	0.130 113.64	0.133 114.28 0.140
8	10.0	28	S:(1-3,6-19) L:(1-3,6-11)	MAD X(43.0) MSE	0.039 34.37 0.039	0.038 34.70 0.040	0.039 45.16	0.038 49.60	0.039 35.54 0.040
9	10.0	14	S:(7) L:(7) M:(7)	MAD X(24.6) MSE	0.117 38.85 0.130	0.115 37.50 0.127	0.117 39.59	0.117 39.62	0.115 40.26 0.132
10	10.0	27	S:(4,5) L:(4,5)	MAD X(41.7) MSE	0.128 64.33 0.137	0.129 65.92 0.137	0.129 65.62	0.128 66.61	0.127 62.64 0.135

TS1 - Transformed scale, time dependent variance

TS2 - Transformed scale, time independent variance

OS1 - Original scale, time dependent variance

OS2 - Original scale, time independent variance

EM - Efron-Morris method



matrix  $E$  always had  $(K - P - 2)$  as its diagonal elements. Because these results indicated no worthwhile improvements over the first five methods, no further testing of the vector method was conducted.

Finally, the performance of the heuristic aggregation algorithm listed in Appendix A was also evaluated. For each test case, the total inventory of cells below  $T_0$  was summed and this value divided by  $T_0$ . The integer part of this number provides an upper bound on the number of aggregated cells that can be obtained by any aggregation technique. This upper bound was compared to the actual number of aggregated cells produced by the algorithm. The algorithm achieved the maximum in 71.4% (20 of 28) of the test cases. It achieved one less than the maximum in 21.4% (6 of 28) of the test cases, and two less than the maximum in 7.2% (2 of 28) of the test cases (only 28 test cases required aggregation: No. 12 was infeasible; No. 14 all cells were above  $T_0$ ). This performance is acceptable for our application.

**Table 6. SUMMARY OF RESULTS (CASES 11-20)**

No.	$T_0$	$K$	Expansion Required	MOE	TS1	TS2	OS1	OS2	EM
11	10.0	11	S:(20-25) L:(20-25)	MAD X(20.4) MSE	0.109 18.79 0.141	0.106 19.75 0.142	0.108 19.96	0.107 20.53	0.107 18.99 0.139
12	10.0	0	S:(26) L:(26) M:(26)	MAD X(0.0) MSE					
13	10.0	14	S:(7) L:(7) M:(7)	MAD X(24.6) MSE	0.117 38.85 0.130	0.115 37.50 0.127	0.117 39.59	0.117 39.62	0.115 40.26 0.132
14	10.0	10	S:(4,5) L:(4,5)	MAD X(18.9) MSE	0.113 57.80 0.102	0.110 60.07 0.103	0.113 57.71	0.113 57.80	0.115 59.36 0.104
15	5.0	32	S:(4,5) L:(4,5)	MAD X(48.0) MSE	0.137 69.96 0.156	0.140 70.72 0.158	0.139 70.27	0.139 72.01	0.139 68.15 0.155
16	5.0	32	S:(20-25) L:(20-25) M:(20-22)	MAD X(48.0) MSE	0.122 39.41 0.146	0.122 40.38 0.146	0.121 44.35	0.121 47.84	0.121 42.27 0.148
17	5.0	3	S:(26) L:(26) M:(26)	MAD X(7.9) MSE	0.166 3.66 0.0.189	0.166 3.57 0.188	0.168 3.88	0.168 3.78	0.168 4.02 0.202
18	5.0	29	S:(6,7) L:(6,7) M:(7)	MAD X(44.2) MSE	0.141 79.04 0.176	0.141 78.23 0.176	0.142 78.61	0.141 81.29	0.141 78.84 0.177
19	5.0	24	S:(2,3,6-10)	MAD X(37.9) MSE	0.085 28.95 0.122	0.082 29.28 0.123	0.080 30.91	0.084 43.36	0.080 35.44 0.132
20	5.0	19	S:(20-25) L:(20-25) M:(20)	MAD X(31.3) MSE	0.111 17.29 0.113	0.113 17.29 0.114	0.113 18.92	0.106 23.37	0.110 18.28 0.114

TS1 - Transformed scale, time dependent variance

TS2 - Transformed scale, time independent variance

OS1 - Original scale, time dependent variance

OS2 - Original scale, time independent variance

EM - Efron-Morris method

**Table 7. SUMMARY OF RESULTS (CASES 21-30)**

No.	$T_0$	$K$	Expansion Required	MOE	TS1	TS2	OS1	OS2	EM
21	5.0	3	S:(26) L:(26) M:(26)	MAD X(7.9) MSE	0.167 3.66 0.189	0.166 3.57 0.188	0.168 3.88	0.168 3.78	0.168 4.02 0.202
22	5.0	22	S:(1-5,8-19) L:(3,4)	MAD X(35.3) MSE	0.032 23.56 0.059	0.042 15.03 0.041	0.024 63.10	0.022 92.85	0.032 22.56 0.056
23	5.0	9	S:(20-25) L:(20)	MAD X(17.5) MSE	0.121 8.12 0.141	0.121 8.19 0.141	0.119 8.65	0.121 9.25	0.120 8.17 0.137
24	5.0	3	S:(26) L:(26) M:(26)	MAD X(7.9) MSE	0.166 3.66 0.189	0.166 3.57 0.188	0.168 3.88	0.168 3.78	0.168 4.02 0.202
25	5.0	10	S:(1-6,8-19) L:(1-6)	MAD X(18.9) MSE	0.050 5.09 0.044	0.051 4.78 0.037	0.020 15.35	0.020 16.54	0.048 4.85 0.039
26	5.0	11	S:(1-3,6-19) L:(6,7)	MAD X(20.4) MSE	0.138 13.61 0.184	0.138 13.65 0.186	0.138 14.09	0.135 16.10	0.135 14.28 0.189
27	5.0	6	S:(6-8)	MAD X(12.9) MSE	0.070 4.64 0.075	0.069 4.55 0.074	0.055 6.88	0.050 9.41	0.068 4.60 0.074
28	5.0	7	S:(20,21)	MAD X(14.5) MSE	0.114 7.59 0.140	0.116 7.67 0.143	0.118 7.99	0.113 8.74	0.116 8.37 0.147
29	5.0	5	S:(4,5)	MAD X(11.3) MSE	0.170 6.36 0.211	0.169 6.23 0.210	0.168 7.64	0.167 8.25	0.169 8.06 0.281
30	5.0	6	S:(1-6,8-19) L:(17-19)	MAD X(12.9) MSE	0.112 6.15 0.136	0.110 6.40 0.136	0.110 7.31	0.104 8.73	0.108 6.42 0.135

TS1 - Transformed scale, time dependent variance

TS2 - Transformed scale, time independent variance

OS1 - Original scale, time dependent variance

OS2 - Original scale, time independent variance

EM - Efron-Morris method

**Table 8. SUMMARY OF RESULTS (CASES 7 AND 9 EXPANDED)**

No.	$T_0$	$K$	Expansion Required	MOE	TS1	TS2	OS1	OS2	EM
7-1	10.0	32	S:(4,5) L:(4,5) M:(4)	X(48.0)	111.67	113.23	112.64	113.64	114.28
7-2	10.0	17	S:(4,5) L:(4)	X(28.7)	45.31	45.99	45.90	46.58	43.68
7-3	10.0	6	S:(4,5)	X(12.9)	13.08	12.98	13.41	13.53	13.03
7-4	5.0	19	S:(4,5) L:(4)	X(31.3)	49.28	49.53	49.23	50.84	46.91
7-5	5.0	7	S:(4,5)	X(18.9)	14.42	14.27	14.82	14.93	14.18
7-6	5.0	4	S:(4)	X(9.7)	9.20	8.88	9.22	9.20	9.49
9-1	10.0	14	S:(7) L:(7) M:(7)	X(24.6)	38.85	37.50	39.59	39.62	40.26
9-2	10.0	4	S:(7)	X(9.7)	10.35	10.14	10.58	10.57	10.11
9-3	5.0	17	S:(7) L:(7) M:(7)	X(28.7)	44.95	42.87	44.40	46.03	46.15
9-4	5.0	5	S:(7)	X(11.3)	11.91	11.69	12.16	12.15	11.64

TS1 - Transformed scale, time dependent variance

TS2 - Transformed scale, time independent variance

OS1 - Original scale, time dependent variance

OS2 - Original scale, time independent variance

EM - Efron-Morris method

**Table 9. SUMMARY OF RESULTS (VECTOR METHOD)**

No.	$T_0$	KP	Vector Component	MOE	Vector Method
2	30.0	24	SC	MAD X(37.9) MSE	0.149 61.03 0.229
2	30.0	28	CS	MAD X(43.0) MSE	0.222 115.34 0.398
3	20.0	93	SC	MAD X(120.3) MSE	0.158 110.96 0.219
3	20.0	155	CS	MAD X(190.2) MSE	0.157 132.37 0.201
6	20.0	66	SC	MAD X(89.0) MSE	0.062 109.19 0.074
6	20.0	100	CS	MAD X(128.3) MSE	0.083 58.58 0.081
10	10.0	81	SC	MAD X(106.5) MSE	0.212 251.63 0.368
10	10.0	120	CS	MAD X(151.0) MSE	0.321 707.85 0.625
11	10.0	42	SC	MAD X(60.3) MSE	0.193 44.86 0.214
11	10.0	60	CS	MAD X(81.9) MSE	0.222 53.55 0.225
20	5.0	72	SC	MAD X(0.0) MSE	
20	5.0	100	CS	MAD X(128.3) MSE	0.254 55.92 0.245

SC - service component

CS - commissioning source



## V. CONCLUSIONS AND RECOMMENDATIONS

### A. CONCLUSIONS

The results indicate that the desired stability in estimating attrition rates for low inventory cells has been achieved with the aggregation and estimation methods presented in this study. The use of “shrinkage” methods applied to well selected groups of cells allows for the achievement of quality estimates of attrition in the face of low inventory numbers for the individual cells.

None of the six estimation methods stood out as a clear favorite. The vector method did not provide any additional benefits using service component or commissioning source as vector components. Since it is a more complicated method and has the potential to become unsolvable with zero inventory vector components, it appears to be the least favorite. Perhaps more success would be obtained with alternative classifications for the vector component.

The Efron-Morris method also involves more computational effort than the first four empirical Bayes methods. Its performance was very much similar to the transformed scale, time dependent variance method since the only difference between them is the iterative algorithm used to determine the amount of shrinkage. The Efron-Morris method has the potential to become unsolvable when a cell has zero attrition for every year--a distinct possibility when dealing with low inventory cells. This suggests that it is the least favorite of the first five methods.

Of the remaining four methods, there seems to be only small difference between the time dependent variance and the time independent variance methods on the same scale. In test cases where the chi square values were marginal or unacceptable, the time dependent variance methods were usually better. In these same test cases, the transformed scale methods performed better than the original scale methods. Therefore, if one method was to be singled out as best, it would be the first method: transformed scale, time dependent variance.

The tendency to overestimate or underestimate as shown by the weighted average fraction of MAD from underage may also be a consideration when selecting a method. An analysis of this type must weigh the costs of overestimating versus the costs of underestimating, which generally are not the same. This type of an analysis is beyond

the scope of this study. In addition, further testing of the methods would be required to gain a more accurate estimate of this tendency.

The threshold levels also seem to strongly influence the performance of the estimation methods. It appears that expansion past the large MOS group begins to detract from homogeneous attrition behavior. While further study would be required to identify optimal threshold levels, it is apparent that both thresholds should not exceed 20.0, and the value of  $T_0 \times K_0$  should not exceed 100.

A method for dealing with cells whose inventory is much greater than  $T_0$  must be developed. In some test cases, cells with inventory three or more times as large as  $T_0$  were obtained and used in the estimation process. This did not seem to affect the results, as they were present in almost all test cases. These cells could be disaggregated into multiple cells with inventory closer to the threshold, although the effect of this has not been determined.

## **B. RECOMMENDATIONS**

The proposed aggregation method should be implemented as a method of identifying additional cells to be used in the attrition rate estimation process. This method provides greater homogeneity of attrition behavior among cells over the current method.

The empirical Bayes estimation methods developed in this study are recommended for use in estimating the attrition rates for low personnel inventory cells.

Overall, the empirical Bayes estimation methods when combined with the proposed aggregation method have achieved the stability in attrition rate estimation that is required to provide a foundation for manpower planning.

## APPENDIX A. AGGREGATION ALGORITHMS

### A. HEURISTIC ALGORITHM

The heuristic algorithm for aggregating cells is as follows:

1. Given a set of cells,  $S$ , and the (time average) inventory of each cell,  $INV_c$ , partition  $S$  into two subsets as follows:
 
$$S_1 = \{c : c \in S ; INV_c \geq T_0\}$$

$$S_2 = \{c : c \in S ; INV_c < T_0\}$$
2. Put the cells in  $S_1$  into the set of aggregated cells,  $K$ .
3. Order the cells in  $S_2$  according to size of their inventory:
 
$$INV_1 \leq INV_2 \leq \dots \leq INV_n \quad n = |S_2|$$
4. Start with  $c_n$ , the cell in  $S_2$  with the largest inventory. Find the smallest cell in  $S_2$ ,  $c'$ , that when united with  $c_n$  the resulting total inventory will meet or exceed  $T_0$ . Combine its data with  $c_n$ , put  $c_n$  into  $K$ , and remove  $c'$  from  $S_2$  (the modified set  $S_2$  will now be referred to as  $S_2^-$ ). Repeat the procedure with  $c_{n-1}$ , and so forth.
5. If no cell in  $S_2^-$  when combined with the current largest cell,  $c_{n-i}$ , exceeds  $T_0$ , use the next largest cell,  $c_{n-i-1}$ , and remove  $c_{n-i-1}$  from  $S_2^-$ . This will create an aggregated cell that is still below threshold. Return to the procedure in Step 4 of trying to find  $c'$ . If no such cell is contained in  $S_2^-$ , use  $c_{n-i-2}$ , and so forth.
6. Continue this procedure until the sum of all the cells remaining in  $S_2^-$  is less than  $T_0$ . These cells are sequentially added to the aggregated cells in  $K$  in Step 7.
7. Add the largest cell in  $S_2^-$  to the smallest cell in  $K$ , and update its average inventory. Add the next largest cell in  $S_2^-$  to the current smallest cell in  $K$ , and update the inventory. Continue until all cells in  $S_2^-$  have been used.

We now have  $|K|$  aggregated cells which exceed the threshold,  $T_0$ , to use in the attrition rate estimation procedure.

### B. INTEGER LINEAR PROGRAM

The formulation as an integer linear program is as follows:

#### Index Use

$c$	cell (before aggregation)
$a$	aggregated cell

#### Given Data

$INV_c$	average inventory of cell $c$
$T_0$	threshold cell inventory

### Binary Variables

$X_{c,a}$       1 indicates use cell c in aggregated cell a

$Z_a$       1 indicates use cell a for aggregation

### Formulation

$$\text{MAX} \quad \sum_a Z_a$$

subject to

$$\sum_a X_{c,a} \leq 1 \quad \forall c \quad (\text{each cell used at most once})$$

$$\sum_c INV_c \cdot X_{c,a} \geq T_0 \cdot Z_a \quad \forall a \quad (\text{aggregated cell must have size} \geq T_0)$$

$$X_{c,a}, Z_a \in \{0,1\}$$

## APPENDIX B. COMPUTER PROGRAMS

### A. GENERAL

A computer program written in FORTRAN is used to conduct the cross validation using the methods developed in this thesis. Although the program consists of 33 subroutines, 6 function subroutines, and over 2000 lines of code, it can be easily summarized by breaking it into the two areas of the thesis: cell aggregation and estimation methods.

The main program and aggregation subroutines (listed in paragraph B) read the input parameters and execute the expansion and aggregation methods discussed in Chapter II. An existing program written by Luis Uribe, an independent contractor under the direction of Professor Read, underwent extensive modification to fulfill these requirements. The input parameters-- $T_0$ ,  $K_0$ , MOS, YCS, grade, service component(s), and commissioning source(s)--are read by Subroutine GETPAR either in the interactive mode via the terminal or by using MC87 EXEC (listed in paragraph E). Uribe uses an innovative method to estimate the amount of expansion required to meet the threshold parameters. This approach precludes the requirement to read the data base after each step in the expansion process which would be extremely computer time intensive. Inventory information is extracted from the data base and stored in a separate data file for each pay grade (a sample data file and the program used to create it are listed in paragraph F). The data file is accessed via the user's A-disk which is significantly faster than accessing the data base through MVS. Subroutine READET reads the appropriate data file for the specified grade and constructs a table of cells for those records that are in the same major MOS group as the user defined MOS, and meet the service component and commissioning source parameters. All YCSs are accepted, since the extent of expansion is not yet determined. Function NCEVAL screens this table using the current level of expansion and estimates the number of aggregated cells with average inventory greater than or equal to  $T_0$  that will be obtained. If this number is less than  $K_0$ , Subroutine EXPAND begins the expansion stages as described in paragraph II.C.. After each increment of expansion, NCEVAL screens the table and estimates the number of aggregated cells that will be obtained. This loop through EXPAND and NCEVAL continues until the estimated number of aggregated cells meets the threshold,  $K_0$ . The estimated number of cells and the level of expansion are then displayed on the terminal screen.



The user may elect to go forth and read the data base to determine the actual number of aggregated cells obtained, or may elect to change the level of expansion.

The level of expansion is changed through the variable AGGPCT. This variable estimates the effectiveness of the heuristic aggregation method listed in Appendix A. To estimate the number of aggregated cells that will be obtained, NCEVAL compares the cells which meet the expansion criteria to the minimum inventory threshold,  $T_0$ . Those that are greater than  $T_0$  will obviously produce one aggregated cell. The inventory of those that are less than  $T_0$  is summed. The estimated number of cells is then the total of the number of cells greater than  $T_0$  and AGGPCT times the sum of the cell inventory below  $T_0$  divided by  $T_0$ . The variable AGGPCT is initially set at 0.9, but can be interactively changed via the terminal. By increasing the value of AGGPCT we can decrease the level of expansion; by decreasing the value of AGGPCT we can increase the level of expansion.

Once we decide to go forth and read the actual data base, Subroutine READER extracts records meeting the expansion criteria developed using EXPAND and NCEVAL and pools them into cells. Subroutine AGGREG aggregates these cells to meet the average inventory threshold,  $T_0$ . The actual number of aggregated cells obtained is then compared to the threshold number of cells,  $K_0$ . Again, the user has the option of changing the level of expansion to obtain more or fewer cells, or continuing on to the estimation process.

The first five estimation methods are called by SUBROUTINE MC87BZ (listed in paragraph C). The estimation methods are contained in separate subroutines: EBTS1, EBTS2, EBOS1, EBOS2 and EMTS (EB-empirical Bayes; EM-Efron-Morris; TS-transformed scale; OS-original scale; 1-time dependent variance; 2-time independent variance). The iterations required by the first four methods are conducted in Subroutine EBITER; the Efron-Morris iterations are conducted in Subroutine EMITER. The MOEs are then computed by Subroutines MSE and OSMOE.

If the vector method is to be used, Subroutine BKDOWN then breaks the cells out by their vector components (a vector of length three for service component; a vector of length five for commissioning source). The vector estimation method is contained in Subroutine MC87V (listed in paragraph D). Since all of its computations are unique, this subroutine is self-contained with the exception of the transformation formula, which is contained in Function FTTV.

## B. MAIN PROGRAM AND AGGREGATION SUBROUTINES

```

C --- PROGRAM TO CONDUCT AGGREGATION AND ESTIMATION METHODS      MC800010
C                                                                    MC800020
C --- PARAMETER MXY MUST BE UPDATED TO REFLECT EXACT NO. YEARS OF DATA MC800030
C --- PARAMETER MXP IS MAX LENGTH OF 3RD DIMENSION P-VECTOR      MC800040
C --- PARAMETER MXK IS MAX NUMBER OF AGGREGATED CELLS (MAX NO)    MC800050
C   PARAMETER (MXX=600, MXY=10, MXP=6, MXK=50)                    MC800060
C   PARAMETER (NMS=81, NG=14, NLG=6, NMG=4, NYB=4, NYE=18, NYEG=4) MC800070
C                                                                    MC800080
C   INTEGER ST1,ST2,LYR                                           MC800090
C   INTEGER SYCS(31), NYCS                                         MC800100
C   INTEGER SYCSG(31),SYCSL(31),SYCSM(31),NYCSG,NYCSL,NYCSM       MC800110
C   INTEGER SMOS(30), NMOS                                          MC800120
C   INTEGER SVCMP(5), NSC                                           MC800130
C   INTEGER SCSRC(16),NCSR                                          MC800140
C   INTEGER SGRD                                                    MC800150
C   INTEGER*2 MOSGR(2,NMS), YCSB(NYE,NYB,NYEG), VYC(NYE)         MC800160
C   INTEGER*2 LGRP(NG), MGRP(NLG)                                   MC800170
C   REAL INV(MXX,MXY),Y(MXX,MXY), SINV(MXX,MXY),SY(MXX,MXY)      MC800180
C   INTEGER DATA(MXY)                                              MC800190
C --- ARRAYS FOR MC87BZ                                           MC800200
C   REAL XTB(MXX),VXTB(MXX),XEB(MXX),A(MXX)                       MC800210
C --- ARRAYS FOR MC87V                                           MC800220
C   REAL XTBJI(MXP,MXK), DELTA(MXP,MXK), X(MXP,MXK)              MC800230
C   REAL XVYR(MXP,MXK), VYRINV(MXP,MXK), VYRY(MXP,MXK)           MC800240
C   REAL BSTAR(MXP,MXP), S(MXP,MXP), GAMMA(MXP,MXP)               MC800250
C   REAL XBBJ(MXP), EVAL(MXP)                                      MC800260
C                                                                    MC800270
C   INTEGER*2 PTRTBL(MXX, 2), INDX(MXX), MKG(MXX), RETTBL(MXX,3)  MC800280
C   INTEGER*2 PTBL(MXX, 3), BKTBL(MXX,3)                           MC800290
C   REAL AVINV(MXX), RETINV(MXX)                                   MC800300
C   DATA MKG/MXX*0/                                               MC800310
C --- ASSIGN MOS TO SMALL, LARGE AND MAJOR MOS GROUP              MC800320
C   DATA MOSGR/013,1, 020,2, 027,2, 038,2, 039,2,               MC800330
C   * 005,3, 007,3, 049,3, 052,3,                                MC800340
C   * 074,4, 079,4, 085,4, 101,4,                                MC800350
C   * 016,5, 060,5, 064,5, 076,5, 111,5, 116,5,                 MC800360
C   * 132,6, 134,6, 135,6, 139,6,                                MC800370
C   * 143,7, 147,7, 150,7, 153,7, 154,7, 155,7, 170,7,          MC800380
C   * 149,8, 151,8,                                               MC800390
C   * 160,9, 161,9, 164,9, 166,9, 167,9, 168,9, 178,9,          MC800400
C   * 173,10, 174,10, 175,10, 176,10, 177,10, 179,10, 144,10,    MC800410
C   * 145,10, 165,10,                                             MC800420
C   * 001,11, 006,11, 012,11, 015,11, 019,11, 026,11, 037,11,    MC800430
C   * 048,11, 051,11, 059,11, 070,11, 075,11, 078,11, 084,11,    MC800440
C   * 087,11, 100,11, 110,11, 115,11, 131,11, 138,11, 217,11,    MC800450
C   * 172,12, 187,12, 188,12, 189,12,                            MC800460
C   * 142,13, 146,13, 148,13, 152,13, 156,13, 163,13, 169,13,    MC800470
C   * 088,14 /                                                    MC800480
C   DATA LGRP/1,1,4*2,3,3,4,4,5,5,5,6/                          MC800490
C   DATA MGRP/1,1,2,2,3,4/                                       MC800500
C --- CREATE YCS EXPANSION BOUNDS                                  MC800510
C   DATA YCSB/1,2,3,4,5,6, 8,9,10,11,12,13,14,15,16,17,18,19,  MC800520
C   * 7,17*0, 20,21,22,23,24,25,12*0, 26,17*0,                 MC800530
C   * 1,2,3,4,5, 8,9,10,11,12,13,14,15,16,17,18,19,1*0,        MC800540

```

```

*          6,7,16*0,    20,21,22,23,24,25,12*0,    26,17*0,    MC800
*          1,2,3,4,5,6, 8,9,10,11,12,13,14,15,16,17,18,19,    MC800
*          7,17*0,    20,21,22,23,24,25,12*0,    26,17*0,    MC800
*          1,2,3, 6,7,8,9,10,11,12,13,14,15,16,17,18,19,1*0,    MC800
*          4,5,16*0,    20,21,22,23,24,25,12*0,    26,17*0    /    MC800
C --- INITIALIZE INVENTORY AND ATTRITION ARRAYS    MC800
  DO 1 I=1,MXX    MC800
    DO 2 J=1,MXY    MC800
      SINV(I,J)=0    MC800
      SY(I,J)=0    MC800
      INV(I,J)=0    MC800
      Y(I,J)=0    MC800
    2 CONTINUE    MC800
  1 CONTINUE    MC800
C --- DEFINE FILE FOR OUTPUT    MC800
  CALL EXCMS('FILEDEF 11 DISK MC87 OUTPUT A')    MC800
C --- FIRST/LAST YEAR OF DATA ON TAPE.  UPDATE WHEN NECESSARY    MC800
  ST1=77    MC800
  NYR=MXY    MC800
  LYR=ST1+NYR-1    MC800
C --- INITIAL VALUE FOR AGGREGATION ESTIMATION PERCENTAGE    MC800
  AGGPCT=0.9    MC800
  ICYCLE=1    MC800
C --- GET INPUT PARAMETERS    MC800
  CALL GETPAR(AIMIN,NO,NMOS,SMOS,NYCS,SYCS,SGRD,    MC800
*          NSC,SVCMP, NCSR,SCSRC, IGR,MOSGR,NMS, ISFLAG)    MC800
C --- MAJOR GROUP IS MG, LARGE GROUP LG, GROUP IGR, YCS BLOCK IY    MC800
  LG=LGRP(IGR)    MC800
  MG=MGRP(LG)    MC800
    WRITE(6,*) ' '    MC800
    WRITE(6,*) '----- GR,LG,MG=',IGR,LG,MG    MC800
    WRITE(6,*) ' '    MC800
C --- READ EVALUATION TABLE.  SELECT ONLY RECS PASSING SELECTION CRITERIA    MC800
  CALL READET(RETTL,RETINV,MXX,NRET,SGRD,NSC,SVCMP,NCSR,SCSRC,    MC800
*          MG,LGRP,MGRP,MOSGR,NMS)    MC800
5  RC=0    MC800
  IGX=IGR    MC800
  LGX=0    MC800
  MGX=0    MC800
  NYCSG=1    MC800
  SYCSG(1)=SYCS(1)    MC800
  NYCSL=1    MC800
  SYCSL(1)=SYCS(1)    MC800
  NYCSM=1    MC800
  SYCSM(1)=SYCS(1)    MC800
  NCTOT=0    MC800
  NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSG,SYCSG,RETTL,RETINV,NRET,MXX,    MC800
*  LGRP,MGRP,NMS,AGGPCT,IGR,LG)    MC800
C --- DO WHILE NCTOT<NO & RC=0  (EXPAND AS LONG AS NO NOT MET)    MC800
10 IF(NC.GE. NO) THEN    MC800
  WRITE(6,*) '$GG EVAL NC,SYCSG=',NC,(SYCSG(II),II=1,NYCSG)    MC800
  GO TO 60    MC800
ENDIF    MC800
IF(NYCSG.EQ.1) THEN    MC800
  CALL GETVYC(SYCS(1),LG,YCSB,NYE,NYB,NYEG,VYC)    MC800
  WRITE(6,*) '=== VYC=',(VYC(I),I=1,NYE)    MC800

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ENDIF	MC801110
CALL EXPAND(NYCSG,SYCSG,VYC,NYE,IGX,LGX,MGX,LG,MG,RC)	MC801120
IF(IGX.EQ. 0) GO TO 20	MC801130
NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSG,SYCSG,RETTBL,RETINV,NRET,MXX,	MC801140
* LGRP,MGRP,NMS,AGGPCT,IGR,LG)	MC801150
GO TO 10	MC801160
20 NCTOT=NC	MC801170
WRITE(6,*) '\$\$G EVAL NC,SYCSG=',NCTOT,(SYCSG(II),II=1,NYCSG)	MC801180
C	MC801190
C --- EXPAND TO LARGE MOS GROUP	MC801200
WRITE(6,*) ' '	MC801210
WRITE(6,*) '== EXPANDING BY LARGE GROUP: ',LGX	MC801220
NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSL,SYCSL,RETTBL,RETINV,NRET,MXX,	MC801230
* LGRP,MGRP,NMS,AGGPCT,IGR,LG)	MC801240
30 IF((NCTOT+NC).GE. NO) THEN	MC801250
WRITE(6,*) '\$LL EVAL NC,SYCSL=',(NCTOT+NC),(SYCSL(II),II=1,NYCSL)	MC801260
GO TO 60	MC801270
ENDIF	MC801280
IF(NYCSL.EQ. 1) CALL GETVYC(SYCS(1),LG,YCSB,NYE,NYB,NYEG,VYC)	MC801290
CALL EXPAND(NYCSL,SYCSL,VYC,NYE,IGX,LGX,MGX,LG,MG,RC)	MC801300
IF(LGX.EQ. 0) GO TO 40	MC801310
NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSL,SYCSL,RETTBL,RETINV,NRET,MXX,	MC801320
* LGRP,MGRP,NMS,AGGPCT,IGR,LG)	MC801330
GO TO 30	MC801340
40 NCTOT=NCTOT+NC	MC801350
WRITE(6,*) '\$\$L EVAL NC,SYCSL=',NCTOT,(SYCSL(II),II=1,NYCSL)	MC801360
C	MC801370
C --- EXPAND TO MAJOR MOS GROUP	MC801380
WRITE(6,*) ' '	MC801390
WRITE(6,*) '== EXPANDING BY MAJOR GROUP: ',MGX	MC801400
NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSM,SYCSM,RETTBL,RETINV,NRET,MXX,	MC801410
* LGRP,MGRP,NMS,AGGPCT,IGR,LG)	MC801420
50 IF((NCTOT+NC).GE. NO .OR. RC.NE. 0) THEN	MC801430
WRITE(6,*) '\$MM EVAL NC,SYCSM=',(NC+NCTOT),(SYCSM(II),II=1,NYCSM)	MC801440
GO TO 60	MC801450
ENDIF	MC801460
IF(NYCSM.EQ. 1) CALL GETVYC(SYCS(1),LG,YCSB,NYE,NYB,NYEG,VYC)	MC801470
CALL EXPAND(NYCSM,SYCSM,VYC,NYE,IGX,LGX,MGX,LG,MG,RC)	MC801480
NC=NCEVAL(AIMIN,IGX,LGX,MGX,NYCSM,SYCSM,RETTBL,RETINV,NRET,MXX,	MC801490
* LGRP,MGRP,NMS,AGGPCT,IGR,LG)	MC801500
GO TO 50	MC801510
C	MC801520
C --- EXPANSION FINISHED	MC801530
60 IF(RC.NE. 0) THEN	MC801540
WRITE(5,*) '*** REQUIRED NO MAY NOT BE MET: NO,NC=',NO,(NC+NCTOT)	MC801550
ENDIF	MC801560
C --- ALLOW USER TO CHANGE EXPANSION LEVEL	MC801570
WRITE(5,*) 'ESTIMATED NUMBER OF CELLS =',NC+NCTOT	MC801580
70 WRITE(5,*)	MC801590
WRITE(5,*) 'ENTER 1 TO CALL READER, 0 TO CHANGE EXPANSION'	MC801600
READ(5,*) NPICK1	MC801610
IF(NPICK1.EQ. 1) THEN	MC801620
GO TO 80	MC801630
ELSE	MC801640
WRITE(5,*) 'AGGPCT IS CURRENTLY =', AGGPCT	MC801650
WRITE(5,*) 'ENTER NEW VALUE FOR AGGPCT'	MC801660

READ(5,*) AGGPCT	MC8017
GO TO 5	MC8018
ENDIF	MC8019
80 WRITE(5,*) 'CALLING READER'	MC8019
C	MC8019
C --- USER ELECTS TO READ THE DATA BASE - DETERMINE MOS EXPANSION LEVEL	MC8019
CALL GETMOS(SMOS,NMOS,MGX,LGX,MG,LG,IGR,MOSGR,LGRP,MGRP,	MC8019
* NMS,NG,NLG)	MC8019
C --- READ THE DATA BASE AND CREATE THE CELLS	MC8019
CALL READER(DATA,INV,Y,MXX,NMOS,NYCSG,NYCSL,NYCSM,NSC,NCSR,NYR,	MC8019
* SMOS,SYCSG,SYCSL,SYCSM,SGRD,SVCMP,SCSRC,NRC,PTRTBL,LGX,MGX,IGR,	MC8019
* LG,MGRP,LGRP,MOSGR,NMS,NG,NLG,ICYCLE,NPT,PTBL,ISFLAG,SINV,SY)	MC8019
C --- PERFORM CELL AGGREGATION TO MEET INVENTORY THRESHOLD	MC8019
CALL AGGREG(INV,Y,MXX,NYR,SMOS,SYCSG,	MC8018
* NRC, NRCOLD,PTRTBL,INDX,AVINV,AIMIN,MKG)	MC8018
C --- ALLOW USER TO CHANGE EXPANSION LEVEL	MC8018
WRITE(5,*) 'NUMBER OF CELLS =' ,NRC	MC8018
90 WRITE(5,*)	MC8018
WRITE(5,*) 'ENTER 1 TO CONTINUE, 0 TO CHANGE EXPANSION'	MC8018
READ(5,*) NPICK2	MC8018
IF(NPICK2 .EQ. 1) THEN	MC8018
GO TO 100	MC8018
ELSE	MC8018
WRITE(5,*) 'AGGPCT IS CURRENTLY =' , AGGPCT	MC8019
WRITE(5,*) 'ENTER NEW VALUE FOR AGGPCT'	MC8019
READ(5,*) AGGPCT	MC8019
ICYCLE=ICYCLE+1	MC8019
GO TO 5	MC8019
ENDIF	MC8019
C	MC8019
C --- USER ELECTS TO CONDUCT ESTIMATION	MC8019
100 CONTINUE	MC8019
WRITE(11,201)'EXPANSION INFORMATION: '	MC8019
WRITE(11,203)'ACTUAL NO. OF CELLS USED= ' ,NRC	MC8020
WRITE(11,202)'MOS GROUP #',IGR,' YCS'S USED= ',	MC8020
* (SYCSG(I),I=1,NYCSG)	MC8020
IF(LGX .GT. 0) THEN	MC8020
WRITE(11,204)'LARGE MOS GROUP #',LG,' YCS'S USED= ',	MC8020
* (SYCSL(I),I=1,NYCSL)	MC8020
ELSE IF(MGX .GT. 0) THEN	MC8020
WRITE(11,204)'LARGE MOS GROUP #',LG,' YCS'S USED= ',	MC8020
* (SYCSL(I),I=1,NYCSL)	MC8020
WRITE(11,204)'MAJOR MOS GROUP #',MG,' YCS'S USED= ',	MC8020
* (SYCSM(I),I=1,NYCSM)	MC8021
ENDIF	MC8021
C --- PERFORM ALL BUT VECTOR ESTIMATION METHODS IN MC87BZ	MC8021
CALL MC87BZ(INV,Y,NRC,NYR,XTB,VXTB,XEB,A,MXX,MXY)	MC8021
C --- VECTOR METHOD--BREAK CELLS INTO VECTOR, CONDUCT ESTIMATION	MC8021
IF(ISFLAG .GT. 0) THEN	MC8021
CALL BKDOWN(PTBL,NPT,PTRTBL,NRCOLD,INDX,MKG,MXX,MXY,	MC8021
* SINV,SY,INV,Y,BKTBL,NBK)	MC8021
CALL MC87V(INV,Y,MXX,NYR,NRC,XTBJI,DELTA,X,XVYR,VYRINV,VYRY,	MC8021
* BSTAR,S,GAMMA,XBBJ,EVAL,MXP,MXK,BKTBL,NBK,NSC,NCSR,ISFLAG)	MC8021
ENDIF	MC8022
C	MC8022
201 FORMAT(/1X,A)	MC8022



202	FORMAT(1X,A,I2,A/1X,18(I3))	MC802230
203	FORMAT(1X,A,I2)	MC802240
204	FORMAT(1X,A,I1,A/1X,18(I3))	MC802250
	END	MC802260
C		MC802270
	*****	MC802280
C	SUBROUTINE EXPAND(NYCSX,SYCSX,VYC,NYE,IGX,LGX,MGX,LG,MG,RC)	MC802290
C ---	EXPAND YCS IF FEASIBLE, ELSE EXPAND MOS TO LG/MG	MC802300
	INTEGER SYCSX(31), NYCSX	MC802310
	INTEGER*2 VYC(NYE)	MC802320
C ---	FIND POSITION OF ORIGINALLY REQUESTED SYCS(1)	MC802330
	IY=0	MC802340
	DO 10 I=1,NYE	MC802350
	IF(SYCSX(I) .EQ. VYC(I)) IY=I	MC802360
10	CONTINUE	MC802370
	IF(IY.EQ.0) GO TO 30	MC802380
C ---	FIND NEAREST NON-ZERO YCS TO USE FOR EXPANSION	MC802390
	DO 20 I=1,NYE	MC802400
	J=IY-I	MC802410
	IF(J.GE.1) THEN	MC802420
	IF(VYC(J).GT.0) GO TO 50	MC802430
	ENDIF	MC802440
	J=IY+I	MC802450
	IF(J.LE.NYE) THEN	MC802460
	IF(VYC(J).GT.0) GO TO 50	MC802470
	ENDIF	MC802480
20	CONTINUE	MC802490
30	CONTINUE	MC802500
C ---	NO MORE YCS EXPANSION POSSIBLE. SEE IF MOS EXP. FEASIBLE	MC802510
	IF(IGX.GT.0) THEN	MC802520
C ---	EXPAND FROM GROUPS TO LARGE GROUP LGX	MC802530
	IGX=0	MC802540
	LGX=LG	MC802550
	ELSE IF(LGX.GT.0) THEN	MC802560
C ---	EXPAND FROM LARGE GROUP LGX TO MAJOR GROUP MGX	MC802570
	LGX=0	MC802580
	MGX=MG	MC802590
	ELSE	MC802600
	RC=1	MC802610
	ENDIF	MC802620
	RETURN	MC802630
C		MC802640
C ---	EXPAND WITH YCS IN POSITION J & CLEAR VYC(J)	MC802650
50	CONTINUE	MC802660
	NYCSX=NYCSX+1	MC802670
	SYCSX(NYCSX)=VYC(J)	MC802680
	VYC(J)=0	MC802690
	END	MC802700
C		MC802710
	*****	MC802720
C		MC802730
	FUNCTION NCEVAL(AIMIN,IGX,LGX,MGX,NYCSX,SYCSX,RETTBL,RETINV,	MC802740
*	NRET,MXX,LGRP,MGRP,NMS,AGGPCT,IGR,LG)	MC802750
C ---	COMPUTE ESTIMATED NO. CELLS TO BE OBTAINED WITH CURRENT EXPANSION	MC802760
	INTEGER SYCSX(31),NYCSX	MC802770
		MC802780

	INTEGER*2 LGRP(14),MGRP(6)	MC8027
	INTEGER*2 RETTBL(MXX, 3)	MC8028
	REAL RETINV(MXX)	MC8028
	NCEVAL=0	MC8028
	IF(IGX.EQ.0 .AND. LGX.EQ.0 .AND. MGX.EQ.0) RETURN	MC8028
	TAINV=0.0	MC8028
	DO 100 I=1,NRET	MC8028
C ---	SCREEN ON YCS	MC8028
	DO 10 J=1,NYCSX	MC8028
	IF(RETTBL(I,2) .EQ. SYCSX(J)) GO TO 15	MC8028
10	CONTINUE	MC8028
	GO TO 100	MC8029
C ---	SCREEN ON MOS BY GROUP, L.GRP OR MG DEPENDING ON IGX, LGX, MGX	MC8029
15	CONTINUE	MC8029
	MOS=RETTBL(I,1)	MC8029
	IGP=RETTBL(I,3)	MC8029
	LGP=LGRP(IGP)	MC8029
	IF(MGX .GT. 0) THEN	MC8029
	IF(MGRP(LGP) .EQ. MGX) THEN	MC8029
	IF(LGP .NE. LG) GO TO 80	MC8029
	ENDIF	MC8029
	ELSE IF(LGX .GT. 0) THEN	MC8030
	IF(LGP .EQ. LGX) THEN	MC8030
	IF(IGP .NE. IGR) GO TO 80	MC8030
	ENDIF	MC8030
	ELSE	MC8030
	IF(IGP .EQ. IGX) GO TO 80	MC8030
	ENDIF	MC8030
	GO TO 100	MC8030
80	CONTINUE	MC8030
C ---	ACCEPTED	MC8030
	IF(RETINV(I) .GE. AIMIN) THEN	MC8031
	NCEVAL=NCEVAL+1	MC8031
	ELSE	MC8031
	TAINV=TAINV+RETINV(I)	MC8031
	ENDIF	MC8031
100	CONTINUE	MC8031
C ---	FINAL ESTIMATE IS NCEVAL	MC8031
	IF(AIMIN.GT.0) NCEVAL=NCEVAL + AGGPCT*TAINV/AIMIN	MC8031
	END	MC8031
C		MC8031
	*****	MC8032
C		MC8032
	SUBROUTINE GETVYC(SYCS, LG, YCSB, NYE, NYB, NYEG, VYC)	MC8032
	INTEGER*2 YCSB(NYE, NYB, NYEG), VYC(NYE), LGEX(6)	MC8032
	INTEGER SYCS	MC8032
	DATA LGEX/4,4,1,2,4,3/	MC8032
C ---	L INDICATES LAST DIMENSION IN YCS EXPANSION TABLE	MC8032
	L=LGEX(LG)	MC8032
C ---	FIND TO WHICH YCS BLOCK SYCS BELONGS AND MAKE COPY IN VYC	MC8032
	DO 10 J=1,NYB	MC8032
	DO 20 I=1,NYE	MC8033
	IF(SYCS .EQ. YCSB(I,J,L)) THEN	MC8033
	DO 30 K=1,NYE	MC8033
	VYC(K)=YCSB(K,J,L)	MC8033
30	CONTINUE	MC8033

	RETURN	MC803350
	ENDIF	MC803360
20	CONTINUE	MC803370
10	CONTINUE	MC803380
	WRITE(6,*) '***** YCS NOT FOUND IN YCSB TABLE YCS=',SYCS	MC803390
	END	MC803400
C		MC803410
	*****	MC803420
C		MC803430
	SUBROUTINE READET(RETTL,RETINV,MXX,NRET, SGRD, NSC,SVCMP,	MC803440
	* NCSR,SCSRC, MG,LGRP,MGRP, MOSGR,NMS)	MC803450
C ---	READ TABLE WITH ALL EXISTING COMBINATIONS FOR SELECTION CRITERIA	MC803460
C ---	ACCEPT RECS WITH MATCHING PG,MG,CS,SVC. ACCEPT ALL YCS	MC803470
	INTEGER SVCMP(5), NSC, SVC	MC803480
	INTEGER SCSRC(16),NCSR, CS	MC803490
	INTEGER SGRD, PG	MC803500
	INTEGER MOS,YCS	MC803510
	INTEGER*2 MOSGR(2,NMS), MGRP(*),LGRP(*)	MC803520
	INTEGER*2 RETTL(MXX, 3)	MC803530
	REAL RETINV(MXX), AI	MC803540
	NRET=0	MC803550
	DO 10 I=1,999999	MC803560
	READ(10+SGRD,100,END=999) PG,MOS,YCS,SVC,CS, NRECS,AI	MC803570
	IF(PG .NE. SGRD) GO TO 10	MC803580
	IGR=IGFIND(MOS, MOSGR,NMS)	MC803590
	LG=LGRP(IGR)	MC803600
	IF(MGRP(LG) .NE. MG) GO TO 10	MC803610
	DO 20 J=1,NSC	MC803620
	IF(SVC .EQ. SVCMP(J)) GO TO 21	MC803630
20	CONTINUE	MC803640
	GO TO 10	MC803650
21	CONTINUE	MC803660
	DO 30 J=1,NCSR	MC803670
	IF(CS .EQ. SCSRC(J)) THEN	MC803680
	CALL ACCEPT(MOS,YCS,IGR,RETTL,MXX,NRET,RETINV,AI)	MC803690
	GO TO 10	MC803700
	ENDIF	MC803710
30	CONTINUE	MC803720
C		MC803730
10	CONTINUE	MC803740
999	CONTINUE	MC803750
	IF(NRET .GT. MXX) THEN	MC803760
	WRITE(6,*) '***** ERROR - TOO MANY RECORDS IN RETTL'	MC803770
	STOP	MC803780
	ENDIF	MC803790
100	FORMAT(I2,I4,I3,I2,I3,I4,F7.2)	MC803800
	END	MC803810
C		MC803820
	*****	MC803830
C		MC803840
	SUBROUTINE ACCEPT(MOS,YCS,IGR, RETTL,MXX,NRET,RETINV,AI)	MC803850
C ---	ACCEPT ENTRY. ACCUMULATE IF ALREADY SAME COMBINATION IS PRESENT	MC803860
	INTEGER MOS,YCS	MC803870
	INTEGER*2 RETTL(MXX, 3)	MC803880
	REAL RETINV(MXX), AI	MC803890
	DO 10 I=1,NRET	MC803900

IF(MOS.EQ.RETTBL(I,1) .AND. YCS.EQ.RETTBL(I,2) ) THEN	MC8039
RETINV(I)=RETINV(I) + AI	MC8039
RETURN	MC8039
ENDIF	MC8039
10 CONTINUE	MC8039
C --- NEW COMBINATION	MC8039
NRET=NRET+1	MC8039
RETTBL(NRET,1)=MOS	MC8039
RETTBL(NRET,2)=YCS	MC8039
RETTBL(NRET,3)=IGR	MC8040
RETINV(NRET)=AI	MC8040
END	MC8040
C	MC8040
*****	MC8040
C	MC8040
SUBROUTINE GETPAR(AIMIN,NO,NMOS,SMOS,NYCS,SYCS,SGRD,	MC8040
* NSC,SVCMP, NCSR,SCSRC, IGR,MOSGR,NMS, ISFLAG)	MC8040
C --- GET SELECTION CRITERIA FROM USER AND VALIDATE	MC8040
INTEGER SYCS(31), NYCS	MC8040
INTEGER SMOS(20), NMOS	MC8041
INTEGER SVCMP(5), NSC	MC8041
INTEGER SCSRC(16),NCSR	MC8041
INTEGER SGRD	MC8041
INTEGER*2 MOSGR(2,NMS)	MC8041
WRITE(5,*) ' ENTER THRESHOLD MIN. FOR AVERAGE INVENTORY'	MC8041
READ(5,*) AIMIN	MC8041
WRITE(5,*) ' ENTER THRESHOLD MIN. FOR NUMBER OF CELLS'	MC8041
READ(5,*) NO	MC8041
WRITE(5,*) ' THRESHOLDS TO USE AIMIN, NO=',AIMIN,NO	MC8041
C	MC8042
WRITE(5,*) ' ENTER MOS (ONLY 1 ACCEPTED)'	MC8042
NMOS=1	MC8042
READ(5,*) SMOS(1)	MC8042
WRITE(6,*) ' MOS SELECTED:', SMOS(1)	MC8042
IGR=IGFIND(SMOS(1), MOSGR,NMS)	MC8042
WRITE(6,*) ' GROUP TO USE:', IGR	MC8042
IF(IGR.EQ.0) THEN	MC8042
WRITE(5,*) '***** ERROR - INVALID MOS SELECTED:',SMOS(1)	MC8042
STOP	MC8042
ENDIF	MC8043
C	MC8043
WRITE(5,*) ' ENTER YCS (ONLY 1 ACCEPTED)'	MC8043
NYCS=1	MC8043
READ(5,*) SYCS(1)	MC8043
WRITE(6,*) ' YCS SELECTED:', SYCS(1)	MC8043
C	MC8043
WRITE(5,*) ' ENTER GRADE'	MC8043
READ(5,*) SGRD	MC8043
WRITE(6,*) ' GRADE SELECTED', SGRD	MC8043
C	MC8044
WRITE(5,*) ' ENTER NO. OF SVC. COMPS & ARRAY (1-3, 4=1+2, 5=ALL)'	MC8044
READ(5,*) NSC, (SVCMP(I), I=1,NSC)	MC8044
C --- EXPAND 4 TO 1,2 AND 5 TO 1,2,3	MC8044
DO 10 I=1,NSC	MC8044
IF(SVCMP(I).EQ.4 .OR. SVCMP(I).EQ.5) THEN	MC8044
NSC=SVCMP(I)-2	MC8044



DO 15 J=1,NSC	MC804470
SVCMP(J)=J	MC804480
15 CONTINUE	MC804490
GO TO 11	MC804500
ENDIF	MC804510
10 CONTINUE	MC804520
11 CONTINUE	MC804530
WRITE(6,*) ' SERVICE COMPONENTS SELECTED', (SVCMP(I), I=1,NSC)	MC804540
C WRITE(5,*) ' ENTER NO. COMM. SOURCES AND ARRAY (1-15, 16=ALL)'	MC804550
READ(5,*) NCSR, (SCSRC(I), I=1,NCSR)	MC804560
C --- IF 16 IS SELECTED THEN EXPAND ARRAY TO COVER ALL 1-15	MC804570
DO 20 I=1,NCSR	MC804580
IF(SCSRC(I) .EQ. 16) THEN	MC804590
NCSR=15	MC804600
DO 25 J=1,NCSR	MC804610
SCSRC(J)=J	MC804620
25 CONTINUE	MC804630
GO TO 26	MC804640
ENDIF	MC804650
20 CONTINUE	MC804660
26 CONTINUE	MC804670
WRITE(5,*) ' COMM. SOURCES SELECTED:', (SCSRC(I), I=1,NCSR)	MC804680
C	MC804690
C --- FLAG TO DETERMINE WHICH OF SVC OR CS WILL BE USED AS 3RD DIMENSION	MC804700
WRITE(5,*) 'SELECT 3RD DIM. TO USE: 0=NONE, 1=SVC, 2=COMM. SOURCE'	MC804710
READ(5,*) ISFLAG	MC804720
C --- WRITE INPUT PARAMETER INFO TO OUTPUT FILE	MC804730
WRITE(11,101) 'TEST CASE INPUT PARAMETERS:'	MC804740
WRITE(11,102) 'INVENTORY THRESHOLD= ',AIMIN,	MC804750
* 'THRESHOLD NO. OF CELLS= ',NO	MC804760
WRITE(11,103) 'MOS= ',SMOS(1),'YCS= ',SYCS(1),'GRADE= ',SGRD	MC804770
WRITE(11,104) 'SERVICE COMPONENTS= ',(SVCMP(I),I=1,NSC)	MC804780
WRITE(11,104) 'COMM SOURCES= ',(SCSRC(I),I=1,NCSR)	MC804790
WRITE(6,*) '3RD DIMENSION= ',ISFLAG	MC804800
C	MC804810
101 FORMAT(1X,A)	MC804820
102 FORMAT(1X,A,F4.1,7X,A,I2)	MC804830
103 FORMAT(1X,A,I3,2(5X,A,I2))	MC804840
104 FORMAT(1X,A,15(I3))	MC804850
END	MC804860
C	MC804870
*****	MC804880
C	MC804890
SUBROUTINE GETMOS(SMOS,NMOS,MGX,LGX,MG,LG,IGR,MOSGR,LGRP,MGRP,	MC804900
* NMS,NG,NLG)	MC804910
C --- BUILD SMOS ARRAY BASED UPON EXPANSION	MC804920
INTEGER SMOS(30)	MC804930
INTEGER*2 MOSGR(2,NMS), LGRP(NG), MGRP(NLG)	MC804940
NMOS=0	MC804950
IF(MGX .GT. 0) THEN	MC804960
C --- HAVE EXPANDED TO MAJOR MOS GROUP	MC804970
DO 10 I=1,NMS	MC804980
IGP=MOSGR(2,I)	MC804990
LGP=LGRP(IGP)	MC805000
IF(MGRP(LGP) .EQ. MG) THEN	MC805010
	MC805020



	NMOS=NMOS+1	MC8050
	SMOS(NMOS)=MOSGR(1,I)	MC8050
	ENDIF	MC8050
10	CONTINUE	MC8050
	RETURN	MC8050
	ELSE IF(LGX .GT. 0) THEN	MC8050
C ---	HAVE EXPANDED TO LARGE MOS GROUP	MC8050
	DO 20 I=1,NMS	MC8051
	IGP=MOSGR(2,I)	MC8051
	IF(LGRP(IGP) .EQ. LG) THEN	MC8051
	NMOS=NMOS+1	MC8051
	SMOS(NMOS)=MOSGR(1,I)	MC8051
	ENDIF	MC8051
20	CONTINUE	MC8051
	RETURN	MC8051
	ELSE	MC8051
C ---	HAVE EXPANDED TO SMALL MOS GROUP	MC8051
	DO 30 I=1,NMS	MC8052
	IF(MOSGR(2,I) .EQ. IGR) THEN	MC8052
	NMOS=NMOS+1	MC8052
	SMOS(NMOS)=MOSGR(1,I)	MC8052
	ENDIF	MC8052
30	CONTINUE	MC8052
	RETURN	MC8052
	ENDIF	MC8052
	END	MC8052
C		MC8052
*****		MC8053
C		MC8053
	FUNCTION IGFIND(MOS, MOSGR,NMS)	MC8053
C ---	FIND LOCATION OF MATCHING MOS IN GROUP TABLE. RETURN GROUP NO	MC8053
	INTEGER*2 MOSGR(2,NMS)	MC8053
	DO 10 I=1,NMS	MC8053
	IF(MOSGR(1,I) .EQ. MOS) THEN	MC8053
		IGFIND=MOSGR(2,I)
		RETURN
	ENDIF	MC8053
10	CONTINUE	MC8054
	IGFIND=0	MC8054
	END	MC8054
C		MC8054
*****		MC8054
C		MC8054
	SUBROUTINE READER(DATA, INV, Y, MXX, NMOS, NYCSG, NYCSL, NYCSM, NSC, NCSR,	MC8054
	* NYR, SMOS, SYCSG, SYCSL, SYCSM, SGRD, SVCMP, SCSRC, NRC, PTRTBL, LGX, MGX,	MC8054
	* IGR, LG, MGRP, LGRP, MOSGR, NMS, NG, NLG, ICYCLE, NPT, PTBL, ISFLAG, SINV, SY)	MC8054
	REAL INV(MXX, NYR), Y(MXX, NYR), SINV(MXX, NYR), SY(MXX, NYR)	MC8054
	INTEGER*2 PTRTBL(MXX, 2), PTBL(MXX, 3)	MC8055
	INTEGER SYCSG(*), SYCSL(*), SYCSM(*)	MC8055
	INTEGER SMOS(*), NMOS	MC8055
	INTEGER SVCMP(*), NSC	MC8055
	INTEGER SCSRC(*), NCSR	MC8055
	INTEGER SGRD	MC8055
	INTEGER TYPE, YCS, PG, MOS, SEX, CS, EDLV, SVC, MOS1, MOS2, RACE	MC8055
	INTEGER DATA(NYR)	MC8055
	CHARACTER*7 CITLS	MC8055

INTEGER*2 MOSGR(2,NMS),LGRP(NG),MGRP(NLG)	MC805590
C	MC805600
C --- REWIND DATA FILE AND RESET INV,Y IF CYCLING THRU READER	MC805610
IF(ICYCLE .GT. 1) THEN	MC805620
REWIND 1	MC805630
DO 6 I=1,MXX	MC805640
DO 5 J=1,NYR	MC805650
INV(I,J)=0.0	MC805660
Y(I,J)=0.0	MC805670
SINV(I,J)=0.0	MC805680
SY(I,J)=0.0	MC805690
5        CONTINUE	MC805700
6        CONTINUE	MC805710
ENDIF	MC805720
C --- READ RECORD AND STORE IN MATRIX	MC805730
ICR=0	MC805740
NRC=0	MC805750
NPT=0	MC805760
ICNT=0	MC805770
IYNO=0	MC805780
IYR=0	MC805790
C	MC805800
1 READ(1,101,END=999) TYPE,YCS,PG,MOS,SEX,CS,EDLV,SVC,MOS1,MOS2,	MC805810
* RACE,CITLS,DATA	MC805820
ICR=ICR+1	MC805830
C --- CHECK IF RECORD MEETS SELECTION CRITERIA. OTHERWISE REJECT.	MC805840
C --- COLLECT TYPES 0=INVENTORY, AND 1-5 ALL LOSSES	MC805850
IF(TYPE.GT.5) GO TO 999	MC805860
C	MC805870
C --- SCREEN FOR GRADE	MC805880
IF(PG .NE. SGRD) GO TO 1	MC805890
C	MC805900
C --- SCREEN FOR MOS	MC805910
IGP=IGFIND(MOS,MOSGR,NMS)	MC805920
IF(IGP.EQ.0) GO TO 1	MC805930
LGP=LGRP(IGP)	MC805940
IF(MGX .GT. 0) THEN	MC805950
C --- HAVE EXPANDED TO MAJOR MOS GROUP	MC805960
IF(LGP .EQ. LG) THEN	MC805970
DO 10 I=1,NYCSL	MC805980
IF(YCS .EQ. SYCSL(I)) THEN	MC805990
IY=I	MC806000
GO TO 60	MC806010
ENDIF	MC806020
10        CONTINUE	MC806030
GO TO 1	MC806040
ELSE IF(MGRP(LGP) .EQ. MGX) THEN	MC806050
DO 20 I=1,NYCSM	MC806060
IF(YCS .EQ. SYCSM(I)) THEN	MC806070
IY=I	MC806080
GO TO 60	MC806090
ENDIF	MC806100
20        CONTINUE	MC806110
GO TO 1	MC806120
ELSE	MC806130
GO TO 1	MC806140

	ENDIF	MC8061
	ELSE IF(LGX .GT. 0) THEN	MC8061
C ---	HAVE EXPANDED TO LARGE MOS GROUP	MC8061
	IF(IGP .EQ. IGR) THEN	MC8061
	DO 30 I=1,NYCSG	MC8061
	IF(YCS .EQ. SYCSG(I)) THEN	MC8062
	IY=I	MC8062
	GO TO 60	MC8062
	ENDIF	MC8062
30	CONTINUE	MC8062
	GO TO 1	MC8062
	ELSE IF(LGP .EQ. LGX) THEN	MC8062
	DO 40 I=1,NYCSL	MC8062
	IF(YCS .EQ. SYCSL(I)) THEN	MC8062
	IY=I	MC8062
	GO TO 60	MC8063
	ENDIF	MC8063
40	CONTINUE	MC8063
	GO TO 1	MC8063
	ELSE	MC8063
	GO TO 1	MC8063
	ENDIF	MC8063
	ELSE	MC8063
C ---	HAVE EXPANDED TO SMALL MOS GROUP	MC8063
	IF(IGP .EQ. IGR) THEN	MC8063
	DO 50 I=1,NYCSG	MC8064
	IF(YCS .EQ. SYCSG(I)) THEN	MC8064
	IY=I	MC8064
	GO TO 60	MC8064
	ENDIF	MC8064
50	CONTINUE	MC8064
	GO TO 1	MC8064
	ELSE	MC8064
	GO TO 1	MC8064
	ENDIF	MC8064
	ENDIF	MC8065
60	CONTINUE	MC8065
C		MC8065
	DO 70 I=1,NMOS	MC8065
	IF(MOS .EQ. SMOS(I)) THEN	MC8065
	IM=I	MC8065
	GO TO 80	MC8065
	ENDIF	MC8065
70	CONTINUE	MC8065
	WRITE(6,*) '*** ERROR IN MOS SCREENING ***',MOS	MC8065
	WRITE(6,*) 'NMOS,SMOS=',NMOS,(SMOS(I),I=1,NMOS)	MC8066
	GO TO 1	MC8066
C		MC8066
C ---	SCREEN FOR SERVICE COMPONENT	MC8066
80	CONTINUE	MC8066
	DO 90 I=1,NSC	MC8066
	IF(SVC .EQ. SVCMP(I)) THEN	MC8066
	IS=I	MC8066
	GO TO 100	MC8066
	END IF	MC8066
90	CONTINUE	MC8067

GO TO 1	MC806710
C	MC806720
C --- SCREEN FOR COMMISSIONING SOURCE	MC806730
100 CONTINUE	MC806740
DO 110 I=1,NCSR	MC806750
IF(CS .EQ. SCSRC(I)) THEN	MC806760
IR=I	MC806770
GO TO 120	MC806780
END IF	MC806790
110 CONTINUE	MC806800
GO TO 1	MC806810
C	MC806820
120 CONTINUE	MC806830
C	MC806840
C --- RECORD ACCEPTED - INSTALL IT IN INV,Y,SINV,SY, PTRTBL AND PTBL	MC806850
ICNT=ICNT+1	MC806860
IF(ISFLAG.EQ. 1) THEN	MC806870
IW=IS	MC806880
ELSE IF(ISFLAG.EQ. 2) THEN	MC806890
IW=IR	MC806900
ELSE	MC806910
IW=-99	MC806920
ENDIF	MC806930
MINV=GINV(PTRTBL, MXX,NRC, IM,IY,-99)	MC806940
MV=GINV(PTBL, MXX,NPT,IM,IY,IW)	MC806950
IF(TYPE.EQ. 0) THEN	MC806960
CALL INSINV(PTRTBL,MXX,NYR,NRC,MINV,IM,IY,-99,INV,DATA)	MC806970
CALL INSINV(PTBL, MXX,NYR,NPT,MV, IM,IY, IW,SINV,DATA)	MC806980
ELSE	MC806990
CALL INSY(MXX,NYR,MINV,Y,DATA)	MC807000
CALL INSY(MXX,NYR,MV, SY,DATA)	MC807010
IYR=IYR+1	MC807020
IF(MINV.EQ. 0) THEN	MC807030
WRITE(6,*) '*** ERROR IN DATA BASE. LOSS W/O INV. REC. '	MC807040
WRITE(6,122) 'Y**:', MOS,YCS,PG,EDLV,SVC,RACE,	MC807050
* (DATA(IT), IT=1,NYR)	MC807060
IYNO=IYNO+1	MC807070
ENDIF	MC807080
ENDIF	MC807090
C	MC807100
GO TO 1	MC807110
C	MC807120
999 CONTINUE	MC807130
WRITE(6,*) ' '	MC807140
WRITE(6,*) 'TOTAL RECORDS READ =',ICR	MC807150
WRITE(6,*) 'TOTAL INV. MOS/YCS COMBINATIONS=',NRC	MC807160
WRITE(6,*) 'TOTAL INV. MOS/YCS/IW COMBINATIONS=',NPT	MC807170
WRITE(6,*) 'TOTAL RECORDS ACCEPTED =',ICNT	MC807180
WRITE(6,*) 'TOTAL LOSS RECORDS ACCEPTED =',IYR	MC807190
WRITE(6,*) 'TOTAL LOSS RECORDS NOT MATCHED =',IYNO	MC807200
C --- TERMINATE IF NO DATA COLLECTED	MC807210
IF(NRC .EQ. 0) THEN	MC807220
WRITE(6,*) '***** NO DATA MEETS SELECTION REQS'	MC807230
STOP	MC807240
ENDIF	MC807250
C	MC807260



101	FORMAT(3I2,I3,I1,I2,2I1,2I3,I1,A7, 1X, 10I4)	MC8071
121	FORMAT(A8,13I6)	MC8071
122	FORMAT(A8,7I6, 5X, 12I6)	MC8071
131	FORMAT(I4, 2I6)	MC8071
132	FORMAT(I4, 3I6, 10F7.2)	MC8071
	END	MC8071
C		MC8071
*****		
C		MC8071
	FUNCTION GINV(PTBL, MXX,NPT, IM,IY,IW)	MC8071
C ---	FIND LOCATION OF INVENTORY ENTRY FOR MOS,YCS,SVC/CS COMBINATIONS	MC8071
C ---	3RD DIMENSION CHECKED ONLY IN CASE IW>0	MC8071
	INTEGER*2 PTBL(MXX, *)	MC8071
	DO 10 I=1,NPT	MC8071
	IF(PTBL(I, 1) .EQ. IM .AND.	MC8071
*	PTBL(I, 2) .EQ. IY ) THEN	MC8071
	IF(IW.LT.0 .OR. (IW.GT.0 .AND. PTBL(I, 3).EQ.IW)) THEN	MC8071
	GINV=I	MC8071
	RETURN	MC8071
	ENDIF	MC8071
	ENDIF	MC8071
10	CONTINUE	MC8071
	GINV=0	MC8071
	END	MC8071
C		MC8071
*****		
C		MC8071
	SUBROUTINE INSINV(PT,MXX,NYR,N,K,IM,IY,IW,INV,DATA)	MC8071
C ---	ACCUIM INTO KTH ENTRY. INSTALL IN POINTER TABLE IF NOT PRESENT	MC8071
	REAL INV(MXX, NYR)	MC8071
	INTEGER*2 PT(MXX, *)	MC8071
	INTEGER DATA(NYR)	MC8071
	IF(K .EQ. 0) THEN	MC8071
C ---	ADD NEW ENTRY	MC8071
	N=N+1	MC8071
	IF(N .GT. MXX) THEN	MC8071
	WRITE(6,*) '*** ERROR - TOO MANY INV. COMBINATIONS',N	MC8071
	STOP	MC8071
	ENDIF	MC8071
	K=N	MC8071
	PT(K, 1)=IM	MC8071
	PT(K, 2)=IY	MC8071
	IF(IW.GT.0) PT(K, 3)=IW	MC8071
	ENDIF	MC8071
	DO 130 IT=1,NYR	MC8071
	INV(K,IT)=INV(K,IT) + .25*FLOAT(DATA(IT))	MC8071
130	CONTINUE	MC8071
	END	MC8071
C		MC8071
*****		
C		MC8071
	SUBROUTINE INSY(MXX,NYR,K,Y,DATA)	MC8071
C ---	ACCUIM INTO KTH ENTRY FOR LOSS	MC8071
	REAL Y(MXX, NYR)	MC8071
	INTEGER DATA(NYR)	MC8071
	IF(K .EQ. 0) RETURN	MC8071



DO 10 IT=1,NYR	MC807830
Y(K,IT)=Y(K,IT) + DATA(IT)	MC807840
10 CONTINUE	MC807850
END	MC807860
C	MC807870
*****	MC807880
C	MC807890
SUBROUTINE AGGREG(INV,Y,MXX,NYR,SMOS,SYCSG,	MC807900
* NRC,NRCOLD,PTRTBL,INDX,AVINV, AIMIN,MKG)	MC807910
C --- COMP. AVERAGE INV. & SORT	MC807920
REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX)	MC807930
INTEGER*2 PTRTBL(MXX, 2), INDX(MXX),MKG(MXX)	MC807940
INTEGER SYCSG(*), SMOS(*)	MC807950
REAL*8 TINV,TY	MC807960
C	MC807970
C --- RESET MKG (NECESSARY WHEN CYCLING THRU AGGPCT VALUES)	MC807980
DO 10 I=1,MXX	MC807990
MKG(I)=0	MC808000
10 CONTINUE	MC808010
TINV=0	MC808020
TY=0	MC808030
DO 100 I=1,NRC	MC808040
C --- FIX INV. ENTRIES LOWER THAN CORRESP. LOSSES & COMP. AVG INV.	MC808050
AI=0	MC808060
DO 201 J=1,NYR	MC808070
TINV=TINV+INV(I,J)	MC808080
TY= TY+ Y(I,J)	MC808090
IF(INV(I,J).LT.Y(I,J)) INV(I,J)=Y(I,J)	MC808100
AI=AI+INV(I,J)	MC808110
201 CONTINUE	MC808120
AVINV(I)=AI/NYR	MC808130
INDX(I)=I	MC808140
100 CONTINUE	MC808150
WRITE(6,*) '==== TOTAL INV,Y=',TINV,TY	MC808160
C	MC808170
C --- SORT ASCENDING BY AVG INVENTORY	MC808180
CALL SORT2(AVINV,INDX,NRC)	MC808190
C	MC808200
NS1=0	MC808210
C --- DISPLAY TABLE IN SORT SEQUENCE	MC808220
CALL DSPTBL(INV,Y,AVINV,PTRTBL,INDX,AIMIN,NRC,MKG,MXX,NYR,	MC808230
* SYCSG,SMOS )	MC808240
C	MC808250
DO 200 K=NRC,1,-1	MC808260
IF(AVINV(K) .GE. AIMIN) THEN	MC808270
C --- MARK AS MEMBER OF SET S0	MC808280
MKG(K)=32767	MC808290
ELSE	MC808300
C --- INITIAL COUNT OF MEMBERS OF SET S1	MC808310
NS1=K	MC808320
GO TO 202	MC808330
ENDIF	MC808340
200 CONTINUE	MC808350
202 CONTINUE	MC808360
C --- DO AGGREGATIONS WITHIN SET S1 UNTIL NO MORE POSSIBLE (KF GE 0)	MC808370

	KF=-1	MC8081
C ---	DO WHILE KF<0	MC8083
300	IF(KF.GE.0) GO TO 310	MC8084
	CALL AGG1(AVINV,INDX,MKG,NS1,INV,Y,MXX,NYR,AIMIN,KF)	MC8084
	GO TO 300	MC8084
310	CONTINUE	MC8084
C ---	DISPLAY TABLE AFTER 1ST AGGREGATION	MC8084
	CALL DSPTBL(INV,Y,AVINV,PTRTBL,INDX,AIMIN,NRC,MKG,MXX,NYR,	MC8084
	* SYCSG,SMOS )	MC8084
	IF(NS1.EQ.NRC) THEN	MC8084
	WRITE(6,*) '***** SET S0 EMPTY. NO CELLS ABOVE THRESHOLD'	MC8084
	STOP	MC8084
	ENDIF	MC8085
C ---	DO AGGREGATIONS FROM SET S1 INTO SET S0 UNTIL NO MORE POSSIBLE	MC8085
	KF=1	MC8085
C ---	DO WHILE KF>0	MC8085
320	IF(KF.LE.0) GO TO 330	MC8085
	CALL AGG2(AVINV,INDX,MKG,NS1,NRC,INV,Y,MXX,NYR, KF)	MC8085
	GO TO 320	MC8085
330	CONTINUE	MC8085
C ---	DISPLAY TABLE AFTER 2ND AGGREGATION	MC8085
	CALL DSPTBL(INV,Y,AVINV,PTRTBL,INDX,AIMIN,NRC,MKG,MXX,NYR,	MC8085
	* SYCSG,SMOS )	MC8086
C ---	MOVE VALUES GE AIMIN TO BEGINNING OF ARRAYS	MC8086
	CALL CMPRS(INV,Y,MXX,NYR,NRC,NRCOLD,AIMIN,AVINV)	MC8086
C ---	DISPLAY TABLE AFTER MOVING VALUES.	MC8086
	DO 400 K=1,NRC	MC8086
	WRITE(6,122)K,AVINV(K), (INV(K,J),J=1,NYR)	MC8086
	WRITE(6,123) ( Y(K,J),J=1,NYR)	MC8086
400	CONTINUE	MC8086
122	FORMAT(/I5,14X,F8.3, 6X, 10F7.2)	MC8086
123	FORMAT( 33X, 10F7.2)	MC8086
	END	MC8087
C *****		MC8087
	SUBROUTINE AGG1(AVINV,INDX,MKG,NS1,INV,Y,MXX,NYR,AIMIN,KF)	MC8087
C ---	DO ONE PASS OF AGGREGATION	MC8087
	REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX)	MC8087
	INTEGER*2 INDX(MXX),MKG(MXX)	MC8087
	KF=0	MC8087
	CI=0	MC8087
	DO 10 I=NS1,1,-1	MC8087
	IF(MKG(I).EQ.0) THEN	MC8087
	IF(KF.EQ.0) THEN	MC8088
C ---	THIS WILL BE THE COLLECTING CELL	MC8088
	KF=I	MC8088
	CI=AVINV(I)	MC8088
	ELSE	MC8088
	IF(CI+AVINV(I).LT.AIMIN) THEN	MC8088
C ---	ACCUM. WITH CELL KF TEMPORARILY. SET TEMP. POINTER -KF	MC8088
	CI=CI+AVINV(I)	MC8088
	MKG(I)=-KF	MC8088
	ELSE	MC8088
C ---	FIND SMALLEST CELL TO ADD	MC8089
	CALL AGG1A(AVINV,MKG,I,CI,AIMIN,KF,MXX)	MC8089
	ENDIF	MC8089

	IF(CI.GE.AIMIN) THEN	MC808930
C ---	MAKE THIS AGGREGATION PERMANENT AND EXIT	MC808940
	AVINV(KF)=CI	MC808950
	CALL AGG1B(INDX,MKG,KF,INV,Y,NYR,MXX)	MC808960
	NS1=NS1-1	MC808970
	MKG(KF)=32767	MC808980
	KF=-1	MC808990
	RETURN	MC809000
	ENDIF	MC809010
	ENDIF	MC809020
	ENDIF	MC809030
10	CONTINUE	MC809040
C		MC809050
	IF(KF.EQ.0) RETURN	MC809060
C ---	CLEAR TEMPORARY POINTERS LEFT. THIS WAS AN UNSUCCESSFUL AGGREG.	MC809070
	DO 20 I=1,NS1	MC809080
	IF(MKG(I).LT.0) MKG(I)=0	MC809090
20	CONTINUE	MC809100
	END	MC809110
C *****		MC809120
	SUBROUTINE AGG1A(AVINV,MKG,ILAST,CI,AIMIN,KF,MXX)	MC809130
C ---	FIND SMALLEST CELL TO ADD AND SET TEMPORARY POINTER	MC809140
	REAL AVINV(MXX)	MC809150
	INTEGER*2 MKG(MXX)	MC809160
	DO 10 I=1,ILAST	MC809170
	IF(MKG(I).EQ.0) THEN	MC809180
	IF(CI+AVINV(I).GE. AIMIN) THEN	MC809190
	CI=CI+AVINV(I)	MC809200
	MKG(I)=-KF	MC809210
	RETURN	MC809220
	ENDIF	MC809230
	ENDIF	MC809240
10	CONTINUE	MC809250
	WRITE(6,*) '*** ERROR IN AGG1A. NO VALUE FOUND ***'	MC809260
	STOP	MC809270
	END	MC809280
C *****		MC809290
	SUBROUTINE AGG1B(INDX,MKG,KF,INV,Y,NYR,MXX)	MC809300
C ---	MAKE AGGREGATION PERMANENT	MC809310
	REAL INV(MXX, NYR), Y(MXX, NYR)	MC809320
	INTEGER*2 INDX(MXX),MKG(MXX)	MC809330
	K=INDX(KF)	MC809340
	DO 10 I=1,KF-1	MC809350
	IF(MKG(I).LT. 0) THEN	MC809360
	IF(MKG(I).NE. -KF) STOP 777	MC809370
	MKG(I)=KF	MC809380
	L=INDX(I)	MC809390
	DO 20 J=1,NYR	MC809400
	INV(K,J)=INV(K,J)+INV(L,J)	MC809410
	Y(K,J)= Y(K,J)+ Y(L,J)	MC809420
20	CONTINUE	MC809430
	ENDIF	MC809440
10	CONTINUE	MC809450
	END	MC809460
C *****		MC809470

	SUBROUTINE AGG2(AVINV,INDX,MKG,NS1,NRC,INV,Y,MXX,NYR, KF)	MC8094
C ---	DO ONE PASS OF AGGREGATION FROM SET S1 TO SET S0	MC8094
C ---	ON EACH PASS ONE ELEMENT OF S1 IS TAKEN & ADDED TO SMALLEST OF S0	MC8095
	REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX)	MC8095
	INTEGER*2 INDX(MXX),MKG(MXX)	MC8095
	KF=0	MC8095
C ---	FIND ELEMENT OF S1 (ONLY THOSE WITH POINTER MKG(I)=0)	MC8095
	DO 10 I=1,NS1	MC8095
	IF(MKG(I).EQ.0) THEN	MC8095
	KF=I	MC8095
	GO TO 12	MC8095
	ENDIF	MC8095
	10 CONTINUE	MC8096
	12 CONTINUE	MC8096
C ---	IF KF STILL 0 THEN NO MORE ELEMENTS IN S1 LEFT	MC8096
	IF(KF.EQ.0) RETURN	MC8096
C		MC8096
C ---	FIND SMALLEST ELEMENT OF S0 AND ADD TO IT. ONLY WITH MKG(I)=32767	MC8096
	ISM=NRC	MC8096
	SMALL=AVINV(ISM)	MC8096
	DO 20 I=1, NRC	MC8096
	IF(MKG(I).EQ.32767) THEN	MC8096
	IF(AVINV(I).LT.SMALL) THEN	MC8097
	ISM=I	MC8097
	SMALL=AVINV(I)	MC8097
	ENDIF	MC8097
	ENDIF	MC8097
	20 CONTINUE	MC8097
C ---	JOIN ELEMENT KF TO ELEMENT ISM	MC8097
	AVINV(ISM)=AVINV(ISM) + AVINV(KF)	MC8097
	MKG(KF)=ISM	MC8097
	L=INDX(KF)	MC8097
	K=INDX(ISM)	MC8098
	DO 30 J=1,NYR	MC8098
	INV(K,J)=INV(K,J)+INV(L,J)	MC8098
	Y(K,J)= Y(K,J)+ Y(L,J)	MC8098
	30 CONTINUE	MC8098
	END	MC8098
C *****		MC8098
	SUBROUTINE CMPRS(INV,Y,MXX,NYR,NRC,NRCOLD,AIMIN,AVINV)	MC8098
	REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX)	MC8098
C ---	COMPRESS INV,Y IN PLACE. MOVE ALL ROWS GE AIMIN TO TOP	MC8098
	NRCOLD=NRC	MC8099
	NRC=0	MC8099
	DO 10 I=1,NRCOLD	MC8099
	AI=CAINV(INV,I,MXX,NYR)	MC8099
	IF(AI .GE. AIMIN) THEN	MC8099
C ---	TRANSFER ACTIVE CELL I ---> NRC	MC8099
	NRC=NRC+1	MC8099
	AVINV(NRC)=AI	MC8099
	DO 20 J=1,NYR	MC8099
	INV(NRC,J)=INV(I,J)	MC8099
	Y(NRC,J)= Y(I,J)	MC8100
	20 CONTINUE	MC8100
	ENDIF	MC8100
	10 CONTINUE	MC8100



	END	MC810040
C	*****	MC810050
	FUNCTION CAINV(INV,I,MXX,NYR)	MC810060
	REAL INV(MXX, NYR)	MC810070
C	--- COMPUTE AVERAGE INVENTORY FOR ROW I	MC810080
	CAINV=0	MC810090
	DO 10 J=1,NYR	MC810100
	CAINV=CAINV+INV(I,J)	MC810110
10	CONTINUE	MC810120
	CAINV=CAINV/NYR	MC810130
	END	MC810140
C	*****	MC810150
	SUBROUTINE DSPTBL(INV,Y,AVINV,PTRTBL,INDX,AIMIN,NRC,MKG,MXX,NYR,	MC810160
	* SYCSG,SMOS)	MC810170
C	--- DISPLAY TABLE IN SORT SEQUENCE	MC810180
	REAL INV(MXX, NYR), Y(MXX, NYR), AVINV(MXX)	MC810190
	INTEGER*2 PTRTBL(MXX, 2), INDX(MXX),MKG(MXX)	MC810200
	INTEGER SYCSG(*)	MC810210
	INTEGER SMOS(*)	MC810220
	INTEGER IATT(2)	MC810230
	CHARACTER*1 STI	MC810240
	WRITE(6,121)	MC810250
	WRITE(6,*) 'INV. THRESHOLD MIN. VALUE=',AIMIN	MC810260
C		MC810270
	WRITE(6,*) ' I INDX AVG MKG INVENTORY/LOSSES'	MC810280
	DO 200 K=1,NRC	MC810290
	STI=' '	MC810300
	I=INDX(K)	MC810310
	AI=AVINV(K)	MC810320
	IF(AI .LT. AIMIN) STI='\$'	MC810330
	IATT(1)=SMOS(PTRTBL(I,1))	MC810340
	IATT(2)=SYCSG(PTRTBL(I,2))	MC810350
	WRITE(6,122)K,I,AI,MKG(K),STI,(INV(I,J),J=1,NYR),(IATT(J),J=1,2),	MC810360
	* PTRTBL(I,1),PTRTBL(I,2)	MC810370
	WRITE(6,123) ( Y(I,J),J=1,NYR)	MC810380
200	CONTINUE	MC810390
C		MC810400
	121 FORMAT(///)	MC810410
	122 FORMAT(/2I5,F8.3,I9,1X,A2, 10F7.2, 5X, 6I5)	MC810420
	123 FORMAT( 30X, 10F7.2)	MC810430
	END	MC810440
C	*****	MC810450
	SUBROUTINE SORT2(Y,INDX, N)	MC810460
C	--- INPLACE SORT USING SHELL ALGORITHM *****	MC810470
C	--- SORTS ON Y AND DOES SAME REORDERING ON INDEXES INDX	MC810480
	REAL Y(N),TEMP	MC810490
	INTEGER GAP	MC810500
	INTEGER*2 INDX(N), ITEMP	MC810510
	LOGICAL EXCH	MC810520
C		MC810530
	GAP=(N/2)	MC810540
5	IF (.NOT.(GAP.NE.0)) GO TO 500	MC810550
10	CONTINUE	MC810560
	EXCH=. TRUE.	MC810570
	K=N-GAP	MC810580
	DO 200 I=1,K	MC810590

	KK=I+GAP	MC8106
	IF(.NOT.(Y(I).GT.Y(KK))) GO TO 100	MC8106
	TEMP=Y(I)	MC8106
	Y(I)=Y(KK)	MC8106
	Y(KK)=TEMP	MC8106
	ITEMP=INDX(I)	MC8106
	INDX(I)=INDX(KK)	MC8106
	INDX(KK)=ITEMP	MC8106
	EXCH=.FALSE.	MC8106
100	CONTINUE	MC8106
200	CONTINUE	MC8107
	IF (.NOT.(EXCH)) GO TO 10	MC8107
	GAP=(GAP/2)	MC8107
	GO TO 5	MC8107
500	CONTINUE	MC8107
	RETURN	MC8107
	END	MC8107
C	*****	MC8107
C	SUBROUTINE BKDOWN(PTBL,NPT,PTRTBL,NRC,INDX,MKG,MXX,MXY, * SINV,SY,INV,Y,BKTBL,NBK )	MC8108
C ---	BREAKDOWN AGGREGATED VALUES BY THE 3RD DIMENSION SVC/CS	MC8108
	REAL INV(MXX,MXY),Y(MXX,MXY), SINV(MXX,MXY),SY(MXX,MXY)	MC8108
	INTEGER*2 PTRTBL(MXX, 2), INDX(MXX), MKG(MXX)	MC8108
	INTEGER*2 PTBL(MXX, 3), BKTBL(MXX,3)	MC8108
	REAL*8 TINV,TY	MC8108
	NBK=0	MC8108
C ---	TRAVERSE MKG ARRAY AND BUILD BKTBL	MC8108
	DO 10 I=1,NRC	MC8108
	IF(MKG(I).NE.32767) THEN	MC8109
	ICELL=MKG(I)	MC8109
	ELSE	MC8109
	ICELL=I	MC8109
	ENDIF	MC8109
	IX=INDX(I)	MC8109
	IM=PTRTBL(IX,1)	MC8109
	IY=PTRTBL(IX,2)	MC8109
	CALL BLDBK(ICELL,IM,IY,PTBL,NPT,MXX,BKTBL,NBK)	MC8109
10	CONTINUE	MC8109
C ---	DISPLAY BKTBL PRIOR TO SORTING	MC8110
	WRITE(6,101) (I,(BKTBL(I,J),J=1,3), I=1,NBK)	MC8110
	CALL SORT3(BKTBL,NBK,MXX)	MC8110
	WRITE(6,101) (I,(BKTBL(I,J),J=1,3), I=1,NBK)	MC8110
C ---	SUMMARIZE SINV,SY INTO INV,Y FOR MATCHING ENTRIES IN BKTBL	MC8110
	CALL SUMBK(BKTBL,NBK,MXX,SINV,SY,INV,Y,MXY)	MC8110
	WRITE(6,102) (I,(INV(I,J),J=1,MXY),(BKTBL(I,J),J=1,2), I=1,NBK)	MC8110
	WRITE(6,102) (I,( Y(I,J),J=1,MXY),(BKTBL(I,J),J=1,2), I=1,NBK)	MC8110
101	FORMAT(I4, 3I6)	MC8110
102	FORMAT(I4, 10F7.2,10X,2I4)	MC8110
103	FORMAT(/I5,10F7.2)	MC8110
104	FORMAT( 5X,10F7.2)	MC8110
	END	MC8110
C	*****	MC8110
	SUBROUTINE BLDBK( ICELL,IM,IY,PTBL,NPT,MXX,BKTBL,NBK)	MC8110

	INTEGER*2 PTBL(MXX, 3), BKTBL(MXX,3)	MC811150
C ---	RECORD ALL ENTRIES IN PTBL WITH MATCHING IM,IY IN BKTBL	MC811160
	DO 10 I=1,NPT	MC811170
	IF(PTBL(I,1).EQ. IM .AND. PTBL(I,2).EQ. IY) THEN	MC811180
C ---	INSTALL WITH CELL ID, IW & POINTER	MC811190
	NBK=NBK+1	MC811200
	BKTBL(NBK,1)=ICELL	MC811210
	BKTBL(NBK,2)=PTBL(I,3)	MC811220
	BKTBL(NBK,3)=I	MC811230
	ENDIF	MC811240
10	CONTINUE	MC811250
	END	MC811260
C *****		MC811270
	SUBROUTINE SORT3(T,N,MXX)	MC811280
C ---	INPLACE SORT USING SHELL ALGORITHM *****	MC811290
C ---	SORTS ON 1ST 2 COLS. OF T & DOES SAME REORDERING ON 3RD COLUMN	MC811300
	INTEGER*2 T(MXX,3), ITEMP	MC811310
	INTEGER GAP	MC811320
	LOGICAL EXCH	MC811330
C		MC811340
	GAP=(N/2)	MC811350
5	IF (GAP.EQ.0) GO TO 500	MC811360
10	CONTINUE	MC811370
	EXCH=.FALSE.	MC811380
	K=N-GAP	MC811390
	DO 200 I=1,K	MC811400
	KK=I+GAP	MC811410
	IF(T(I,1).GT. T(KK,1) .OR.	MC811420
*	(T(I,1).EQ. T(KK,1) .AND. T(I,2).GT. T(KK,2)) ) THEN	MC811430
	IT1=T(I,1)	MC811440
	IT2=T(I,2)	MC811450
	IT3=T(I,3)	MC811460
	T(I,1)=T(KK,1)	MC811470
	T(I,2)=T(KK,2)	MC811480
	T(I,3)=T(KK,3)	MC811490
	T(KK,1)=IT1	MC811500
	T(KK,2)=IT2	MC811510
	T(KK,3)=IT3	MC811520
	EXCH=.TRUE.	MC811530
	ENDIF	MC811540
200	CONTINUE	MC811550
	IF (EXCH) GO TO 10	MC811560
	GAP=(GAP/2)	MC811570
	GO TO 5	MC811580
500	CONTINUE	MC811590
	RETURN	MC811600
	END	MC811610
C *****		MC811620
	SUBROUTINE SUMBK(BKTBL,NBK,MXX,SINV,SY,INV,Y,MXY)	MC811630
C ---	CREATE AGGREGATED ARRAYS INV,Y FROM CELL & 3RD DIM. INFO. IN BKTBL	MC811640
	REAL INV(MXX,MXY),Y(MXX,MXY), SINV(MXX,MXY),SY(MXX,MXY)	MC811650
	INTEGER*2 BKTBL(MXX,3)	MC811660
	REAL*8 TINV,TY	MC811670
	IP=0	MC811680
	I1=-1	MC811690
	I2=-1	MC811700

TINV=0	MC8117
TY=0	MC8117
DO 10 I=1,NBK	MC8117
IF(BKTBL(I,1).NE.I1 .OR. BKTBL(I,2).NE.I2) THEN	MC8117
C --- CHANGE OF CELL,IW IDENTIFIERS	MC8117
IP=IP+1	MC8117
I1=BKTBL(I,1)	MC8117
I2=BKTBL(I,2)	MC8117
DO 15 J=1,MXY	MC8117
INV(IP,J)=0	MC8118
Y(IP,J)=0	MC8118
15 CONTINUE	MC8118
BKTBL(IP,1)=I1	MC8118
BKTBL(IP,2)=I2	MC8118
ENDIF	MC8118
C --- ACCUMULATE	MC8118
I3=BKTBL(I,3)	MC8118
DO 20 J=1,MXY	MC8118
INV(IP,J)=INV(IP,J)+SINV(I3,J)	MC8118
Y(IP,J)= Y(IP,J)+ SY(I3,J)	MC8119
TINV=TINV+SINV(I3,J)	MC8119
TY= TY+ SY(I3,J)	MC8119
20 CONTINUE	MC8119
10 CONTINUE	MC8119
WRITE(6,*) '==== TOTAL INV,Y AFTER BREAKDOWN=',TINV,TY	MC8119
C	MC8119
NBK=IP	MC8119
C --- FIX INV. ENTRIES LOWER THAN CORRESP. LOSSES	MC8119
DO 40 I=1,NBK	MC8119
DO 30 J=1,MXY	MC8120
IF(INV(I,J).LT.Y(I,J)) INV(I,J)=Y(I,J)	MC8120
30 CONTINUE	MC8120
40 CONTINUE	MC8120
END	MC8120



## C. ESTIMATION SUBROUTINES

	SUBROUTINE MC87BZ(INV,Y,NRC,NYR,XTB,VXTB,XEB,A,MXX,MXY)	MC800010
C ---	CONDUCTS FIRST FIVE ESTIMATION METHODS	MC800020
C		MC800030
	REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC800040
	REAL XTB(MXX), VXTB(MXX), A(MXX)	MC800050
C		MC800060
	CALL EBTS1(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC800070
	PRINT *, 'COMPLETED EBTS1'	MC800080
C		MC800090
	CALL EBTS2(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC800100
	PRINT *, 'COMPLETED EBTS2'	MC800110
C		MC800120
	CALL EBOS1(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC800130
	PRINT *, 'COMPLETED EBOS1'	MC800140
C		MC800150
	CALL EBOS2(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC800160
	PRINT *, 'COMPLETED EBOS2'	MC800170
C		MC800180
	CALL EMTS(INV,Y,NRC,NYR,XTB,VXTB,XEB,A,MXX,MXY)	MC800190
	PRINT *, 'COMPLETED EMTS'	MC800200
C		MC800210
	END	MC800220
C		MC800230
	*****	MC800240
C		MC800250
	SUBROUTINE EBTS1(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC800260
C ---	TRANSFORMED SCALE, TIME INDEPENDENT VARIANCE METHOD	MC800270
	REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC800280
	REAL XTB(MXX), VXTB(MXX)	MC800290
	REAL MAXL,MINL,L,MAXCHI,MINCHI	MC800300
	INTEGER T, VYR	MC800310
	DATA AA/1.6835/, B1/-.8934/, B2/.9881/	MC800320
	MAXL= -1000.0	MC800330
	MINL= 1000.0	MC800340
	SUML= 0.0	MC800350
	KLSUM=0	MC800360
	MAXCHI= -1000.0	MC800370
	MINCHI= 1000.0	MC800380
	SUMCHI= 0.0	MC800390
	KSUM=0	MC800400
	SUMMAD=0.0	MC800410
	KPSUM=0	MC800420
	WRITE(11,32)' '	MC800430
	WRITE(11,21)'EMP BAYES TRANS SCALE - TIME DEP VAR:'	MC800440
	WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE):'	MC800450
	WRITE(11,28)'FRACTION CELLS','FRACTION MAD'	MC800460
	WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD'	MC800470
	WRITE(11,30)	MC800480
C		MC800490
C ---	LOOP THROUGH VALIDATION YEARS	MC800500
	DO 280 VYR=1, NYR	MC800510
C ---	LOOP THROUGH CELLS	MC800520
	DO 260 IN=1, NRC	MC800530

T=0	MC8005
SUMXT=0	MC8005
SUMVAR=0	MC8005
C --- LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB)	MC8005
DO 200 IT=1, NYR	MC8005
IF(IT .NE. VYR) THEN	MC8005
IF(INV(IN,IT) .NE. 0) THEN	MC8006
X=FTT(INV(IN,IT), Y(IN,IT))	MC8006
C=SQRT(0.5+INV(IN,IT))	MC8006
XX=X+C*(3.141592654/2.0)	MC8006
XT=X/C	MC8006
T=T+1	MC8006
SUMXT=SUMXT+XT	MC8006
IF(XX .LT. 1.001) XX=1.001	MC8006
VARX=AA*(XX**B1)*(XX-1)**B2	MC8006
IF(VARX .GT. 1.0) VARX=1.0	MC8006
VARXT=VARX/(0.5+INV(IN,IT))	MC8007
SUMVAR=SUMVAR+VARXT	MC8007
ENDIF	MC8007
200 CONTINUE	MC8007
XTB(IN)=SUMXT/T	MC8007
VXTB(IN)=SUMVAR/T**2	MC8007
260 CONTINUE	MC8007
C	MC8007
C --- CONDUCT ALGORITHM TO FIND XEB	MC8007
CALL EBITER(NRC,XTB,VXTB,XEB,MXX,VYR)	MC8008
C	MC8008
C --- COMPUTE MEAN SQUARED ERROR	MC8008
CALL MSE(INV,Y,NRC,NYR,VYR,XEB,L,MXX,MXY,KL)	MC8008
IF(L .LT. MINL) THEN	MC8008
MINL=L	MC8008
MINLK=KL	MC8008
MINLYR=VYR	MC8008
ELSE IF(L .GT. MAXL) THEN	MC8008
MAXL=L	MC8008
MAXLK=KL	MC8009
MAXLYR=VYR	MC8009
ENDIF	MC8009
SUML=SUML+L*KL	MC8009
KLSUM=KLSUM+KL	MC8009
C	MC8009
C --- INVERT XEB TO ORIGINAL SCALE	MC8009
CALL INVERT(NRC,XEB,MXX)	MC8009
C	MC8009
C --- COMPUTE MAD AND CHI SQUARE	MC8009
CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,	MC8010
* FCELLU,FMADU,PMAD,KP)	MC8010
IF(CHI .LT. MINCHI) THEN	MC8010
MINCHI=CHI	MC8010
MNCHIK=K	MC8010
MNCHYR=VYR	MC8010
ELSE IF(CHI .GT. MAXCHI) THEN	MC8010
MAXCHI=CHI	MC8010
MXCHIK=K	MC8010
MXCHYR=VYR	MC8010

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        ENDIF
        SUMCHI=SUMCHI+CHI*K
        KSUM=KSUM+K
        KPSUM=KPSUM+KP
        SUMMAD=SUMMAD+PMAD*KP
WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD
280 CONTINUE
C
C --- WRITE RESULTS TO OUTPUT FILE
AVGL=SUML/KLSUM
AVGCHI=SUMCHI/KSUM
AVGMAD=SUMMAD/KPSUM
WRITE(11,19)'AVG MAD = ',AVGMAD
WRITE(11,21)'CHI SQUARE (ORIG SCALE): '
WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYR
WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYR
WRITE(11,26)'AVG CHI = ',AVGCHI
WRITE(11,21)'MEAN SQUARED ERROR (TRANS SCALE): '
WRITE(11,25)'MIN MSE = ',MINL,'K = ',MINLK,'VALID YR = ',MINLYR
WRITE(11,25)'MAX MSE = ',MAXL,'K = ',MAXLK,'VALID YR = ',MAXLYR
WRITE(11,27)'AVG MSE = ',AVGL
19  FORMAT(38X,A,F5.3)
21  FORMAT(/1X,A)
25  FORMAT(1X,A,F6.3,5X,A,I3,5X,A,I2)
26  FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)
27  FORMAT(1X,A,F6.3/)
28  FORMAT(17X,A,2X,A)
29  FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A)
30  FORMAT(1X,8(' - '),2X,4(' - '),2X,14(' - '),2X,13(' - '),2X,5(' - '))
31  FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3)
32  FORMAT(1X,A)
RETURN
END
C
*****
C
SUBROUTINE EBTS2(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)
C --- TRANSFORMED SCALE, TIME INDEPENDENT VARIANCE METHOD
REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)
REAL XTB(MXX), VXTB(MXX)
REAL MAXL,MINL,L,MAXCHI,MINCHI
INTEGER T, VYR
MAXL= -1000.0
MINL= 1000.0
SUML= 0.0
KLSUM=0
MAXCHI= -1000.0
MINCHI= 1000.0
SUMCHI= 0.0
KSUM=0
SUMMAD=0.0
KPSUM=0
WRITE(11,21)'EMP BAYES TRANS SCALE - TIME INDEP VAR: '
WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE): '
WRITE(11,28)'FRACTION CELLS','FRACTION MAD'
WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD'

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WRITE(11,30)	MC8016
C	MC8016
C --- LOOP THROUGH VALIDATION YEARS	MC8016
DO 380 VYR=1, NYR	MC8016
C --- LOOP THROUGH CELLS	MC8017
DO 360 IN=1, NRC	MC8017
T=0	MC8017
SUMXT=0	MC8017
SUMXT2=0	MC8017
C --- LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB)	MC8017
DO 300 IT=1, NYR	MC8017
IF(IT .NE. VYR) THEN	MC8017
IF(INV(IN,IT) .NE. 0) THEN	MC8017
X=FTT(INV(IN,IT), Y(IN,IT))	MC8017
XT=X/SQRT(0.5+INV(IN,IT))	MC8018
T=T+1	MC8018
SUMXT=SUMXT+XT	MC8018
SUMXT2=SUMXT2+XT**2	MC8018
ENDIF	MC8018
ENDIF	MC8018
300 CONTINUE	MC8018
XTB(IN)=SUMXT/T	MC8018
VXTB(IN)=((T*SUMXT2)-(SUMXT**2))/((T-1)*T**2)	MC8018
360 CONTINUE	MC8018
C	MC8019
C --- CONDUCT ALGORITHM TO FIND XEB	MC8019
CALL EBITER(NRC,XTB,VXTB,XEB,MXX,VYR)	MC8019
C	MC8019
C --- COMPUTE MEAN SQUARED ERROR	MC8019
CALL MSE(INV,Y,NRC,NYR,VYR,XEB,L,MXX,MXY,KL)	MC8019
IF(L .LT. MINL) THEN	MC8019
MINL=L	MC8019
MINLK=KL	MC8019
MINLYR=VYR	MC8019
ELSE IF(L .GT. MAXL) THEN	MC8020
MAXL=L	MC8020
MAXLK=KL	MC8020
MAXLYR=VYR	MC8020
ENDIF	MC8020
SUML=SUML+L*KL	MC8020
KLSUM=KLSUM+KL	MC8020
C	MC8020
C --- INVERT XEB TO ORIGINAL SCALE	MC8020
CALL INVERT(NRC,XEB,MXX)	MC8020
C	MC8021
C --- COMPUTE MAD AND CHI SQUARE	MC8021
CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,	MC8021
* FCELLU,FMADU,PMAD,KP)	MC8021
IF(CHI .LT. MINCHI) THEN	MC8021
MINCHI=CHI	MC8021
MNCHIK=K	MC8021
MNCHYR=VYR	MC8021
ELSE IF(CHI .GT. MAXCHI) THEN	MC8021
MAXCHI=CHI	MC8021
MXCHIK=K	MC8022
MXCHYR=VYR	MC8022



ENDIF	MC802220
SUMCHI=SUMCHI+CHI*K	MC802230
KSUM=KSUM+K	MC802240
KPSUM=KPSUM+KP	MC802250
SUMMAD=SUMMAD+PMAD*KP	MC802260
WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD	MC802270
380 CONTINUE	MC802280
C	MC802290
C --- WRITE OUTPUT TO FILE	MC802300
AVGL=SUML/KLSUM	MC802310
AVGCHI=SUMCHI/KSUM	MC802320
AVGMAD=SUMMAD/KPSUM	MC802330
WRITE(11,19)'AVG MAD = ',AVGMAD	MC802340
WRITE(11,21)'CHI SQUARE (ORIG SCALE): '	MC802350
WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYRMC802360	
WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYRMC802370	
WRITE(11,26)'AVG CHI = ',AVGCHI	MC802380
WRITE(11,21)'MEAN SQUARED ERROR (TRANS SCALE): '	MC802390
WRITE(11,25)'MIN MSE = ',MINL,'K = ',MINLK,'VALID YR = ',MINLYR	MC802400
WRITE(11,25)'MAX MSE = ',MAXL,'K = ',MAXLK,'VALID YR = ',MAXLYR	MC802410
WRITE(11,27)'AVG MSE = ',AVGL	MC802420
19 FORMAT(38X,A,F5.3)	MC802430
21 FORMAT(/1X,A)	MC802440
25 FORMAT(1X,A,F6.3,5X,A,I3,5X,A,I2)	MC802450
26 FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)	MC802460
27 FORMAT(1X,A,F6.3/)	MC802470
28 FORMAT(17X,A,2X,A)	MC802480
29 FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A)	MC802490
30 FORMAT(1X,8(' - '),2X,4(' - '),2X,14(' - '),2X,13(' - '),2X,5(' - '))	MC802500
31 FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3)	MC802510
RETURN	MC802520
END	MC802530
C	MC802540
*****	MC802550
C	MC802560
SUBROUTINE EBOS1(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC802570
C --- ORIGINAL SCALE, TIME DEPENDENT VARIANCE METHOD	MC802580
REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC802590
REAL XTB(MXX), VXTB(MXX)	MC802600
REAL MAXCHI, MINCHI	MC802610
INTEGER T, VYR	MC802620
MAXCHI= -1000.0	MC802630
MINCHI= 1000.0	MC802640
SUMCHI= 0.0	MC802650
KSUM=0	MC802660
SUMMAD=0.0	MC802670
KPSUM=0	MC802680
WRITE(11,21)'EMP BAYES ORIG SCALE - TIME DEP VAR: '	MC802690
WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE): '	MC802700
WRITE(11,28)'FRACTION CELLS','FRACTION MAD'	MC802710
WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD'	MC802720
WRITE(11,30)	MC802730
C	MC802740
C --- LOOP THROUGH VALIDATION YEARS	MC802750
DO 480 VYR=1, NYR	MC802760
C --- LOOP THROUGH CELLS	MC802770

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DO 460 IN=1, NRC
  T=0
  SUMXT=0
  SUMVAR=0
C --- LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB)
DO 400 IT=1, NYR
  IF(IT .NE. VYR) THEN
    IF(INV(IN,IT) .NE. 0) THEN
      PHAT=Y(IN,IT)/INV(IN,IT)
      T=T+1
      SUMXT=SUMXT+PHAT
      IF(PHAT .GT. 0.0) THEN
        SUMVAR=SUMVAR+PHAT*(1-PHAT)/INV(IN,IT)
      ELSE
        SUMVAR=SUMVAR+1/(INV(IN,IT)+1)**2
      ENDIF
    ENDIF
  ENDIF
400 CONTINUE
  XTB(IN)=SUMXT/T
  VXTB(IN)=SUMVAR/T**2
460 CONTINUE
C
C --- CONDUCT ALGORITHM TO FIND XEB
CALL EBITER(NRC,XTB,VXTB,XEB,MXX,VYR)
C
C --- COMPUTE MAD AND CHI SQUARE
CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,
*          FCELLU,FMADU,PMAD,KP)
  IF(CHI .LT. MINCHI) THEN
    MINCHI=CHI
    MNCHIK=K
    MNCHYR=VYR
  ELSE IF(CHI .GT. MAXCHI) THEN
    MAXCHI=CHI
    MXCHIK=K
    MXCHYR=VYR
  ENDIF
  SUMCHI=SUMCHI+CHI*K
  KSUM=KSUM+K
  KPSUM=KPSUM+KP
  SUMMAD=SUMMAD+PMAD*KP
WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD
480 CONTINUE
C
C --- WRITE OUTPUT TO FILE
AVGCHI=SUMCHI/KSUM
AVGMAD=SUMMAD/KPSUM
WRITE(11,19)'AVG MAD = ',AVGMAD
WRITE(11,21)'CHI SQUARE (ORIG SCALE): '
WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR
WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR
WRITE(11,27)'AVG CHI = ',AVGCHI
19 FORMAT(38X,A,F5.3)
21 FORMAT(/1X,A)
26 FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)

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27	FORMAT(1X,A,F9.3/)	MC803340
28	FORMAT(17X,A,2X,A)	MC803350
29	FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A)	MC803360
30	FORMAT(1X,8(' - '),2X,4(' - '),2X,14(' - '),2X,13(' - '),2X,5(' - '))	MC803370
31	FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3)	MC803380
	RETURN	MC803390
	END	MC803400
C		MC803410
*****		MC803420
C		MC803430
	SUBROUTINE EBOS2(INV,Y,NRC,NYR,XTB,VXTB,XEB,MXX,MXY)	MC803440
C ---	ORIGINAL SCALE, TIME INDEPENDENT VARIANCE METHOD	MC803450
	REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC803460
	REAL XTB(MXX), VXTB(MXX)	MC803470
	REAL MAXCHI, MINCHI	MC803480
	INTEGER T, VYR	MC803490
	MAXCHI= -1000.0	MC803500
	MINCHI= 1000.0	MC803510
	SUMCHI= 0.0	MC803520
	KSUM=0	MC803530
	SUMMAD=0.0	MC803540
	KPSUM=0	MC803550
	WRITE(11,21)'EMP BAYES ORIG SCALE - TIME INDEP VAR: '	MC803560
	WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE): '	MC803570
	WRITE(11,28)'FRACTION CELLS','FRACTION MAD'	MC803580
	WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD'	MC803590
	WRITE(11,30)	MC803600
C		MC803610
C ---	LOOP THROUGH VALIDATION YEARS	MC803620
	DO 580 VYR=1, NYR	MC803630
C ---	LOOP THROUGH CELLS	MC803640
	DO 560 IN=1, NRC	MC803650
	T=0	MC803660
	SUMXT=0	MC803670
	SUMVAR=0	MC803680
	SUMY=0	MC803690
	SUMINV=0	MC803700
C ---	LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB)	MC803710
	DO 500 IT=1, NYR	MC803720
	IF(IT.NE. VYR) THEN	MC803730
	IF(INV(IN,IT).NE. 0) THEN	MC803740
	PHAT=Y(IN,IT)/INV(IN,IT)	MC803750
	SUMXT=SUMXT+PHAT	MC803760
	SUMY=SUMY+Y(IN,IT)	MC803770
	SUMINV=SUMINV+INV(IN,IT)	MC803780
	T=T+1	MC803790
	SUMVAR=SUMVAR+1.0/INV(IN,IT)	MC803800
	ENDIF	MC803810
	ENDIF	MC803820
500	CONTINUE	MC803830
	XTB(IN)=SUMXT/T	MC803840
	IF(SUMY.GT. 0.0) THEN	MC803850
	PTILDE=SUMY/SUMINV	MC803860
	VXTB(IN)=(PTILDE*(1-PTILDE)*SUMVAR)/T**2	MC803870
	ELSE	MC803880
	VXTB(IN)=SUMINV*SUMVAR/(((1+SUMINV)**2)*T**2)	MC803890



ENDIF	MC8039
560 CONTINUE	MC8039
C	MC8039
C --- CONDUCT ALGORITHM TO FIND XEB	MC8039
CALL EBITER(NRC,XTB,VXTB,XEB,MXX,VYR)	MC8039
C	MC8039
C --- COMPUTE MAD AND CHI SQUARE	MC8039
CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,	MC8039
* FCELLU,FMADU,PMAD,KP)	MC8039
IF(CHI .LT. MINCHI) THEN	MC8039
MINCHI=CHI	MC8040
MNCHIK=K	MC8040
MNCHYR=VYR	MC8040
ELSE IF(CHI .GT. MAXCHI) THEN	MC8040
MAXCHI=CHI	MC8040
MXCHIK=K	MC8040
MXCHYR=VYR	MC8040
ENDIF	MC8040
SUMCHI=SUMCHI+CHI*K	MC8040
KSUM=KSUM+K	MC8040
KPSUM=KPSUM+KP	MC8041
SUMMAD=SUMMAD+PMAD*KP	MC8041
WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD	MC8041
580 CONTINUE	MC8041
C	MC8041
C --- WRITE OUTPUT TO FILE	MC8041
AVGCHI=SUMCHI/KSUM	MC8041
AVGMAD=SUMMAD/KPSUM	MC8041
WRITE(11,19)'AVG MAD = ',AVGMAD	MC8041
WRITE(11,21)'CHI SQUARE (ORIG SCALE): '	MC8041
WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYR	MC8042
WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYR	MC8042
WRITE(11,27)'AVG CHI = ',AVGCHI	MC8042
19 FORMAT(38X,A,F5.3)	MC8042
21 FORMAT(/1X,A)	MC8042
26 FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)	MC8042
27 FORMAT(1X,A,F9.3/)	MC8042
28 FORMAT(17X,A,2X,A)	MC8042
29 FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A)	MC8042
30 FORMAT(1X,8(' - '),2X,4(' - '),2X,14(' - '),2X,13(' - '),2X,5(' - '))	MC8042
31 FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3)	MC8043
RETURN	MC8043
END	MC8043
C	MC8043
*****	MC8043
C	MC8043
SUBROUTINE EMTS(INV,Y,NRC,NYR,XTB,VXTB,XEB,A,MXX,MXY)	MC8043
C --- EFRON-MORRIS METHOD	MC8043
REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC8043
REAL XTB(MXX), VXTB(MXX), A(MXX)	MC8043
REAL MAXL,MINL,L,MAXCHI,MINCHI	MC8044
INTEGER T, VYR	MC8044
DATA AA/1.6835/, B1/-.8934/, B2/.9881/	MC8044
MAXL= -1000.0	MC8044
MINL= 1000.0	MC8044
SUML= 0.0	MC8044



KLSUM=0	MC804460
MAXCHI= -1000.0	MC804470
MINCHI= 1000.0	MC804480
SUMCHI= 0.0	MC804490
KSUM=0	MC804500
SUMMAD=0.0	MC804510
KPSUM=0	MC804520
WRITE(11,21)'EFRON-MORRIS TRANS SCALE - TIME DEP VAR: '	MC804530
WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE): '	MC804540
WRITE(11,28)'FRACTION CELLS','FRACTION MAD'	MC804550
WRITE(11,29)'VALID YR','K','WITH UNDERAGE','FROM UNDERAGE','MAD'	MC804560
WRITE(11,30)	MC804570
C	MC804580
C --- LOOP THROUGH VALIDATION YEARS	MC804590
DO 280 VYR=1, NYR	MC804600
C --- LOOP THROUGH CELLS	MC804610
DO 260 IN=1, NRC	MC804620
T=0	MC804630
SUMXT=0	MC804640
SUMVAR=0	MC804650
C --- LOOP THROUGH YEARS OF DATA TO COMPUTE XTB AND VAR(XTB)	MC804660
DO 200 IT=1, NYR	MC804670
IF(IT .NE. VYR) THEN	MC804680
IF(INV(IN,IT) .NE. 0) THEN	MC804690
X=FTT(INV(IN,IT), Y(IN,IT))	MC804700
C=SQRT(0.5+INV(IN,IT))	MC804710
XX=X+C*(3.141592654/2.0)	MC804720
XT=X/C	MC804730
T=T+1	MC804740
SUMXT=SUMXT+XT	MC804750
IF(XX .LT. 1.001) XX=1.001	MC804760
VARX=AA*(XX**B1)*(XX-1)**B2	MC804770
IF(VARX .GT. 1.0) VARX=1.0	MC804780
VARXT=VARX/(0.5+INV(IN,IT))	MC804790
SUMVAR=SUMVAR+VARXT	MC804800
ENDIF	MC804810
ENDIF	MC804820
200 CONTINUE	MC804830
XTB(IN)=SUMXT/T	MC804840
VXTB(IN)=SUMVAR/T**2	MC804850
260 CONTINUE	MC804860
C	MC804870
C --- CONDUCT ALGORITHM TO FIND XEB	MC804880
CALL EMITER(NRC,XTB,VXTB,XEB,A,MXX,VYR)	MC804890
C	MC804900
C --- COMPUTE MEAN SQUARED ERROR	MC804910
CALL MSE(INV,Y,NRC,NYR,VYR,XEB,L,MXX,MXY,KL)	MC804920
IF(L .LT. MINL) THEN	MC804930
MINL=L	MC804940
MINLK=KL	MC804950
MINLYR=VYR	MC804960
ELSE IF(L .GT. MAXL) THEN	MC804970
MAXL=L	MC804980
MAXLK=KL	MC804990
MAXLYR=VYR	MC805000
ENDIF	MC805010

	SUML=SUML+L*KL	MC8050
	KLSUM=KLSUM+KL	MC8050
C		MC8050
C	--- INVERT XEB TO ORIGINAL SCALE	MC8050
	CALL INVERT(NRC,XEB,MXX)	MC8050
C		MC8050
C	--- COMPUTE MAD AND CHI SQUARE	MC8050
	CALL OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY,	MC8050
	* FCELLU,FMADU,PMAD,KP)	MC8051
	IF(CHI.LT. MINCHI) THEN	MC8051
	MINCHI=CHI	MC8051
	MNCHIK=K	MC8051
	MNCHYR=VYR	MC8051
	ELSE IF(CHI.GT. MAXCHI) THEN	MC8051
	MAXCHI=CHI	MC8051
	MXCHIK=K	MC8051
	MXCHYR=VYR	MC8051
	ENDIF	MC8051
	SUMCHI=SUMCHI+CHI*K	MC8052
	KSUM=KSUM+K	MC8052
	KPSUM=KPSUM+KP	MC8052
	SUMMAD=SUMMAD+PMAD*KP	MC8052
	WRITE(11,31) VYR,KP,FCELLU,FMADU,PMAD	MC8052
280	CONTINUE	MC8052
C		MC8052
C	--- WRITE OUTPUT TO FILE	MC8052
	AVGL=SUML/KLSUM	MC8052
	AVGCHI=SUMCHI/KSUM	MC8052
	AVGMAD=SUMMAD/KPSUM	MC8053
	WRITE(11,19)'AVG MAD = ',AVGMAD	MC8053
	WRITE(11,21)'CHI SQUARE (ORIG SCALE): '	MC8053
	WRITE(11,26)'MIN CHI = ',MINCHI,'K = ',MNCHIK,'VALID YR = ',MNCHYR	MC8053
	WRITE(11,26)'MAX CHI = ',MAXCHI,'K = ',MXCHIK,'VALID YR = ',MXCHYR	MC8053
	WRITE(11,26)'AVG CHI = ',AVGCHI	MC8053
	WRITE(11,21)'MEAN SQUARED ERROR (TRANS SCALE): '	MC8053
	WRITE(11,25)'MIN MSE = ',MINL,'K = ',MINLK,'VALID YR = ',MINLYR	MC8053
	WRITE(11,25)'MAX MSE = ',MAXL,'K = ',MAXLK,'VALID YR = ',MAXLYR	MC8053
	WRITE(11,27)'AVG MSE = ',AVGL	MC8053
19	FORMAT(38X,A,F5.3)	MC8054
21	FORMAT(/1X,A)	MC8054
25	FORMAT(1X,A,F6.3,5X,A,I3,5X,A,I2)	MC8054
26	FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)	MC8054
27	FORMAT(1X,A,F6.3)	MC8054
28	FORMAT(17X,A,2X,A)	MC8054
29	FORMAT(1X,A,4X,A,3X,A,2X,A,3X,A)	MC8054
30	FORMAT(1X,8(' - '),2X,4(' - '),2X,14(' - '),2X,13(' - '),2X,5(' - '))	MC8054
31	FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3)	MC8054
	RETURN	MC8054
	END	MC8055
C		MC8055
	*****	MC8055
C		MC8055
	SUBROUTINE EBITER(NRC,XTB,VXTB,XEB,MXX,VYR)	MC8055
C	--- ITERATIVE ALGORITHM TO SOLVE FOR XEB	MC8055
	REAL XTB(MXX), VXTB(MXX), XEB(MXX)	MC8055
	INTEGER VYR	MC8055

A=0	MC805580
ITER=0	MC805590
100 CONTINUE	MC805600
ITER=ITER+1	MC805610
IF(ITER .GT. 100) PRINT *, 'EBITER GT 100'	MC805620
A0=A	MC805630
SUMALK=0	MC805640
C	MC805650
C --- SUM THE ALPHAS	MC805660
DO 200 I=1,NRC	MC805670
SUMALK=SUMALK+1/(A+VXTB(I))	MC805680
200 CONTINUE	MC805690
C	MC805700
C --- COMPUTE XBB	MC805710
XBB=0	MC805720
DO 300 I=1,NRC	MC805730
ALPHA=1/(A+VXTB(I))	MC805740
GAMMA=ALPHA/SUMALK	MC805750
XBB=XBB+GAMMA*XTB(I)	MC805760
300 CONTINUE	MC805770
C	MC805780
C --- UPDATE VALUE OF A	MC805790
SUMNUM=0	MC805800
SUMDEN=0	MC805810
DO 400 I=1,NRC	MC805820
ALPHA=1/(A+VXTB(I))	MC805830
SUMNUM=SUMNUM+ALPHA*(XTB(I)-XBB)**2	MC805840
SUMDEN=SUMDEN+((XTB(I)-XBB)**2)*ALPHA**2	MC805850
400 CONTINUE	MC805860
A=A-(NRC-1-SUMNUM)/SUMDEN	MC805870
IF(A .LE. 0) THEN	MC805880
A=0	MC805890
GO TO 500	MC805900
ENDIF	MC805910
IF(ABS(A-A0) .GT. 0.0001) GO TO 100	MC805920
500 CONTINUE	MC805930
C	MC805940
C --- ITERATIONS CONVERGED, COMPUTE XEB	MC805950
DO 600 I=1,NRC	MC805960
X=XTB(I)	MC805970
V=VXTB(I)	MC805980
XEB(I)=(A*X)/(A+V)+(V*XBB)/(A+V)	MC805990
600 CONTINUE	MC806000
RETURN	MC806010
END	MC806020
C	MC806030
*****	MC806040
C	MC806050
SUBROUTINE EMITER(NRC,XTB,VXTB,XEM,A,MXX,VYR)	MC806060
C --- ITERATIVE ALGORITHM TO SOLVE FOR XEB FOR EFRON-MORRIS METHOD	MC806070
REAL XTB(MXX), VXTB(MXX), XEM(MXX), A(MXX)	MC806080
INTEGER VYR	MC806090
DO 100 I=1,NRC	MC806100
A(I)=0	MC806110

100	CONTINUE	MC8061
C		MC8061
C	--- SUM THE ALPHAS	MC8061
	SUMALK=0	MC8061
	DO 200 I=1,NRC	MC8061
	SUMALK=SUMALK+1/(A(I)+VXTB(I))	MC8061
200	CONTINUE	MC8061
C		MC8061
C	--- COMPUTE XHAT	MC8062
	XHAT=0	MC8062
	DO 300 I=1,NRC	MC8062
	ALPHA=1/(A(I)+VXTB(I))	MC8062
	GAMMA=ALPHA/SUMALK	MC8062
	XHAT=XHAT+GAMMA*XTB(I)	MC8062
300	CONTINUE	MC8062
311	XHATP=XHAT	MC8062
	I=1	MC8062
333	AP=A(I)	MC8062
	S=(XTB(I)-XHAT)**2	MC8063
C		MC8063
C	--- COMPUTE SN AND SD	MC8063
	SN=0	MC8063
	SD=0	MC8063
	DO 400 J=1,NRC	MC8063
	IF(J .NE. I) THEN	MC8063
	DEN=(A(J)+VXTB(J))**2	MC8063
	SN=SN+((XTB(J)-XHAT)**2-VXTB(J))/DEN	MC8063
	SD=SD+1/DEN	MC8063
	ENDIF	MC8064
400	CONTINUE	MC8064
C		MC8064
C	--- NEWTON-RAPHSON ITERATIONS TO SOLVE FOR A	MC8064
444	AD=A(I)+VXTB(I)	MC8064
	GNUM=S-3*VXTB(I)+SN*AD**2	MC8064
	GDEN=3+SD*AD**2	MC8064
	GPRM=2*AD*SN/GDEN-2*GNUM*AD*SD/GDEN**2	MC8064
	G=GNUM/GDEN	MC8064
	A(I)=A(I)-((A(I)-G)/(1-GPRM))	MC8064
	IF(A(I) .LE. 0.) THEN	MC8065
	A(I)=0.0	MC8065
	I=I+1	MC8065
	IF(I .LE. NRC) THEN	MC8065
	GO TO 333	MC8065
	ELSE	MC8065
	GO TO 555	MC8065
	ENDIF	MC8065
	ENDIF	MC8065
	IF(ABS(A(I)-AP) .LE. 0.0001) THEN	MC8065
	I=I+1	MC8066
	IF(I .LE. NRC) THEN	MC8066
	GO TO 333	MC8066
	ELSE	MC8066
	GO TO 555	MC8066
	ENDIF	MC8066
	ELSE	MC8066
	AP=A(I)	MC8066



GO TO 444	MC806680
ENDIF	MC806690
C	MC806700
C --- TEST FOR CONVERGENCE: ABS(S-SP) LT EPSILON	MC806710
555 SUMALK=0	MC806720
DO 600 J=1,NRC	MC806730
SUMALK=SUMALK+1/(A(J)+VXTB(J))	MC806740
600 CONTINUE	MC806750
XHAT=0	MC806760
DO 700 J=1,NRC	MC806770
ALPHA=1/(A(J)+VXTB(J))	MC806780
GAMMA=ALPHA/SUMALK	MC806790
XHAT=XHAT+GAMMA*XTB(J)	MC806800
700 CONTINUE	MC806810
DO 800 J=1,NRC	MC806820
S=(XTB(J)-XHAT)**2	MC806830
SP=(XTB(J)-XHATP)**2	MC806840
IF(ABS(S-SP) .GT. 0.0001) GO TO 311	MC806850
800 CONTINUE	MC806860
C	MC806870
C --- ITERATIONS CONVERGED, COMPUTE XEM	MC806880
DO 950 K=1,NRC	MC806890
SD=0	MC806900
DO 900 J=1,NRC	MC806910
IF(J .NE. K) SD=SD+1/(A(J)+VXTB(J))**2	MC806920
900 CONTINUE	MC806930
AD=A(K)+VXTB(K)	MC806940
DSTAR=3+(AD**2)*SD	MC806950
B=(1.-4./DSTAR)*VXTB(K)/AD	MC806960
IF(B .GT. 1.0) B=1.0	MC806970
IF(B .LT. 0.0) B=0.0	MC806980
XEM(K)=XHAT+(1-B)*(XTB(K)-XHAT)	MC806990
950 CONTINUE	MC807000
END	MC807010
C	MC807020
*****	MC807030
C	MC807040
SUBROUTINE MSE(INV,Y,NRC,NYR,VYR,XEB,L,MXX,MXY,KL)	MC807050
C --- COMPUTES MEAN SQUARED ERROR MOE	MC807060
REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX)	MC807070
REAL L,MU	MC807080
INTEGER VYR	MC807090
SUMSE=0	MC807100
KL=0	MC807110
DO 100 I=1,NRC	MC807120
IF(INV(I,VYR) .GT. 0.0) THEN	MC807130
X=FTT(INV(I,VYR),Y(I,VYR))	MC807140
MU=X/SQRT(0.5+INV(I,VYR))	MC807150
SUMSE=SUMSE+(XEB(I)-MU)**2	MC807160
KL=KL+1	MC807170
ENDIF	MC807180
100 CONTINUE	MC807190
L=SUMSE/KL	MC807200
RETURN	MC807210
END	MC807220
C	MC807230

```

*****MC8072
C SUBROUTINE OSMOE(INV,Y,NRC,NYR,VYR,XEB,CHI,K,MXX,MXY, MC8072
* FCELLU,FMADU,PMAD,KP) MC8072
C --- COMPUTES MAD AND CHI SQUARE MOES MC8072
REAL INV(MXX,MXY), Y(MXX,MXY), XEB(MXX) MC8072
INTEGER VYR MC8073
CHI=0.0 MC8073
K=0 MC8073
SUMPMO=0.0 MC8073
SUMPMU=0.0 MC8073
KPMO=0 MC8073
KPMU=0 MC8073
DO 100 I=1,NRC MC8073
P=XEB(I) MC8073
E=P*INV(I,VYR) MC8073
A=Y(I,VYR) MC8074
C MC8074
C --- COMPUTE MAD FOR THIS CELL MC8074
IF(INV(I,VYR) .GT. 0.0) THEN MC8074
PA=A/INV(I,VYR) MC8074
IF(P .GT. PA) THEN MC8074
SUMPMO=SUMPMO+(P-PA) MC8074
KPMO=KPMO+1 MC8074
ELSE MC8074
SUMPMU=SUMPMU+(PA-P) MC8074
KPMU=KPMU+1 MC8075
ENDIF MC8075
ENDIF MC8075
C MC8075
C --- COMPUTE CHI SQUARE FOR THIS CELL MC8075
IF(E .NE. 0.0 .AND. P .NE. 1.0) THEN MC8075
K=K+1 MC8075
CHI=CHI+((A-E)**2)/(E*(1-P)) MC8075
ENDIF MC8075
100 CONTINUE MC8075
C MC8076
C --- COMPUTE WEIGHTED AVERAGES MC8076
KP=KPMO+KPMU MC8076
FCELLU=REAL(KPMU)/REAL(KP) MC8076
FMADU=SUMPMU/(SUMPMU+SUMPMO) MC8076
PMAD=(SUMPMU+SUMPMO)/KP MC8076
RETURN MC8076
END MC8076
C MC8076
*****MC80769
C SUBROUTINE INVERT(NRC,XEB,MXX) MC80770
C --- INVERT XEB TO ORIGINAL SCALE MC80772
REAL XEB(MXX) MC80773
DO 100 I=1, NRC MC80774
P=0.5*(1+SIN(XEB(I))) MC80775
IF (P .LT. 0.0) THEN MC80776
P=0.0 MC80777
ELSE IF (P .GT. 1.0) THEN MC80778
P=1.0 MC80779

```

ENDIF	MC807800
XEB(I)=P	MC807810
100 CONTINUE	MC807820
RETURN	MC807830
END	MC807840
C	MC807850
*****	MC807860
C	MC807870
FUNCTION FTT(INV,Y)	MC807880
C --- CONDUCTS FREMAN-TUKEY TRANSFORM	MC807890
REAL INV,Y	MC807900
TEMP =-1. + 2.*Y/(1.+INV)	MC807910
TEMP1=-1. + 2.*(1.+Y)/(1.+INV)	MC807920
IF(ABS(TEMP).GT.1 .OR. ABS(TEMP1).GT.1) THEN	MC807930
WRITE(6,*) 'FTT ERROR INV,Y=',INV,Y,TEMP,TEMP1	MC807940
FTT=1	MC807950
RETURN	MC807960
ENDIF	MC807970
FTT=SQRT(.5+INV)*.5*(ASIN(TEMP) + ASIN(TEMP1))	MC807980
END	MC807990

## D. VECTOR METHOD SUBROUTINE

```

SUBROUTINE MC87V(INV,Y,MXX,NYR,NRC,XTBJI,DELTA,X,XVYR,VYRINV, MC8000
* VYRY,BSTAR,S,GAMMA,XBBJ,EVAL,MXP,MXK,BKTBL,NBK,NSC,NCSR,ISFLAG) MC8000
C --- VECTOR METHOD MC8000
REAL INV(MXX,NYR), Y(MXX,NYR) MC8000
REAL XTBJI(MXP,MXK), DELTA(MXP,MXK), X(MXP,MXK) MC8000
REAL XVYR(MXP,MXK), VYRINV(MXP,MXK), VYRY(MXP,MXK) MC8000
REAL BSTAR(MXP,MXP), S(MXP,MXP), GAMMA(MXP,MXP) MC8000
REAL XBBJ(MXP), EVAL(MXP) MC8000
INTEGER*2 BKTBL(MXX,3) MC8000
C MC8001
REAL MAXL,MINL,L,MAXCHI,MINCHI,MO,MU,MAD MC8001
INTEGER T, VYR, P MC8001
C MC8001
MAXL= -1000.0 MC8001
MINL= 1000.0 MC8001
SUML= 0.0 MC8001
KPSUM=0 MC8001
MAXCHI= -1000.0 MC8001
MINCHI= 1000.0 MC8001
SUMCHI= 0.0 MC8002
KCSUM=0 MC8002
WRITE(11,32)' ' MC8002
WRITE(11,21)'EMP BAYES TRANS SCALE - VECTOR CASE: ' MC8002
IF (ISFLAG.EQ. 1) THEN MC8002
P=NSC MC8002
WRITE(11,21)'VECTOR IS BY SERVICE COMPONENT' MC8002
ELSE MC8002
P=NCSR MC8002
WRITE(11,21)'VECTOR IS BY COMMISSIONING SOURCE' MC8002
ENDIF MC8003
WRITE(11,22)'K=',NRC,'P=',P,'KP= ',(NRC*P) MC8003
WRITE(11,21)'MEAN ABSOLUTE DEVIATION (ORIG SCALE): ' MC8003
WRITE(11,28)'FRACTION CELLS','FRACTION MAD' MC8003
WRITE(11,29)'VALID YR','KP','WITH UNDERAGE','FROM UNDERAGE','MAD' MC8003
WRITE(11,30) MC8003
K=NRC MC8003
IF(K.LE. (P+2)) THEN MC8003
WRITE(6,*)'*** ERROR IN VECTOR CASE: P+2 GT K ***' MC8003
STOP MC8003
ENDIF MC8004
C MC8004
C --- CONDUCT VALIDATION MC8004
DO 999 VYR=1, NYR MC8004
DO 90 J=1,MXP MC8004
DO 80 I=1,MXK MC8004
XTBJI(J,I)=0.0 MC8004
DELTA(J,I)=0.0 MC8004
XVYR(J,I)=0.0 MC8004
80 CONTINUE MC8004
90 CONTINUE MC8005
KMKGB=BKTBL(1,1) MC8005
NRC=1 MC8005
C --- LOOP THROUGH CELLS IN VECTOR FORM MC8005

```



DO 130	I=1,NBK	MC800540
	IF(BKTBL(I,1) .NE. KMKG) NRC=NRC+1	MC800550
DO 100	J=1,P	MC800560
	IF(BKTBL(I,2) .EQ. J) THEN	MC800570
	JP=J	MC800580
	GO TO 110	MC800590
	ENDIF	MC800600
100	CONTINUE	MC800610
	WRITE(6,*) '*** ERROR IN P VECTOR ASSIGNMENT ***'	MC800620
110	T=0	MC800630
	SUMXT=0	MC800640
	SUMVAR=0	MC800650
C ---	LOOP THROUGH YEARS OF DATA TO SOLVE FOR XTB AND VAR(XTB)	MC800660
	DO 120 IT=1, NYR	MC800670
	IF(IT .NE. VYR) THEN	MC800680
	IF(INV(I,IT) .NE. 0) THEN	MC800690
	XIJ=FTTV(INV(I,IT), Y(I,IT))	MC800700
	C=0.5+INV(I,IT)	MC800710
	XT=XIJ/SQRT(C)	MC800720
	SUMXT=SUMXT+XT	MC800730
	SUMVAR=SUMVAR+1/C	MC800740
	T=T+1	MC800750
	ENDIF	MC800760
	ENDIF	MC800770
120	CONTINUE	MC800780
	XTBJI(JP,NRC)=SUMXT/T	MC800790
C ---	STORE VARIANCE MATRIX IN DELTA MATRIX (TEMPORARY)	MC800800
	DELTA(JP,NRC)=SUMVAR/T**2	MC800810
C ---	GET VALIDATION YEAR ESTIMATE, INVENTORY AND ATTRITION INFO	MC800820
	IF(INV(I,VYR) .GT. 0.0) THEN	MC800830
	XIJ=FTTV(INV(I,VYR), Y(I,VYR))	MC800840
	XT=XIJ/SQRT(0.5+INV(I,VYR))	MC800850
	XVYR(JP,NRC)=XT	MC800860
	ENDIF	MC800870
	VYRINV(JP,NRC)=INV(I,VYR)	MC800880
	VYRY(JP,NRC)=Y(I,VYR)	MC800890
	KMKG=BKTBL(I,1)	MC800900
130	CONTINUE	MC800910
	IF(K .NE. NRC) THEN	MC800920
	WRITE(6,*) '*** ERROR IN VECTOR CASE: K NE NRC ***'	MC800930
	ENDIF	MC800940
C		MC800950
C ---	COMPUTE XBB SUB J	MC800960
	DO 210 J=1,P	MC800970
	SUMXTB=0.0	MC800980
	DO 200 I=1,K	MC800990
	SUMXTB=SUMXTB+XTBJI(J,I)	MC801000
200	CONTINUE	MC801010
	XBBJ(J)=SUMXTB/K	MC801020
210	CONTINUE	MC801030
C		MC801040
C ---	COMPUTE X SUB JI MATRIX, MAKE A COPY IN DELTA MATRIX (TEMPORARY)	MC801050
	DO 230 J=1,P	MC801060
	DO 220 I=1,K	MC801070
	X(J,I)=(XTBJI(J,I)-XBBJ(J))*SQRT(DELTA(J,I))	MC801080
	DELTA(J,I)=X(J,I)	MC801090

220	CONTINUE	MC8011
230	CONTINUE	MC8011
C		MC8011
C	--- COMPUTE S MATRIX	MC8011
	CALL MXYTF(P,K,X,MXP,P,K,DELTA,MXP,P,P,S,MXP)	MC8011
C		MC8011
C	--- DO EIGENANALYSIS OF S	MC8011
C	--- PUT EIGENVALUES INTO EVAL, EIGENVECTORS INTO GAMMA	MC8011
	CALL EVCSF(P,S,MXP,EVAL,GAMMA,MXP)	MC8011
C		MC8011
C	--- CREATE ESTAR INVERSE	MC8012
	KP2=K-P-2	MC8012
	DO 240 J=1,P	MC8012
	IF(EVAL(J) .LT. KP2) THEN	MC8012
	EVAL(J)=KP2	MC8012
	ENDIF	MC8012
	EVAL(J)=1.0/EVAL(J)	MC8012
240	CONTINUE	MC8012
	DO 260 I=1,P	MC8012
	DO 250 J=1,P	MC8012
	IF(I .EQ. J) THEN	MC8013
	BSTAR(I,J)=EVAL(J)	MC8013
	ELSE	MC8013
	BSTAR(I,J)=0.0	MC8013
	ENDIF	MC8013
250	CONTINUE	MC8013
260	CONTINUE	MC8013
C		MC8013
C	--- CREATE BSTAR = I - (K-P-2) S TILDE INVERSE	MC8013
	CALL MRRRRR(P,P,GAMMA,MXP,P,P,BSTAR,MXP,P,P,S,MXP)	MC8013
	CALL MXYTF(P,P,S,MXP,P,P,GAMMA,MXP,P,P,BSTAR,MXP)	MC8014
	DO 280 I=1,P	MC8014
	DO 270 J=1,P	MC8014
	BSTAR(I,J)=KP2*BSTAR(I,J)	MC8014
	IF(I .EQ. J) THEN	MC8014
	BSTAR(I,J)=1.0-BSTAR(I,J)	MC8014
	ELSE	MC8014
	BSTAR(I,J)=0.0-BSTAR(I,J)	MC8014
	ENDIF	MC8014
270	CONTINUE	MC8014
280	CONTINUE	MC8015
C		MC8015
C	--- COMPUTE DELTA SUB JI	MC8015
	DO 300 J=1,P	MC8015
	DO 290 I=1,K	MC8015
	X(J,I)=XTBJI(J,I)-XBBJ(J)	MC8015
290	CONTINUE	MC8015
300	CONTINUE	MC8015
	CALL MRRRRR(P,P,BSTAR,MXP,P,K,X,MXP,P,K,XTBJI,MXP)	MC8015
	DO 320 J=1,P	MC8015
	DO 310 I=1,K	MC8016
	DELTA(J,I)=XBBJ(J)+XTBJI(J,I)	MC8016
310	CONTINUE	MC8016
320	CONTINUE	MC8016
C		MC8016
C	--- COMPUTE MSE	MC8016

KP=0	MC801660
SUMSE=0.0	MC801670
DO 340 J=1,P	MC801680
DO 330 I=1,K	MC801690
IF(INV(I,VYR) .GT. 0.0) THEN	MC801700
SUMSE=SUMSE+(DELTA(J,I)-XVYR(J,I))**2	MC801710
KP=KP+1	MC801720
ENDIF	MC801730
330 CONTINUE	MC801740
340 CONTINUE	MC801750
L=SUMSE/KP	MC801760
IF(L .LT. MINL) THEN	MC801770
MINL=L	MC801780
MINLKP=KP	MC801790
MINLYR=VYR	MC801800
ELSE IF(L .GT. MAXL) THEN	MC801810
MAXL=L	MC801820
MAXLKP=KP	MC801830
MAXLYR=VYR	MC801840
ENDIF	MC801850
SUML=SUML+L*KP	MC801860
KPSUM=KPSUM+KP	MC801870
C	MC801880
C --- INVERT DELTA SUB JI BACK TO ORIGINAL SCALE	MC801890
DO 360 J=1,P	MC801900
DO 350 I=1,K	MC801910
PHAT=0.5*(1+SIN(DELTA(J,I)))	MC801920
IF (PHAT .LT. 0.0) THEN	MC801930
PHAT=0.0	MC801940
ELSE IF (PHAT .GT. 1.0) THEN	MC801950
PHAT=1.0	MC801960
ENDIF	MC801970
DELTA(J,I)=PHAT	MC801980
350 CONTINUE	MC801990
360 CONTINUE	MC802000
C	MC802010
C --- COMPUTE CHI SQUARE AND MAD	MC802020
CHI=0.0	MC802030
KCHI=0	MC802040
SUMPMO=0.0	MC802050
SUMPMU=0.0	MC802060
KPMO=0	MC802070
KPMU=0	MC802080
DO 410 J=1,P	MC802090
DO 400 I=1,K	MC802100
PHAT=DELTA(J,I)	MC802110
E=PHAT*VYRINV(J,I)	MC802120
A=VYRY(J,I)	MC802130
IF(VYRINV(J,I) .GT. 0.0) THEN	MC802140
PACT=A/VYRINV(J,I)	MC802150
IF(PHAT .GT. PACT) THEN	MC802160
SUMPMO=SUMPMO+(PHAT-PACT)	MC802170
KPMO=KPMO+1	MC802180
ELSE	MC802190
SUMPMU=SUMPMU+(PACT-PHAT)	MC802200
KPMU=KPMU+1	MC802210

ENDIF	MC8022
ENDIF	MC8022
IF(E.NE.0.0 .AND. PHAT.NE.1.0) THEN	MC8022
KCHI=KCHI+1	MC8022
CHI=CHI+((A-E)**2)/(E*(1-PHAT))	MC8022
ENDIF	MC8022
400 CONTINUE	MC8022
410 CONTINUE	MC8022
KMAD=KPMO+KPMU	MC8023
FCELLU=REAL(KPMU)/REAL(KMAD)	MC8023
FMADU=SUMPMU/(SUMPMU+SUMPMO)	MC8023
PMAD=(SUMPMU+SUMPMO)/KMAD	MC8023
IF(CHI.LT. MINCHI) THEN	MC8023
MINCHI=CHI	MC8023
MNCHIK=KCHI	MC8023
MNCHYR=VYR	MC8023
ELSE IF(CHI.GT. MAXCHI) THEN	MC8023
MAXCHI=CHI	MC8023
MXCHIK=KCHI	MC8024
MXCHYR=VYR	MC8024
ENDIF	MC8024
SUMCHI=SUMCHI+CHI*KCHI	MC8024
KCSUM=KCSUM+KCHI	MC8024
WRITE(11,31) VYR,KMAD,FCELLU,FMADU,PMAD	MC8024
999 CONTINUE	MC8024
AVGL=SUML/KPSUM	MC8024
AVGCHI=SUMCHI/KCSUM	MC8024
WRITE(11,21)'CHI SQUARE (ORIG SCALE): '	MC8024
WRITE(11,26)'MIN CHI = ',MINCHI,'KP = ',MNCHIK,	MC8025
* 'VALID YR = ',MNCHYR	MC8025
WRITE(11,26)'MAX CHI = ',MAXCHI,'KP = ',MXCHIK,	MC8025
* 'VALID YR = ',MXCHYR	MC8025
WRITE(11,26)'AVG CHI = ',AVGCHI	MC8025
WRITE(11,21)'MEAN SQUARED ERROR (TRANS SCALE): '	MC8025
WRITE(11,25)'MIN MSE = ',MINL,'KP = ',MINLKP,'VALID YR = ',MINLYR	MC8025
WRITE(11,25)'MAX MSE = ',MAXL,'KP = ',MAXLKP,'VALID YR = ',MAXLYR	MC8025
WRITE(11,27)'AVG MSE = ',AVGL	MC8025
21 FORMAT(/1X,A)	MC8025
22 FORMAT(1X,3(A,I3,5X))	MC8026
25 FORMAT(1X,A,F6.3,5X,A,I3,5X,A,I2)	MC8026
26 FORMAT(1X,A,F9.3,5X,A,I3,5X,A,I2)	MC8026
27 FORMAT(1X,A,F6.3/)	MC8026
28 FORMAT(17X,A,2X,A)	MC8026
29 FORMAT(1X,A,3X,A,3X,A,2X,A,3X,A)	MC8026
30 FORMAT(1X,8(' - '),2X,4(' - '),2X,14(' - '),2X,13(' - '),2X,5(' - '))	MC8026
31 FORMAT(1X,I5,I8,8X,F5.3,10X,F5.3,6X,F5.3)	MC8026
32 FORMAT(1X,A)	MC8026
WRITE(6,*)'COMPLETED VECTOR CASE'	MC8026
END	MC8027
C	MC8027
*****	MC8027
C	MC8027
FUNCTION FTTV(INV,Y)	MC8027
C --- CONDUCTS FREMAN-TUKEY TRANSFORM	MC8027
REAL INV,Y	MC8027
TEMP =-1. + 2.*Y/(1.+INV)	MC8027



TEMP1=-1. + 2.*(1.+Y)/(1.+INV)	MC802780
IF(ABS(TEMP).GT.1 .OR. ABS(TEMP1).GT.1) THEN	MC802790
WRITE(6,*) 'FTT ERROR INV,Y=', INV,Y,TEMP,TEMP1	MC802800
FTT=1	MC802810
RETURN	MC802820
ENDIF	MC802830
FTTV=SQRT(.5+INV)*.5*(ASIN(TEMP) + ASIN(TEMP1))	MC802840
END	MC802850

## E. EXEC PROGRAM

CP LINK MVS 103 103 RR

ACC 103 K

\*\*\*\*\*

FIL \* CLEAR

FIL 01 K DSN F0968 MCOR87 DATA (RECFM FB LRECL 69 BLOCK 17940

FIL 02 DISK MC87 TEMP

FIL 06 &1 (RECFM FBA LRECL 150

FIL 25 DISK MCLASS PG15 (RECFM F LRECL 25

FIL 27 DISK MCLASS PG17 (RECFM F LRECL 25

FIL 29 DISK MCLASS PG19 (RECFM F LRECL 25

FIL 30 DISK MCLASS PG20 (RECFM F LRECL 25

FIL 31 DISK MCLASS PG21 (RECFM F LRECL 25

FIL 32 DISK MCLASS PG22 (RECFM F LRECL 25

&BEGSTACK

30.0 /\* AVG INV THRESHOLD T \*/

30 /\* NO. CELLS THRESHOLD K \*/

13 /\* MOS (ONLY 1) \*/

4 /\* YCS (ONLY 1) \*/

15 /\* GRADE (ONLY 1) \*/

3 1 2 3 /\* NO. SVC COMPS AND ARRAY(1-REG,2-AUGREG,3-RES,4=1+2,5=ALL \*/

1 16 /\* NO. COMM SRCS AND ARRAY(1-15, 16=ALL)

1 /\* 3RD DIMENSION (0=NONE, 1=SVC, 2=CS)

&END

LOAD MC87 (START CLEAR

## F. SAMPLE DATA FILE

1	2	3	4	5	6	7
--	-	-	-	--	-	----
15	0	1	1	15	1	0.02
15	0	3	2	9	5	0.42
15	0	3	3	9	6	0.75
15	0	3	2	10	4	0.15
15	0	3	1	11	1	0.10
15	0	3	3	10	2	0.15
15	0	3	3	3	1	0.02
15	0	3	3	4	1	0.02
15	0	4	2	9	6	0.87
15	0	4	2	10	2	0.20
15	0	4	3	9	2	0.07
15	0	4	1	11	1	0.10
15	0	4	3	4	2	0.05
15	0	4	3	10	1	0.10
15	0	5	2	9	3	0.27
15	0	5	2	10	2	0.20
15	0	5	1	11	1	0.07
15	0	6	2	9	1	0.02
15	1	2	3	15	1	0.05
15	1	3	1	1	2	0.20
15	1	3	3	15	1	0.05
15	1	3	3	10	1	0.10
15	1	3	3	7	3	0.12
15	1	3	3	3	5	0.30
15	1	3	3	5	2	0.65
15	1	3	3	2	5	0.45
15	1	3	3	9	3	0.12
15	1	3	2	15	1	0.05
15	1	3	1	11	3	0.12
15	1	3	1	10	2	0.10
15	1	3	2	7	1	0.02
15	1	3	3	6	1	0.10
15	1	4	3	5	2	0.12
15	1	4	3	2	5	0.40
15	1	4	2	3	2	0.12
15	1	4	1	1	1	0.02
15	1	4	2	9	2	0.07
15	1	4	3	9	1	0.02
15	1	4	3	7	5	0.25
15	1	4	3	10	1	0.02
15	1	4	3	3	2	0.05
15	1	4	1	10	1	0.02
15	1	4	3	12	1	0.02
15	1	4	2	12	1	0.07

(remaining entries omitted)

### Column descriptions:

- |                       |                             |
|-----------------------|-----------------------------|
| 1 - grade             | 5 - commissioning source    |
| 2 - MOS               | 6 - number of records       |
| 3 - YCS               | 7 - total average inventory |
| 4 - service component |                             |

C ---	PROGRAM TO CREATE INVENTORY DATA FILE BY GRADE	MC8000
	PARAMETER (MXX=20000, MXY=10)	MC8000
C ---	CLASSIF. TABLE: GRADE, MOS, YCS, SVC, CS	MC8000
	INTEGER*2 PTRTBL(MXX, 5), NRECS(MXX)	MC8000
	REAL AINV(MXX)	MC8000
	INTEGER TYPE,YCS,PG,MOS,SEX,CS,EDLV,SVC,MOS1,MOS2,RACE	MC8000
	INTEGER DATA(MXY), SPG	MC8000
	CHARACTER*7 CITLS	MC8000
	DATA AINV/MXX*0./, NRECS/MXX*0/	MC8000
C		MC8001
	WRITE(5,*) 'ENTER PG'	MC8001
	READ(5,*) SPG	MC8001
	WRITE(5,*) 'PG TO USE=',SPG	MC8001
	ICR=0	MC8001
	NRC=0	MC8001
	NG=0	MC8001
	DO 10 I=1,999999	MC8001
	READ(1,100,END=999) TYPE,YCS,PG,MOS,SEX,CS,EDLV,SVC,MOS1,MOS2,	MC8001
*	RACE,CITLS,DATA	MC8001
	ICR=ICR+1	MC8002
C ---	CLASSIFY ALL RECORDS TYPE 0	MC8002
	IF(TYPE.GT.0) GO TO 999	MC8002
C ---	ADD NEW RECORD TO TABLE	MC8002
	IF(PG.EQ.SPG) CALL ADDTBL(PG,MOS,YCS,SVC,CS, DATA,MXY, PTRTBL,	MC8002
*	MXX, NRC,AINV,NRECS)	MC8002
	IF(PG.EQ.SPG) NG=NG+1	MC8002
	IF(MOD(ICR,5000).EQ.0) WRITE(6,*) 'ICR,NRC=',ICR,NRC	MC8002
	10 CONTINUE	MC8002
C		MC8002
	999 CONTINUE	MC8003
	WRITE(6,*) ' '	MC8003
	WRITE(6,*) 'TOTAL RECORDS READ =',ICR	MC8003
	WRITE(6,*) 'TOTAL RECORDS ACCEPTED =',NG	MC8003
	WRITE(6,*) 'TOTAL INVENTORY COMBINATIONS =',NRC	MC8003
	DO 20 I=1,NRC	MC8003
	WRITE(2,101) (PTRTBL(I,J),J=1,5), NRECS(I),AINV(I)	MC8003
	20 CONTINUE	MC8003
	100 FORMAT(3I2,I3,I1,I2,2I1,2I3,I1,A7, 1X, 10I4)	MC8003
	101 FORMAT(I2,I4,I3,I2,I3, I4, F7.2)	MC8003
	END	MC8004
C		MC8004
	SUBROUTINE ADDTBL(PG,MOS,YCS,SVC,CS, DATA,MXY, PTRTBL,MXX, NRC,	MC8004
*	AINV,NRECS)	MC8004
C ---	SET INVENTORY POINTER FOR THIS ENTRY AND ACCUMULATE	MC8004
	INTEGER*2 PTRTBL(MXX, 5), NRECS(MXX)	MC8004
	REAL AINV(MXX)	MC8004
	INTEGER YCS,PG,MOS,CS,SVC	MC8004
	INTEGER DATA(MXY)	MC8004
	MINV=GETINV(PTRTBL, MXX,NRC, PG,MOS,YCS,SVC,CS)	MC8004
	IF(MINV.EQ.0) THEN	MC8005
C ---	NEW COMBINATION	MC8005
	NRC=NRC+1	MC8005
	IF(NRC.GT. MXX) THEN	MC8005
	WRITE(6,*) '*** ERROR - TOO MANY INV. COMBINATIONS',NRC	MC8005
	STOP	MC8005
	ENDIF	MC8005



MINV=NRC	MC800570
PTRTBL(MINV, 1)=PG	MC800580
PTRTBL(MINV, 2)=MOS	MC800590
PTRTBL(MINV, 3)=YCS	MC800600
PTRTBL(MINV, 4)=SVC	MC800610
PTRTBL(MINV, 5)=CS	MC800620
NRECS(MINV)=0	MC800630
ENDIF	MC800640
AI=0	MC800650
DO 110 IT=1,MXY	MC800660
AI=AI + FLOAT(DATA(IT))	MC800670
110 CONTINUE	MC800680
AINV(MINV)=AINV(MINV) + .25*AI/MXY	MC800690
NRECS(MINV)=NRECS(MINV) + 1	MC800700
END	MC800710
C ---	MC800720
FUNCTION GETINV(PTRTBL, MXX,NRC, PG,MOS,YCS,SVC,CS)	MC800730
C --- FIND LOCATION OF MATCHING INVENTORY ENTRY FOR A LOSS	MC800740
INTEGER*2 PTRTBL(MXX, 5)	MC800750
INTEGER YCS,PG,MOS,CS,SVC	MC800760
DO 10 I=1,NRC	MC800770
IF(PTRTBL(I, 1) .EQ. PG .AND.	MC800780
* PTRTBL(I, 2) .EQ. MOS .AND.	MC800790
* PTRTBL(I, 3) .EQ. YCS .AND.	MC800800
* PTRTBL(I, 4) .EQ. SVC .AND.	MC800810
* PTRTBL(I, 5) .EQ. CS ) THEN	MC800820
	MC800830
	MC800840
	MC800850
10 CONTINUE	MC800860
GETINV=0	MC800870
END	MC800880

GETINV=I  
RETURN

## APPENDIX C. SAMPLE OUTPUT

### A. GENERAL

This appendix contains sample output from the computer program. A sample output for test cases one through 30 which use the first five estimation methods is shown in paragraph B. A sample output for the vector test cases is shown in paragraph C. These examples show the output that is produced by the WRITE statements for file definition 11, e.g., WRITE(11,101). The program also contains several WRITE and PRINT statements that provide interactive information to the user via the terminal screen, e.g., WRITE(6,\*), WRITE(5,\*) and PRINT \*. This interactive output is omitted.

### B. SAMPLE OUTPUT (TEST CASES 1-30)

#### TEST CASE INPUT PARAMETERS:

```
INVENTORY THRESHOLD= 30.0      THRESHOLD NO. OF CELLS= 30
MOS= 13      YCS= 4      GRADE= 15
SERVICE COMPONENTS= 1 2 3
COMM SOURCES= 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15
```

#### EXPANSION INFORMATION:

```
ACTUAL NO. OF CELLS USED= 24
MOS GROUP # 1 YCS'S USED=
  4 5
LARGE MOS GROUP #1 YCS'S USED=
  4 5
MAJOR MOS GROUP #1 YCS'S USED=
  4 5
```

#### EMP BAYES TRANS SCALE - TIME DEP VAR:

#### MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS WITH UNDERAGE	FRACTION MAD FROM UNDERAGE	MAD
1	24	0.458	0.478	0.127
2	24	0.250	0.187	0.099
3	24	0.542	0.441	0.098
4	24	0.333	0.375	0.069
5	24	0.417	0.352	0.072
6	24	0.125	0.053	0.082
7	24	0.208	0.138	0.099
8	24	0.417	0.472	0.077
9	24	0.833	0.943	0.181
10	24	0.833	0.952	0.113
				AVG MAD = 0.102

CHI SQUARE (ORIG SCALE):

MIN CHI = 48.590 K = 24 VALID YR = 8  
 MAX CHI = 329.334 K = 24 VALID YR = 9  
 AVG CHI = 98.791

MEAN SQUARED ERROR (TRANS SCALE):

MIN MSE = 0.033 K = 24 VALID YR = 4  
 MAX MSE = 0.205 K = 24 VALID YR = 9  
 AVG MSE = 0.079

EMP BAYES TRANS SCALE - TIME INDEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS WITH UNDERAGE	FRACTION MAD FROM UNDERAGE	MAD
1	24	0.458	0.504	0.127
2	24	0.250	0.204	0.094
3	24	0.583	0.477	0.101
4	24	0.375	0.432	0.071
5	24	0.417	0.396	0.073
6	24	0.083	0.061	0.076
7	24	0.250	0.152	0.094
8	24	0.458	0.517	0.075
9	24	0.792	0.952	0.183
10	24	0.875	0.961	0.118
				AVG MAD = 0.101

CHI SQUARE (ORIG SCALE):

MIN CHI = 45.452 K = 24 VALID YR = 6  
 MAX CHI = 344.445 K = 24 VALID YR = 9  
 AVG CHI = 99.284

MEAN SQUARED ERROR (TRANS SCALE):

MIN MSE = 0.036 K = 24 VALID YR = 4  
 MAX MSE = 0.213 K = 24 VALID YR = 9  
 AVG MSE = 0.078

EMP BAYES ORIG SCALE - TIME DEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS WITH UNDERAGE	FRACTION MAD FROM UNDERAGE	MAD
1	24	0.458	0.478	0.127
2	24	0.250	0.195	0.097
3	24	0.542	0.461	0.093
4	24	0.333	0.397	0.070
5	24	0.417	0.375	0.074
6	24	0.125	0.057	0.079
7	24	0.208	0.161	0.102
8	24	0.417	0.488	0.079
9	24	0.833	0.944	0.185
10	24	0.833	0.952	0.117
				AVG MAD = 0.102

CHI SQUARE (ORIG SCALE):

MIN CHI = 49.207 K = 24 VALID YR = 6  
 MAX CHI = 340.035 K = 24 VALID YR = 9  
 AVG CHI = 100.985

EMP BAYES ORIG SCALE - TIME INDEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS WITH UNDERAGE	FRACTION FROM UNDERAGE	MAD
1	24	0.458	0.479	0.127
2	24	0.250	0.196	0.097
3	24	0.542	0.462	0.093
4	24	0.333	0.399	0.070
5	24	0.417	0.377	0.075
6	24	0.125	0.056	0.079
7	24	0.208	0.161	0.101
8	24	0.417	0.490	0.079
9	24	0.833	0.945	0.185
10	24	0.833	0.953	0.117
				AVG MAD = 0.102

CHI SQUARE (ORIG SCALE):

MIN CHI = 48.836 K = 24 VALID YR = 6  
 MAX CHI = 339.835 K = 24 VALID YR = 9  
 AVG CHI = 100.960

EFRON-MORRIS TRANS SCALE - TIME DEP VAR:

MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	K	FRACTION CELLS WITH UNDERAGE	FRACTION FROM UNDERAGE	MAD
1	24	0.458	0.475	0.126
2	24	0.250	0.172	0.095
3	24	0.583	0.451	0.102
4	24	0.375	0.365	0.076
5	24	0.333	0.348	0.076
6	24	0.083	0.046	0.082
7	24	0.208	0.135	0.098
8	24	0.458	0.469	0.076
9	24	0.708	0.938	0.185
10	24	0.875	0.960	0.115
				AVG MAD = 0.103

CHI SQUARE (ORIG SCALE):

MIN CHI = 46.301 K = 24 VALID YR = 8  
 MAX CHI = 340.712 K = 24 VALID YR = 9  
 AVG CHI = 101.231

MEAN SQUARED ERROR (TRANS SCALE):

MIN MSE = 0.042 K = 24 VALID YR = 4  
 MAX MSE = 0.211 K = 24 VALID YR = 9  
 AVG MSE = 0.080



### C. SAMPLE OUTPUT (VECTOR TEST CASES)

#### TEST CASE INPUT PARAMETERS:

INVENTORY THRESHOLD= 30.0      THRESHOLD NO. OF CELLS= 30  
 MOS= 151      YCS= 7      GRADE= 17  
 SERVICE COMPONENTS= 1 2 3  
 COMM SOURCES= 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15

#### EXPANSION INFORMATION:

ACTUAL NO. OF CELLS USED= 8  
 MOS GROUP # 8 YCS'S USED=  
 7  
 LARGE MOS GROUP #3 YCS'S USED=  
 7  
 MAJOR MOS GROUP #2 YCS'S USED=  
 7

#### EMP BAYES TRANS SCALE - VECTOR CASE:

#### VECTOR IS BY SERVICE COMPONENT

K= 8      P= 3      KP= 24

#### MEAN ABSOLUTE DEVIATION (ORIG SCALE):

VALID YR	KP	FRACTION CELLS WITH UNDERAGE	FRACTION FROM UNDERAGE	MAD
1	24	0.375	0.219	0.186
2	24	0.458	0.375	0.179
3	24	0.458	0.417	0.130
4	24	0.458	0.422	0.127
5	24	0.542	0.708	0.146
6	24	0.292	0.310	0.142
7	24	0.250	0.193	0.126
8	24	0.375	0.434	0.092
9	24	0.458	0.705	0.161
10	24	0.792	0.912	0.202

#### CHI SQUARE (ORIG SCALE):

MIN CHI = 27.827      KP = 24      VALID YR = 8  
 MAX CHI = 165.694      KP = 24      VALID YR = 10  
 AVG CHI = 61.025

#### MEAN SQUARED ERROR (TRANS SCALE):

MIN MSE = 0.089      KP = 24      VALID YR = 8  
 MAX MSE = 0.483      KP = 24      VALID YR = 10  
 AVG MSE = 0.229

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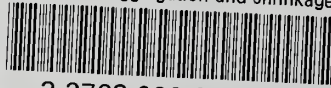
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